

SOFTWARE FOR OPTIMAL DESIGN IN POPULATION PKPD: A COMPARISON

France Mentré¹, Stephen Duffull², Ivelina Gueorguieva³,
Andy Hooker⁴, Sergei Leonov⁵, Kayode
Ogungbenro⁶, Sylvie Retout¹

1. INSERM U738, University Paris 7, Paris, France
2. School of Pharmacy, University of Otago, Dunedin, New Zealand
3. Global PK/PD, Lilly Research Centre, Windlesham, UK
4. Dpt of Pharmaceutical Biosciences, Uppsala University, Uppsala, Sweden
5. GlaxoSmithKline Pharmaceuticals, Collegeville, PA, USA
6. Center for Applied Pharmacokinetic Research, School of Pharmacy, University of Manchester, Manchester, UK

OUTLINE



1. Population design
2. Software tools
3. Comparison
4. Conclusions

1. POPULATION DESIGN

Population PK/PD

- Population PK/PD studies increasingly performed during drug development
- Several methods/software for **maximum likelihood** estimation of population parameters using **NonLinear Mixed Effects Models (NLMEM)**
 - NONMEM
 - Splus/R: nmle, SAS: Proc NLINMIX
 - MCMC estimation methods: SAEM (MONOLIX), MC-PEM,...
- Problem beforehand: choice of **population design**
 - number of patients?
 - number of sampling times?
 - sampling times?
- Recommendations on design in the FDA guidance

Statistical estimation

Statistics:

1. Inference
2. Planning

1. Inference

- hypothesis testing
- **estimation**
- prediction

2. Planning = find 'optimal' design given

- objective (e.g.: estimation)
- statistical method (e.g.: maximum likelihood)
- experimental constraints
- some prior knowledge on expected results (e.g.: models and parameters)

Evaluation of population designs

- Compare designs
 - predicted standard errors of each population parameter
- Optimal design
 - smallest estimation variance
 - greatest information in the data
- Two approaches
 - simulation studies
 - mathematical derivation of the Fisher Information matrix (MF)
 - Cramer-Rao inequality: MF^{-1} is the lower bound of the estimation variance

Fisher Information Matrix

- Problem in NLMEM because no analytical expression of the likelihood
 - Evaluation of MF using first order linearisation
 - first paper: Mentré, Mallet & Baccar, *Biometrika*, 1997
 - (see other references at the end)
- Since first theoretical work
 - Several statistical developments by different teams
 - Applications in drug development, in clinical pharmacology
 - Several software tools

Population Optimum Design of Experiments (PoDe)



■ Creation of a multidisciplinary group: **PODE**

- initiated by Barbara Bogacka (School of Mathematical Sciences, University of London)
- discuss theory of optimum experimental design in NLMEM and their application in drug development

www.maths.qmul.ac.uk/~bb/PODE/PODE2007.html

■ One day workshop

- May 2006: London, University of London (B. Bogacka)
- May 2007: Sandwich, Pfizer (P. Johnson)
 - special session on software tools and their statistical methodology

2. SOFTWARE TOOLS (alphabetical order)

PFIM and PFIM interface



- Developed by Sylvie Retout and France Mentré
 - INSERM & University Paris 7
 - Other participants: Emmanuelle Comets, Hervé Le Nagard, Caroline Bazzoli
- Population Fisher Information Matrix
- Use R
- Available at www.pfim.biostat.fr
- History of PFIM
 - 2001: PFIM 1.1 similar in Splus and Matlab (S. Duffull)
 - 2003: PFIM 2.1 and PFIMOPT 1.0
 - June 2007: PFIM Interface 2.0 (evaluation and optimisation)
 - Soon PFIM 3 (beta version) and PFIM Interface 3

PFIM Interface 2.0



PFIM Interface 2.0 - Exemple B

File Run

Run menu: Evaluation, Optimization

Input design Optimization algorithms Graph

Dose regimen: Identical dose in each elementary design

Dose: 100

Initial population design

Number of groups: 2

Subjects are given as: numbers proportions

Initial population design

| | | | | |
|--|---|--|----|----------------------|
| | + | | -> | 0.0625, 7, 14, 20.58 |
| | | | <- | 0.0625, 12, 20 |

Initial proportions or numbers of subjects per group

| | | |
|--|---|--------|
| | + | 90, 30 |
|--|---|--------|

- Developed by Sergei Leonov
 - Research Statistics Unit, GlaxoSmithKline
 - Other participants: Bob Gagnon, Brian McHugh, Valerii Fedorov
- Sampling Times Allocation - Matlab Platform
- Or STand Alone - Matlab Platform
 - (no need of Matlab)
 - free Matlab Component Runtime environment

- Not available outside GSK

PkStaMP



One-compartment model

PK PARAMETERS

Typical values

| | | |
|-------|------|--|
| Ka | 2.08 | <input checked="" type="checkbox"/> Random |
| Ke CL | 600 | <input checked="" type="checkbox"/> |
| V | 706 | <input checked="" type="checkbox"/> |

Microparameter

Population Covariance (Etas)

| | | |
|------|-------|-------|
| Ka | Ke CL | V |
| 1.22 | 0 | 0 |
| | 0.407 | 0.286 |
| | | 0.90 |

Distribution:

RESIDUAL VARIANCE

Additive 2.6 Proportional 0.598

DOSES

Loading, mg: Repeated:

Maintenance: mg
 Every: h
 To stop at: h

Candidate sampling times

Times:
 Units: Min Delta time:

Forced samples

 Times:

How many samples

Min: Max:

Costs: $C_v + k \cdot C_s$

C_v : C_s :

RESULTS

Optimal sequences:

Weights:

Candidate sequences

| | |
|-----------|-------------------------------|
| Total | <input type="text" value=""/> |
| Processed | <input type="text" value=""/> |
| Iteration | <input type="text" value=""/> |

D-efficiency:

ALGORITHM

Iterations, max:
 Init. sequences:
 Step size, coeff.:
 Weight cut-off:

PopDes

- Developed by Kayode Ogungbenro, Ivelina Gueorguieva and Leon Aarons
 - CAPKR, University of Manchester

- Population Design

- Matlab platform
- Available at www.capkr.man.ac.uk/PopDes
- Since April 2007 (on website)

PopDes

The screenshot displays the PopDes software interface, titled "Untitled". The interface is organized into several panels:

- Design Options:** Contains three groups of radio buttons. The first group has "Individual" and "Population". The second group has "Uniresponse" and "Multiresponse". The third group has "Local" and "Bayesian". A "Select" button is located below these options. At the bottom of this panel is a large "LOAD OPTIMAL DESIGN" button.
- Parameters:** Features a text input field and a "Browse" button. Below this is the "Model" section, which includes a "Library" radio button, a dropdown menu showing "one compartment iv bolus", and an "External" radio button. The "Optimisers" section includes radio buttons for "Exchange" (with a "step size" input field), "Hybrid", and "Simplex". A "SOLVE & SAVE" button is at the bottom of this panel.
- Efficiency:** Contains the "Efficiency of a User Specified Design" section with a "User Design" button, a text input field, a "Browse" button, and a "CALCULATE & SAVE" button. Below this is the "Sampling Windows Calculation" section, which includes a "% Efficiency" input field, a "uniform" dropdown menu, an "Initial Guess of Sampling Windows Half Length" input field, and a "CALCULATE & SAVE" button. The "Sampling Windows Evaluation" section includes the "Efficiency of User Specified Windows" section with a "User Windows" button, a text input field, a "Browse" button, a "uniform" dropdown menu, and a "CALCULATE & SAVE" button.

PopED

- Developed by Andy Hooker, Joakim Nyberg, Mats Karlsson
 - Uppsala University
- Population optimal Experimental Design
- Matlab platform
 - O-matrix with previous versions (University of Washington, Paolo Vicini)
- Matlab version available
 - by request andrew.hooker@farmbio.uu.se
 - soon (July 2007) from www.sourceforge.net
- Previous O-matrix version available
 - depts.washington.edu/rfpk/rd/software_popED.html
 - since March 2003

PopED



PopED Gui optimal_initial.xml

File Optimal Design Help

Main settings

Model name: Theophylline Time and Dose

Model description: Optimization of Theophylline (1 comp model with linear absorption). Optimizing on Dose and Time at the same time. Only PK optimization.

Use log file: log.txt

Design settings | Initial values of model | Function directories | Search parameters | Gradient stepsizes | Sampling Schedule

Optimization settings

Optimization method: D-Optimal

Search Type

- Random Search
- Stochastic Gradient
- Line Search

Tasks to optimize

- Samples per Subject
- Sampling Schedule
- Number of individuals per group
- Covariates
- Other variables

Interpret as zero: 1E-05

Model type:

Design parameters

Use grouping

Number of groups: 3

Max number of samples/group: 3

Min number of samples/group: 1

Num individuals in each group

| | Num individuals |
|----------|-----------------|
| ▶ Group1 | 4 |
| Group2 | 4 |
| Group3 | 4 |

Model size

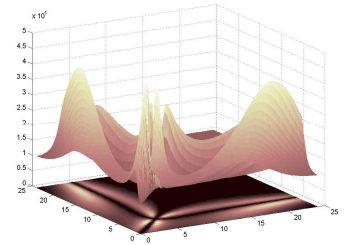
Number bPop in model: 3

Number of random effects in model: 3

Number of covariates in model: 1

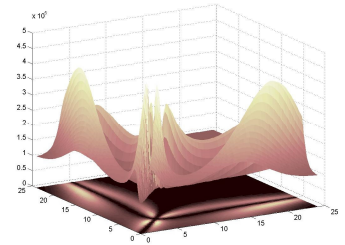
Number of other design-var in model: 0

POPT and WinPOPT



- Developed by Stephen Duffull
 - University of Otago (NZ), University of Queensland, Johnson & Johnson
 - Other participants: Nick Denman, Hui Kimko, John Eccleston
- Matlab platform
- For WinPOPT:
 - stand alone version (no need of Matlab)
 - free Matlab Component Runtime environment
- Available at www.winpopt.com
- POPT: since July 2003
- WinPOPT: since March 2006

WinPOPT



WinPOPT: Optimization for Population PKPD Study Design

File Options Help

Problem name:

Model Details

Single Model Single Response
 Single Model Multiple Response
 Multiple Models Single Response

Model:

Design Details

Number of groups:

Method

Evaluate
 Optimization
 Sampling Windows

This software program was developed with the financial support of Johnson & Johnson Pharmaceutical Research & Development, L.L.C

3. COMPARISON

Summary done by France Mentré from slides at PoDe2007 based on currently available versions (June 2007)

Language, availability, interface, models...

| | PFIM | PFIM Int. | PkStaMP | PopDes | PopED | POPT | WinPOPT |
|-----------------------|-------------|------------------|------------------|----------------|----------------------------------|---------------|------------------|
| Authors | Retout | Retout | Leonov | Ogungben ro | Hooker | Duffull | Duffull |
| Language | R | R | Matlab CR | Matlab | Matlab O matrix | Matlab | Matlab CR |
| Available on website | Yes | Yes | No | Yes | Yes | Yes | Yes |
| GUI | No | Yes | Yes | Yes | Yes | No | Yes |
| Library of PK models | No | Yes | Yes | Yes | Yes | Yes | Yes |
| Multi response models | No* | No* | Yes | Yes | Yes | Yes | Yes |

Evaluation of information matrix

| | PFIM | PFIM Int. | PkStaMP | PopDes | PopED | POPT | WinPOPT |
|---------------------------------|------|-----------|---------|--------|-------|------|---------|
| Analytical derivatives | Yes | Yes | No | No | Yes | No | No |
| ODE Models | No | Yes | No | Yes | Yes | Yes | Yes |
| Off-diagonal terms in MF | Yes | No | Yes | Yes | Yes | No | No |
| Full covariance matrix Ω | No | No | Yes | Yes | No | No | No |
| Designs differ across responses | - | - | No | Yes | Yes | Yes | Yes |

Optimisation

| | PFIM | PFIM Int. | PkStaMP | PopDes | PopED | POPT | WinPOPT |
|----------------------|------------------------------|------------------------------|-------------------|--------------------|------------------------|------------------------------------|------------------------------------|
| Exact Design | Yes | Yes | Yes | Yes | Yes | Yes | Yes |
| Statistical Design | Yes | Yes | Yes | No | No | Yes | No |
| Constraints | Yes | Yes | Yes | Yes | Yes | Yes | Yes |
| Algorithm | Simplex Fedorov - Wynn | Simplex Fedorov - Wynn | Fedorov - Wynn | Simpex Exchange | Stochastic gradient | Simulated annealing Exchange | Simulated annealing Exchange |
| Design Structure | Yes | Yes | Yes | Yes | Yes | Yes | No |
| Bayesian design (ED) | No | No | No | No | Yes | Yes | No |
| Sampling Windows | No | No | No | Yes | Yes | Yes | Yes |

Future developments

- All software tools have ongoing development that should fill the gap with the others
- Some have other specific features
 - See documentation or slides at PoDe2007
- Other statistical developments
 - Models with covariates
 - Models with inter-occasion variability
 - ...
- Main limitation
 - First-order approximation
 - simulation results: closer to FOCE and SAEM than to FO
 - Exact evaluation of MF: stochastic approach or Gaussian quadrature

4. CONCLUSIONS

Conclusion of PoDe2007 Meeting



1. Start a distribution list: PopDesign

- organised by S. Duffull
- to register: <http://lists.otago.ac.nz/listinfo/popdesign>
- to send an email: popdesign@lists.otago.ac.nz
- any questions/comments on design in NLMEM and software tools
- answers by all members of PoDe

2. Start a discussion ‘Would it be possible to combine all software tools in one for future developments?’

- to be organised by A. Hooker & F. Mentré
- role of nlme consortium?

Conclusion

- Results of population PK/PD analyses increasingly used
 - in drug labeling
 - in test of covariates
 - for clinical trial simulation

→ Informative studies with small estimation error

- Evaluation and comparison of population designs without simulation using statistical approach
- Results show that design may CONSIDERABLY affect precision of estimation

SPARSE-SAMPLING DESIGN = BEST INFORMATION NEEDED

- Several software tools available: no excuses!
 - define good population designs (ethical/financial reasons)
 - anticipate fatal population designs

Several Methodological References (1)

■ PFIM

- Mentré F, Mallet A, Baccar D. Optimal design in random-effects regression models. *Biometrika*, 1997, 84: 429-442.
- Mentré F, Dubruc C, Thénot JP. Population pharmacokinetic analysis and optimization of the experimental design for mizolastine solution in children. *J Pharmacokinet Pharmacodyn*, 2001, 28:299-319.
- Retout S, Duffull S, Mentré F. Development and implementation of the population fisher information matrix for evaluation of population pharmacokinetic designs. *Comput Methods Programs Biomed*, 2001, 65: 141-151.
- Retout S, Mentré F, Bruno R. Fisher information matrix for nonlinear mixed-effects models: evaluation and application for optimal design of enoxaparin population pharmacokinetics. *Stat Med*, 2002, 21: 2623-2639.
- Duffull S, Retout S, Mentré F. The use of simulated annealing for finding optimal population designs. *Comput Methods Programs Biomed*, 2002, 69: 25-35.
- Retout S, Mentré F. Further developments of the Fisher information matrix in nonlinear mixed-effects models with evaluation in population pharmacokinetics. *J Biopharm Stat*, 2003, 13: 209-227.
- Retout S, Mentré F. Optimisation of individual and population designs using Splus. *J Pharmacokinet Pharmacodyn*, 2003, 30: 417-443.
- Retout S, Comets E, Samson A, Mentré F. Design in nonlinear mixed effects models: optimization using the Fedorov-Wynn algorithm and power of the Wald test for binary covariates. *Stat Med*, 2007 (in press).

Several Methodological References (2)

■ PkStaMP

- Fedorov VV, Gagnon R, Leonov S. Design of experiments with unknown parameters in variance. *Appl Stoch Models Bus Ind*, 2002,18: 207-218.
- Fedorov VV, Leonov S. Response driven designs in drug development. In: Wong WK, Berger M (Eds). *Applied Optimal Designs*. Wiley: Chichester, 2005, pp.103-136.
- Gagnon R, Leonov S. Optimal population designs for PK models with serial sampling. *J Biopharm Stat*, 2005, 15:143-163.
- Fedorov VV, Gagnon R, Leonov S, Wu Y. Optimal design of experiments in pharmaceutical applications. In: Dmitrienko A, Chuang-Stein C, D'Agostino R. (Eds.), *Pharmaceutical Statistics Using SAS: A Practical Guide*, SAS Press, Cary, NC, 2007, pp. 151-195.

Several Methodological References (3)

■ PopDES

- Ogungbenro K, Graham G, Gueorguieva I, Aarons L. The use of a modified Fedorov exchange algorithm to optimise sampling times for population pharmacokinetic experiments. *Comput Methods Programs Biomed*, 2005, 80: 115-125.
- Gueorguieva I, Aarons L, Ogungbenro K, Jorga KM, Rodgers T, Rowland M. Optimal design for multivariate response pharmacokinetic models. *J Pharmacokinet Pharmacodyn*, 2006, 33: 97-124.
- Gueorguieva I, Ogungbenro K, Graham G, Glatt S, Aarons L. A program for individual and population optimal design for univariate and multivariate response pharmacokinetic-pharmacodynamic models. *Comput Methods Programs Biomed*, 2007, 86: 51-61.
- Ogungbenro K, Gueorguieva I, Majid O, Graham G, Aarons L. Optimal design for multiresponse pharmacokinetic-pharmacodynamic models: dealing with unbalanced designs. *J Pharmacokinet Pharmacodyn*, 2007, 34: 313-331.
- Ogungbenro K, Graham G, Gueorguieva I, Aarons L. Incorporating Correlation in Interindividual Variability for the Optimal Design of Multiresponse Pharmacokinetic Experiments. *J Biopharm Stat*, 2007 (in press).

Several Methodological References (4)

■ PopED

- Hooker A, Foracchia M, Dodds MG, Vicini P. An evaluation of population kinetic d-optimal designs via pharmacokinetic simulations. *Ann Biomed Eng*, 2003, 31: 98-111.
- Foracchia M, Hooker A, Vicini P, Ruggeri A. PopED, a software for optimal experimental design in population kinetics. *Comput Methods Programs Biomed*, 2004, 74: 29-46.
- Hooker A, Vicini P. Simultaneous population optimal design for pharmacokinetic-pharmacodynamic experiments. *AAPS J*, 2005, 7: 758-785.
- Dodds MG, Hooker A, Vicini P. Robust population pharmacokinetic experiment design. *J Pharmacokinet Pharmacodyn*, 2005, 32:33-64.

Several Methodological References (5)

■ POPT/ WinPOPT

- Duffull SB, Mentré F, Aarons L. Optimal design of a population pharmacodynamic experiment for ivabradine. *Pharm Res*, 2001, 18:83-89.
- Green B, Duffull SB. Prospective evaluation of a D-optimal designed population pharmacokinetic study. *J Pharmacokinetic Pharmacodyn*, 2003, 30:145-161
- Duffull SB, Waterhouse TH, Eccleston JA. Some considerations on the design of population pharmacokinetic studies. *J Pharmacokinetic Pharmacodyn*, 2005, 32:441-457.
- Waterhouse TH, Redmann S, Duffull SB, Eccleston JA. Optimal design for model discrimination and parameter estimation for itraconazole population pharmacokinetics in cystic fibrosis patients. *J Pharmacokinetic Pharmacodyn*, 2005, 32:521-545.
- Mould D, Denman N, Duffull SB. Using disease progression models as a tool to detect drug effect. *Clin Pharmacol Ther*, 2007, 82:81-86.
- Hennig S, Waterhouse TH, Bell SC, France M, Wainwright CE, Miller H, Charles BG, Duffull SB. A D-optimal designed population pharmacokinetic study of oral itraconazole in adult cystic fibrosis patients. *Br J Clin Pharmacol*, 2007 (in press).