

Simulated Model Based Adaptive Optimal Design using FDA Stopping Criteria.

- An Adults to Children Bridging Study Example

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Background

In traditional design, the size of the study population is regularly determined *a priori* using power calculations.

Wang *et al.* has previously suggested a precision criteria for sample size determinations for design of pediatric PK studies[1].

Background

Precision Criteria

“The study must be prospectively powered to target a 95% CI [confidence interval] within 60% and 140% of the geometric mean estimates of clearance and volume of distribution for DRUG NAME in each pediatric sub-group with at least 80% power.”

[1] Yaning Wang *et al.* “Clarification on precision criteria to derive sample size when designing pediatric pharmacokinetic studies.”

J Clin Pharmacol 2012;52:1601-1606

Background

Sample size (and design) will be dependent on source of prior information on variability.[2]

Design performance will be dependent on prior information.

Model based adaptive optimal design (MBAOD) has been shown to be **less sensitive to initial misspecification** in the design stage [3].

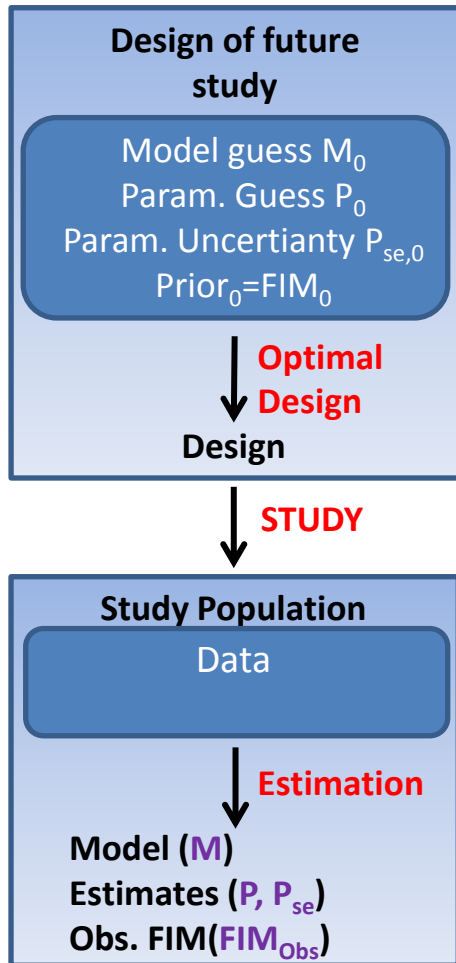
[2] Salem *et al.* 2014, [3] Maloney *et al.* 2007

Implement the **precision criteria** as a **stopping criteria** in the **MBAOD R-Package**[4].

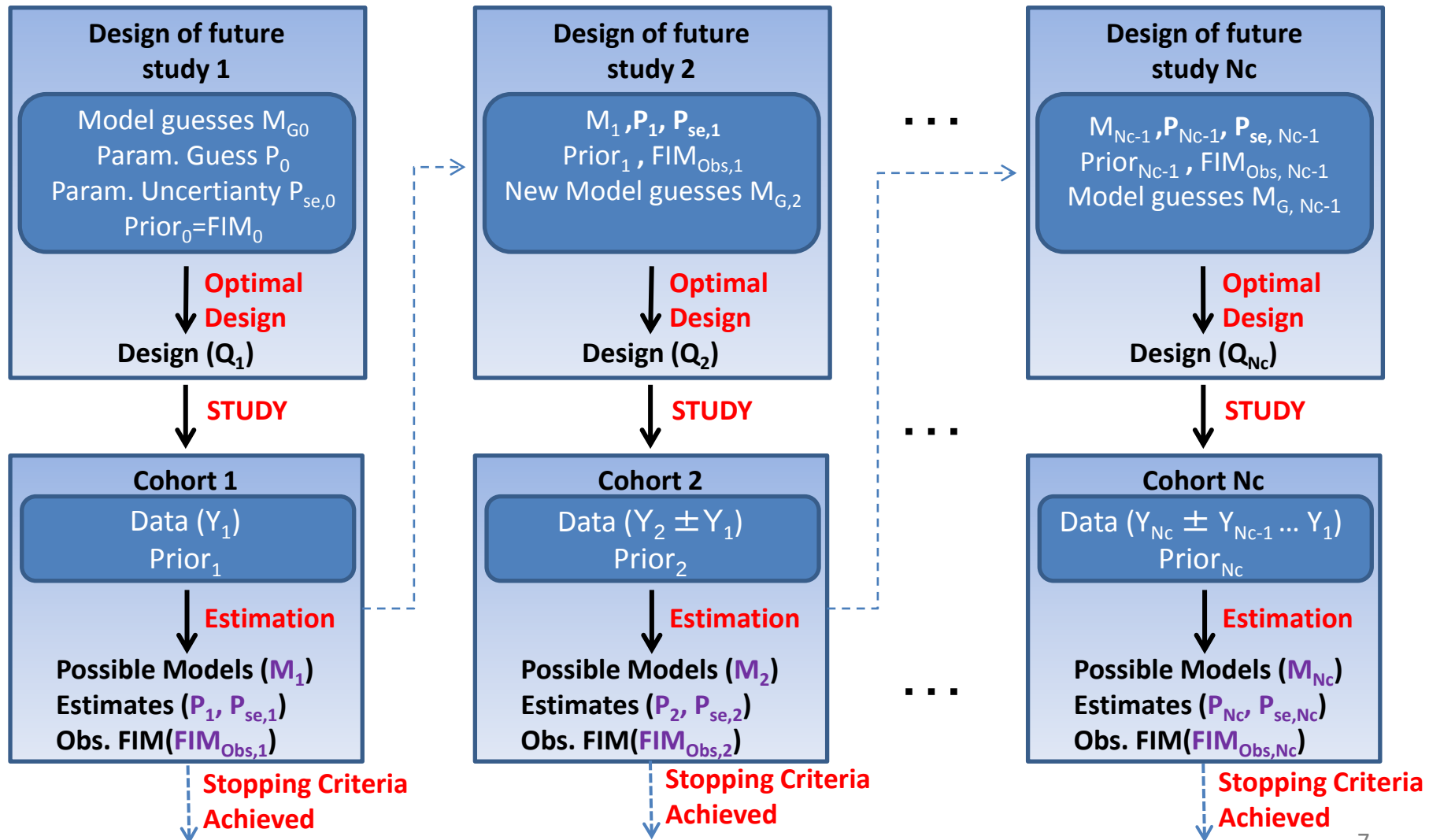
In 100 simulated adult to children PK bridging studies:

Compare the **sample size** of the **MBAOD** simulations with standard **Optimal Design** and **sample size estimation** according to **Wang *et al.***

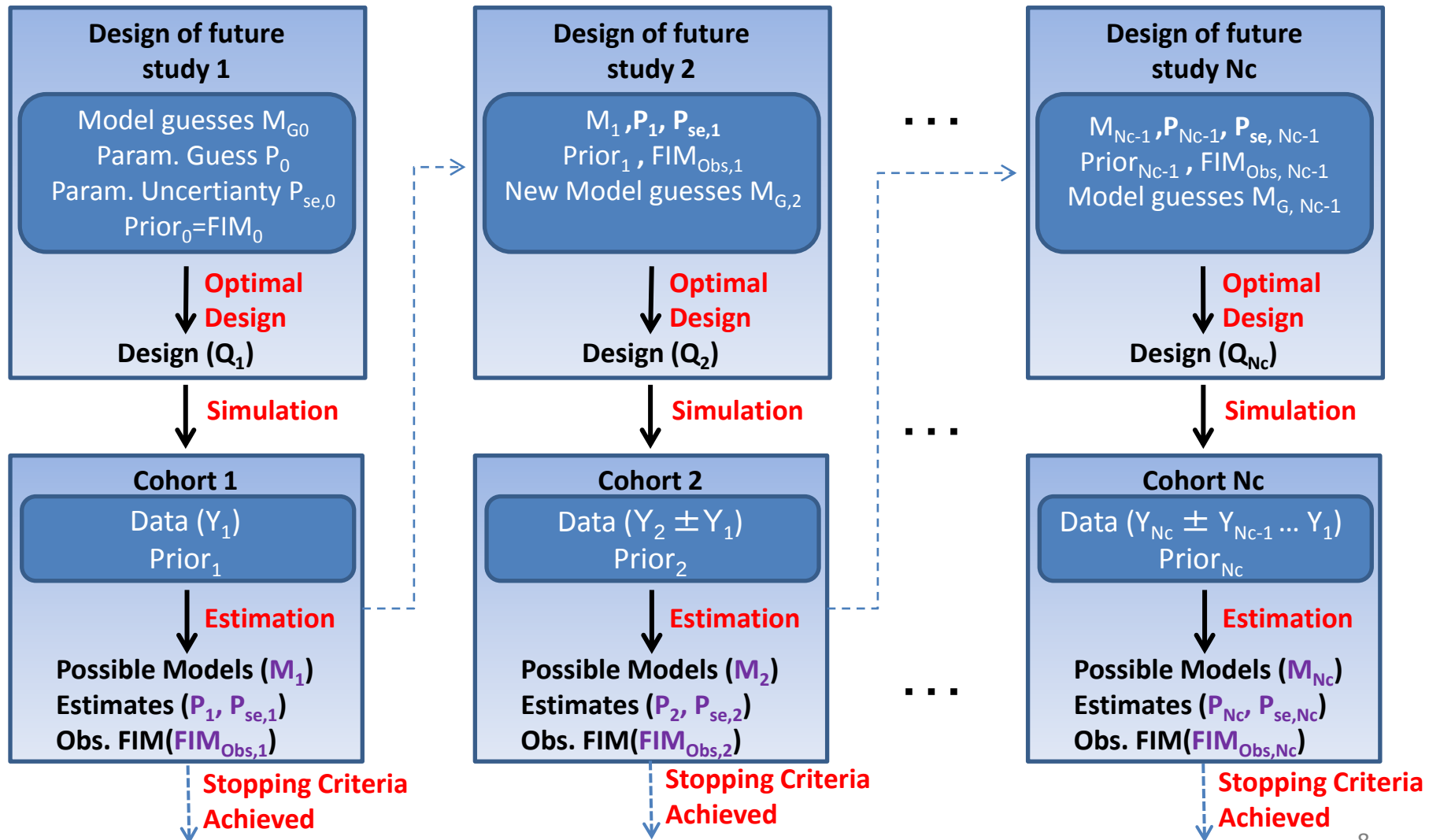
Optimal Design



Adaptive Optimal Design



Adaptive Optimal Design



The Simulated Study Population

Age Group	Age Range	PMA Range [Weeks]	Sub Groups PMA [5]	Sub Groups WT [5]
1	3 - <6 mo	53.05 - <66.1	$a_{1,1}$	$wt_{1,1}$
2	6 - <12 mo	66.1 - <92.2	$a_{2,1}$	$wt_{2,1}$
3	1 - < 2 y	92.2 - <144.4	$a_{3,1}$	$wt_{3,1}$
4	2 - <6 y	144.4 - <353.3	$a_{4,1} \dots a_{4,5}$	$wt_{4,1} \dots wt_{4,5}$
5	6 - <12 y	353.3 - <666.5	$a_{5,1} \dots a_{5,6}$	$wt_{5,1} \dots wt_{5,6}$
6	12 - 18 y	666.5 - <1031.9	$a_{6,1} \dots a_{6,7}$	$wt_{6,1} \dots wt_{6,7}$
7	20 - 29 y	1084 - 1553.8	$a_{7,1} \dots a_{7,10}$	$wt_{7,1} \dots wt_{7,10}$

PMA: Post Menstrual Age

[5] Fryar *et al.* "Anthropometric reference data for children and adults: United States, 2007–2010." National Center for Health Statistics. Vital Health Stat 11(252). 2012.

PK Model and Parameter Scaling

PK Model

$$Dose = 1000 \frac{WT}{70}$$

$$C = \frac{Dose}{V} e\left(-\frac{CL}{V}t\right)$$

TM50: Maturation Half-life

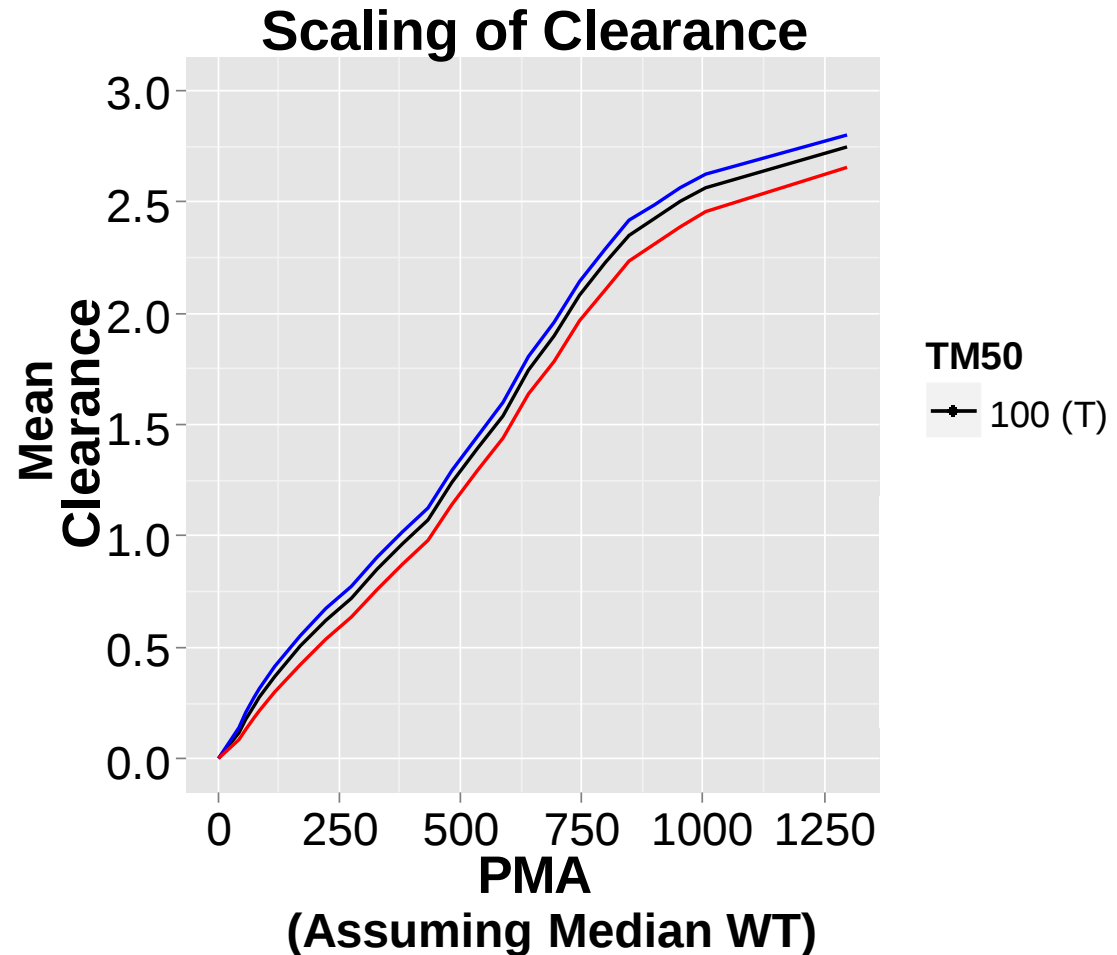
Parameter Scaling

$$CL = CL_A \left(\frac{WT}{70}\right)^{0.75} \left(\frac{PMA}{PMA + TM50}\right)$$

$$V = V_A \left(\frac{WT}{70}\right)^1$$

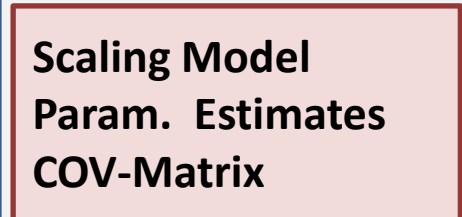
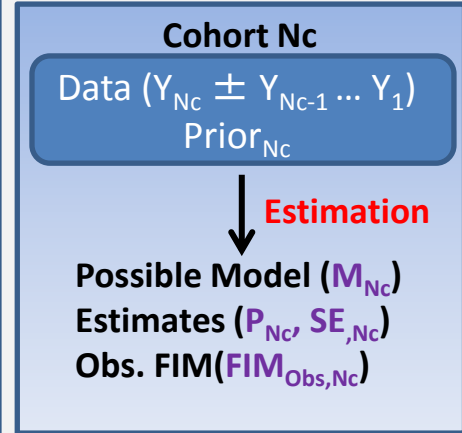
Parameters and Misspecification

Parameter	Value
Fixed Effects	
$\theta (CL_A)$	2.72
$\theta (V_A)$	20.1
$\theta (TM50)$	100 75 150
Random Effects	
$\omega^2 (CL_A)$	0.05
$\omega^2 (V_A)$	0.05
$\sigma^2 (\text{Prop})$	0.015
$\sigma^2 (\text{Add})$	0.0001 FIX

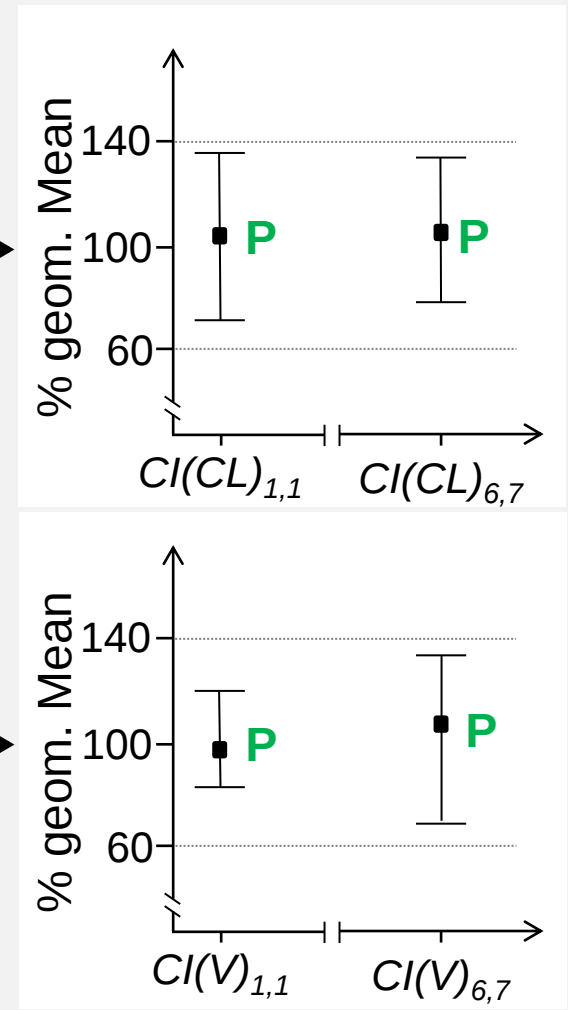
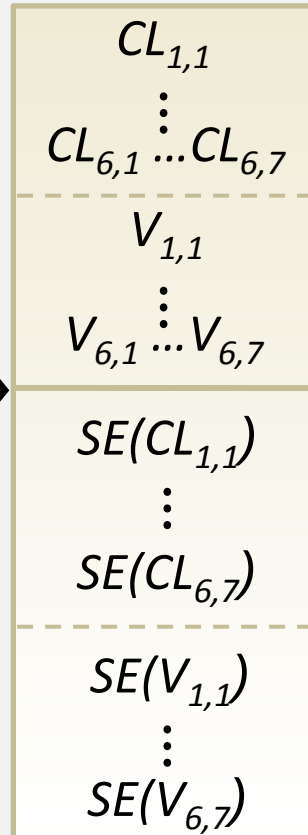
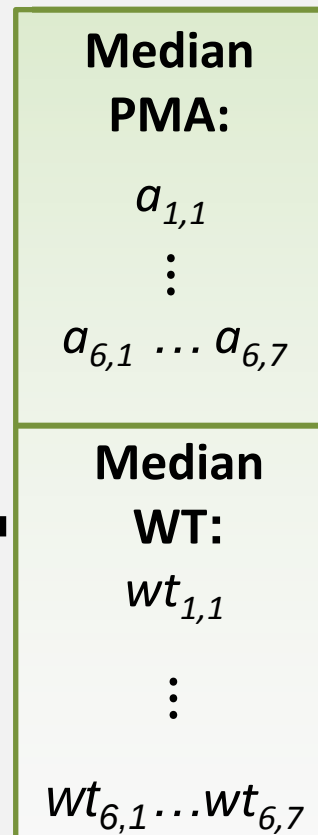


Stopping Criteria

Age Groups 1: 6 All Sub Groups

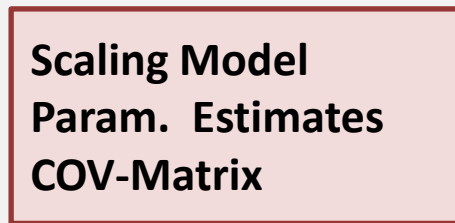
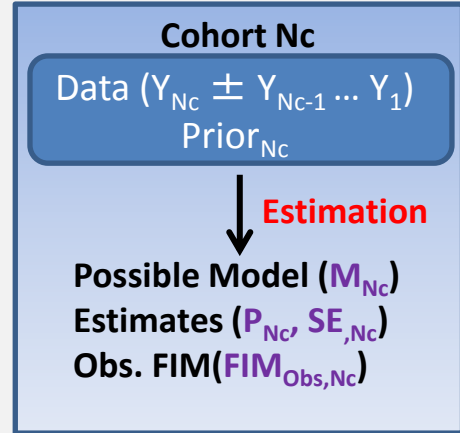


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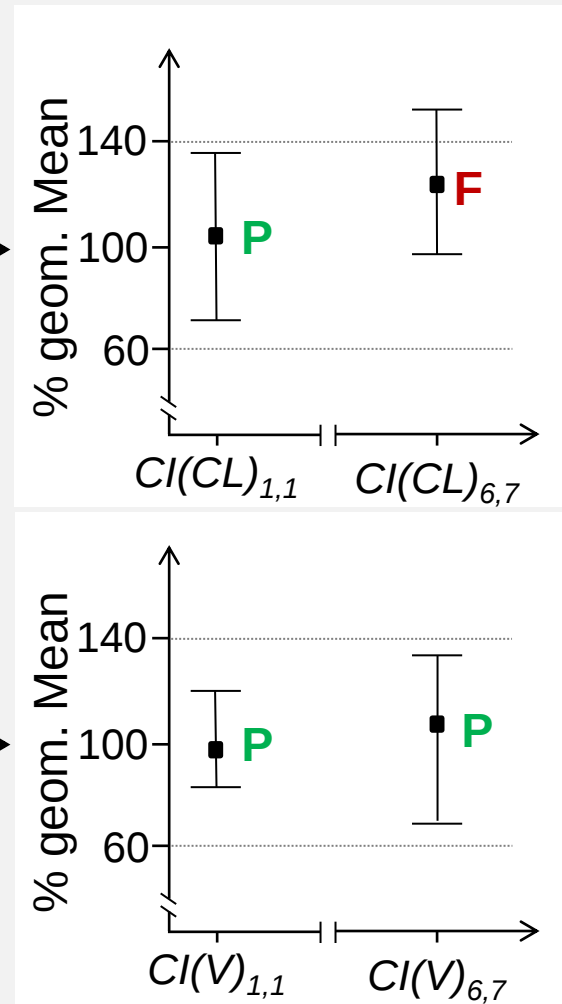
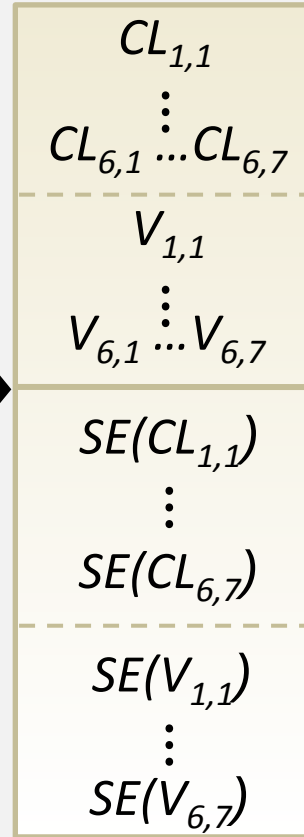
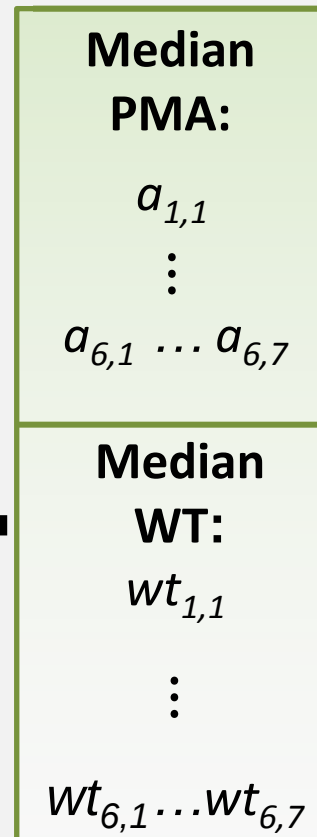


Stopping Criteria

Age Groups 1: 6 All Sub Groups



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Optimal Design

MBAOD

OD

Prior Information:

Simulated Data from 100 Adults

Initial Design:

9 children in the optimal age group
Fixed sampling schedule.

Optimized variable:

Age group from which to **add 2 children** to the study

Design Approaches

Sample Size Estimation

Adult
SD

Scaling
of CL, V

Two estimates of variability:

SD of Adult CL_i and V_i for all
ped. age groups

SD of scaled parameters for
each age group

Design Approaches

Optimal Design

MBAOD

1

OD

2

Power Calculations

Adult
SD

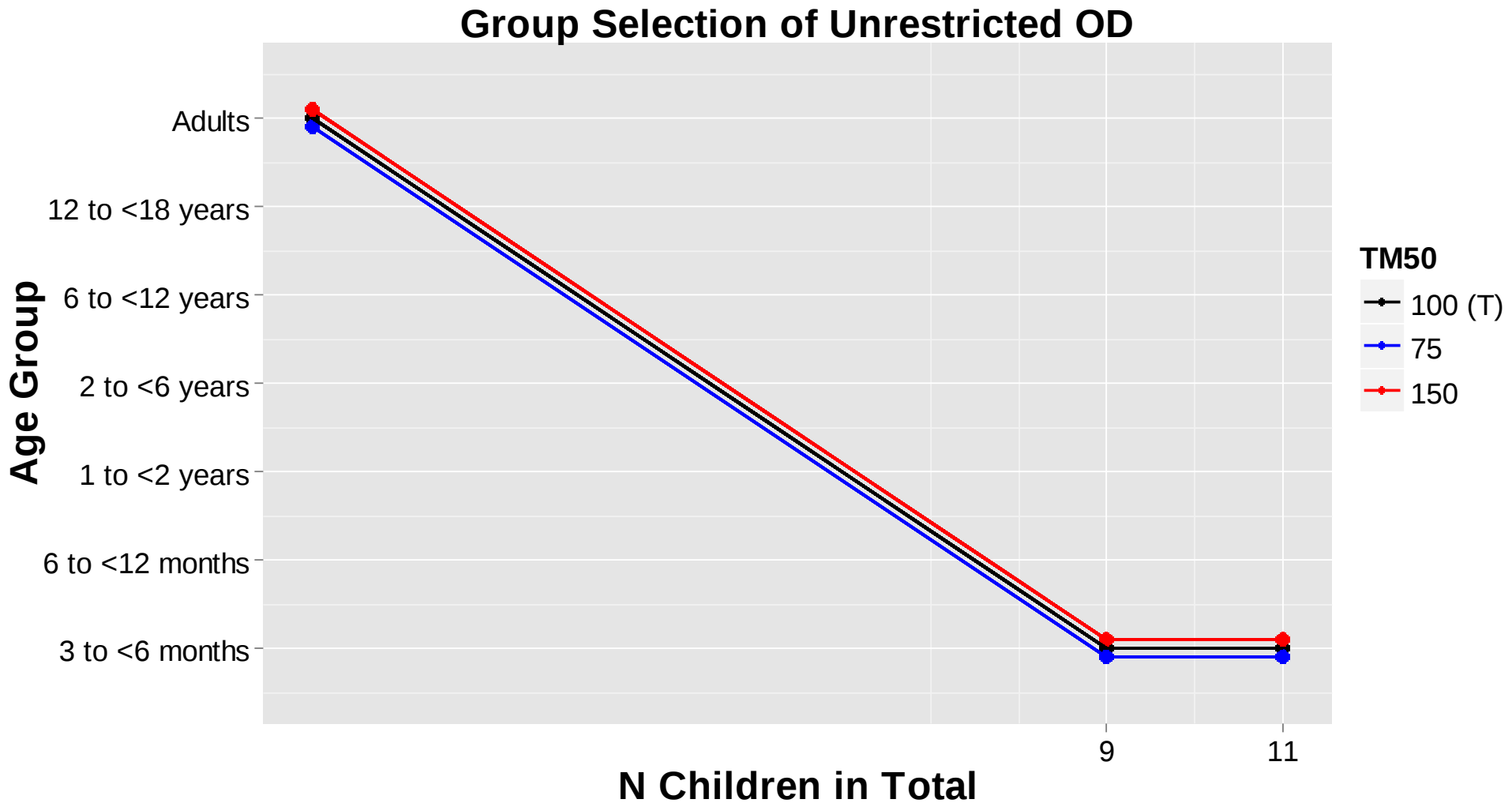
3

Scaling
of CL, V

4

True power to reach the stopping criteria was evaluated for the non-adaptive designs using simulations and estimations.

Restriction of Age Group Inclusion



Restriction of Age Group Inclusion

Initial Design (1st Cohort):

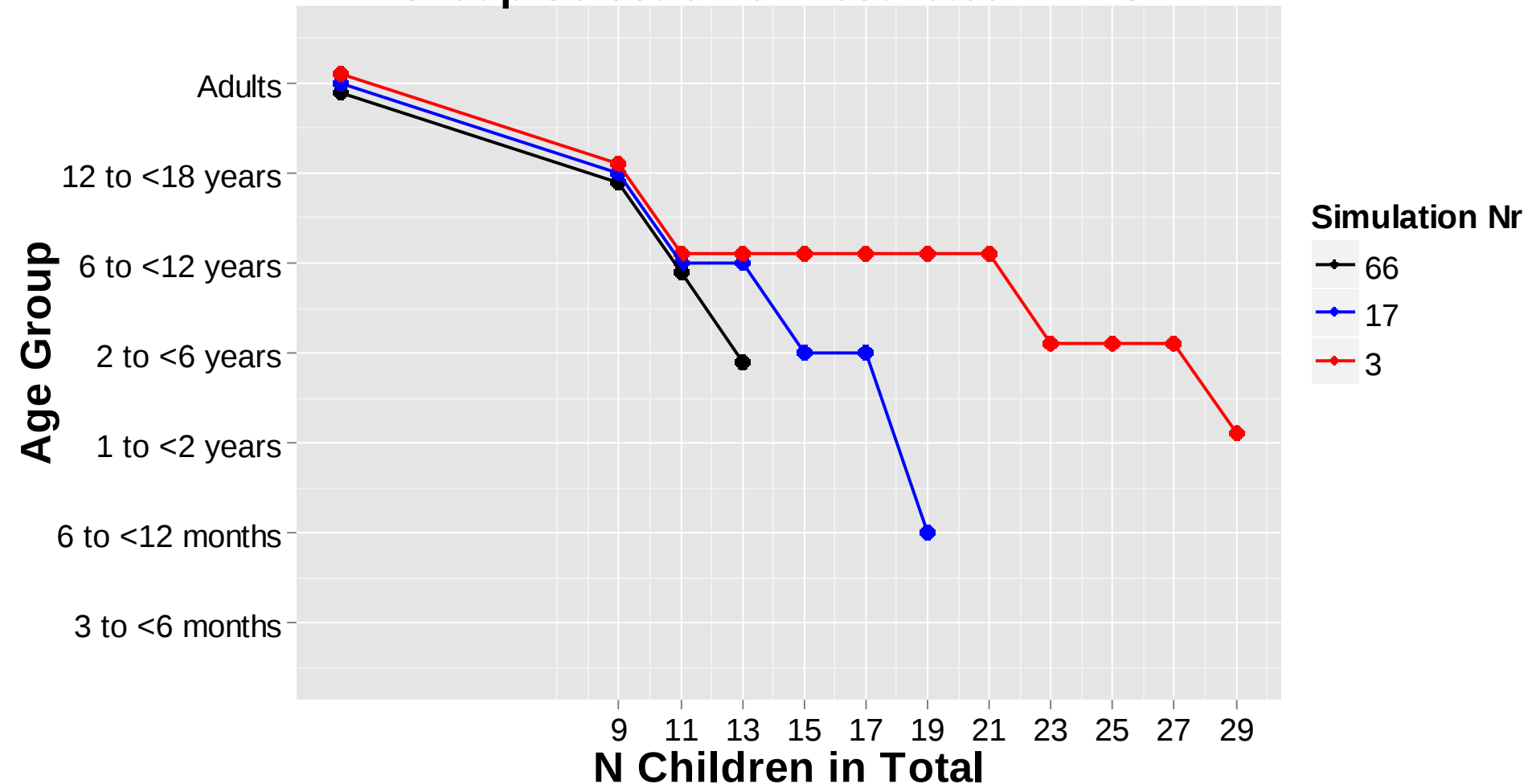
9 children in the oldest age group.

Lowest allowed Age Group:

One age group below the age groups which has passed the stopping criteria.

Restriction of Age Group Inclusion

Group Selection of Restricted MBAOD



Restriction of Age Group Inclusion

OD Stopping Criteria

Design of future study

Model guess M_0
Param. Guess P_0
Param. Uncertainty $P_{se,0}$
Prior $_0$ =FIM $_0$

↓ **Optimal Design**
Design

Scaling Model Guess
Param. Guess
Predicted SE, FIM

+

Median PMA:

$a_{1,1}$
⋮
 $a_{6,1} \dots a_{6,7}$

Median WT:

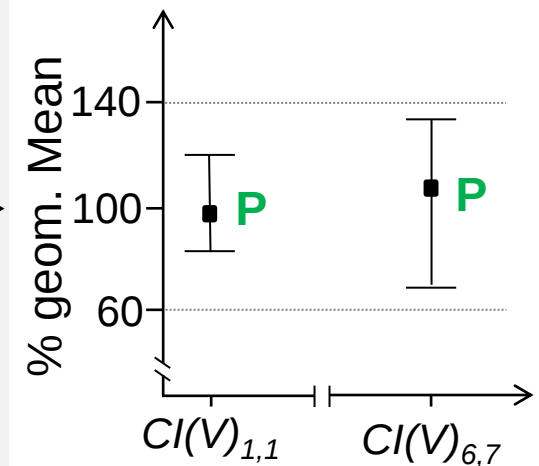
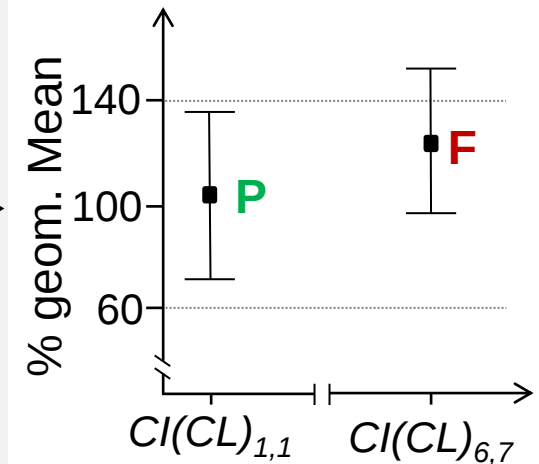
$wt_{1,1}$
⋮
 $wt_{6,1} \dots wt_{6,7}$

$CL_{1,1}$
⋮
 $CL_{6,1} \dots CL_{6,7}$

$V_{1,1}$
⋮
 $V_{6,1} \dots V_{6,7}$

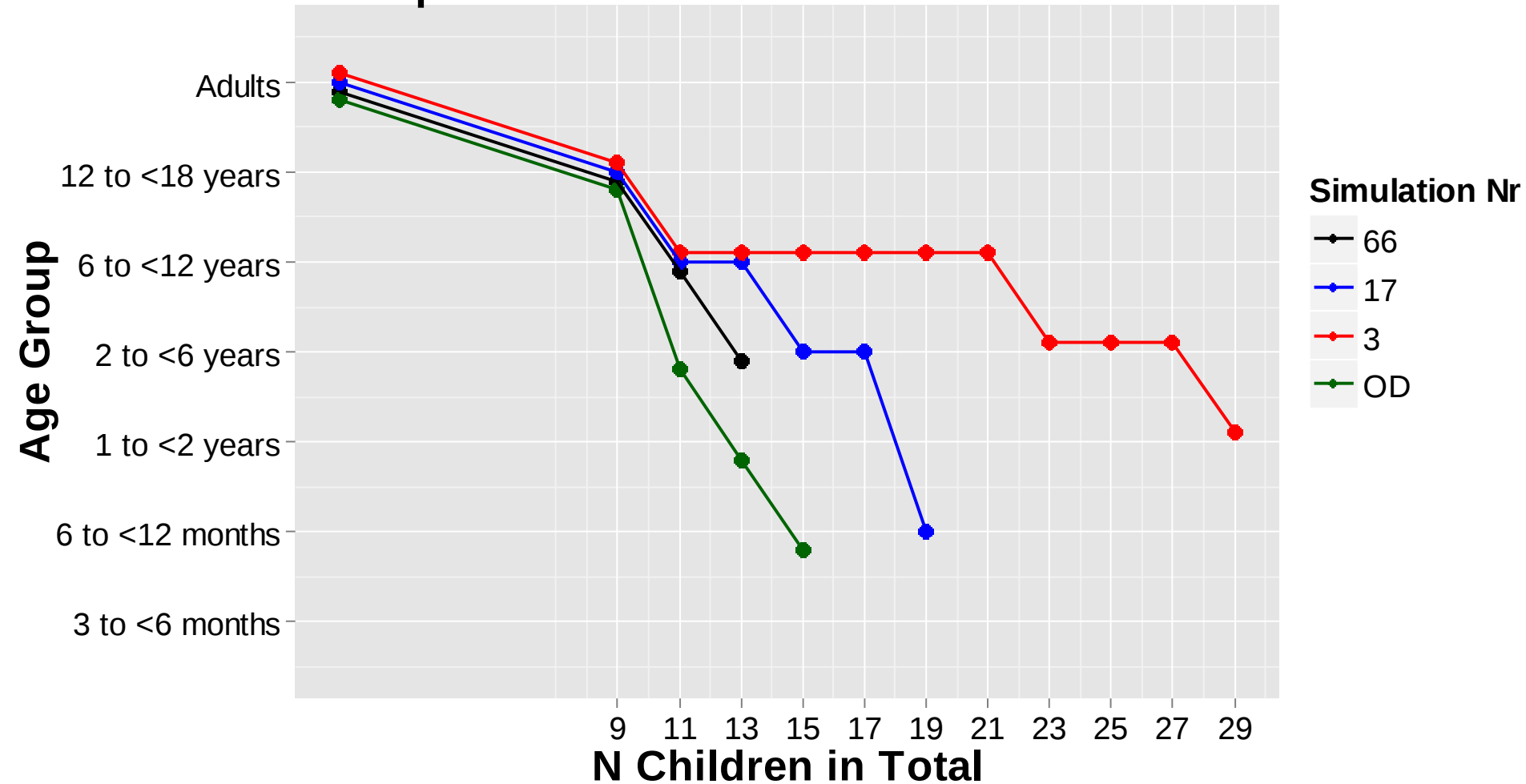
$SE(CL_{1,1})$
⋮
 $SE(CL_{6,7})$

$SE(V_{1,1})$
⋮
 $SE(V_{6,7})$



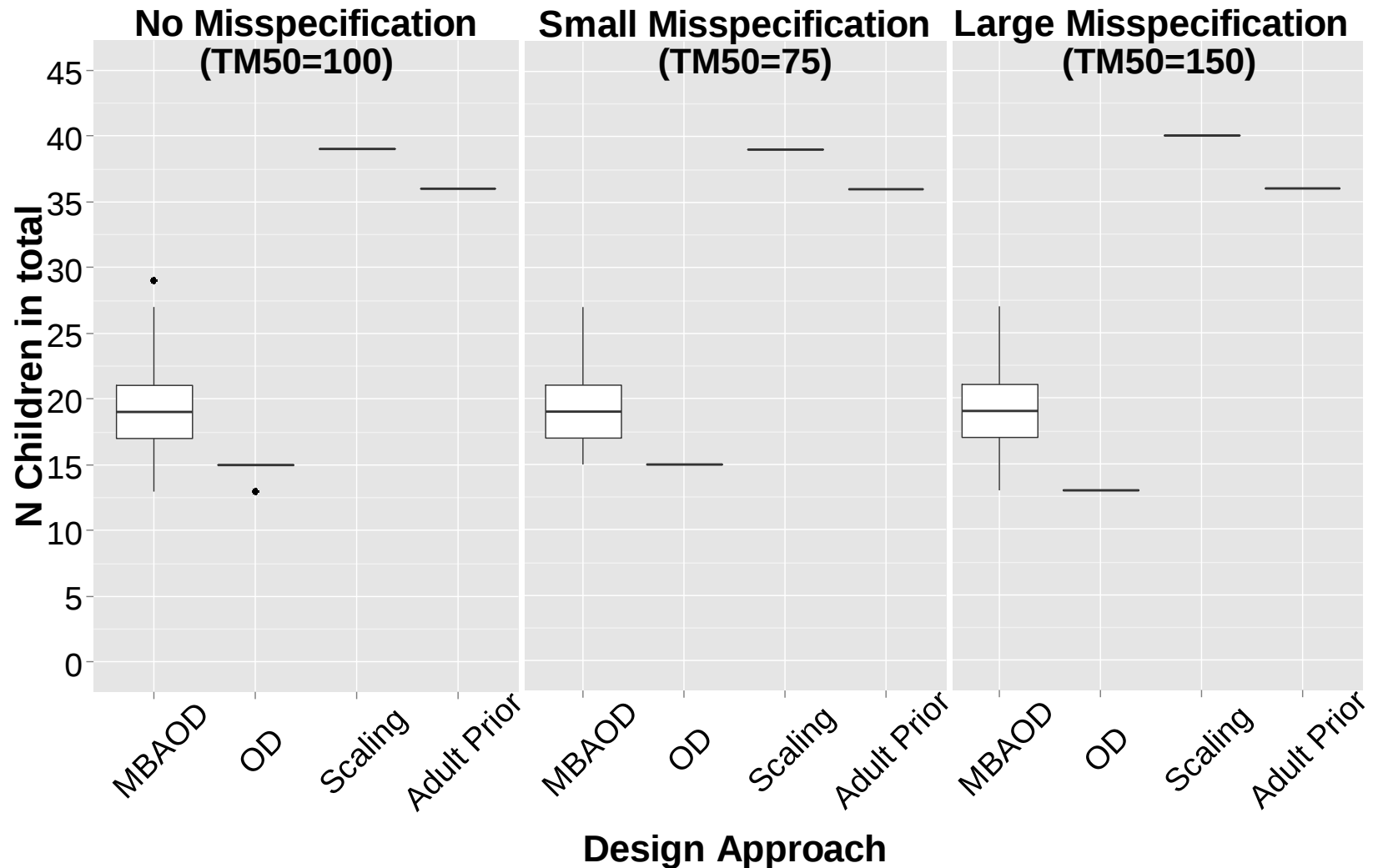
Restriction of Age Group Inclusion

Group Selection of Restricted MBAOD and OD



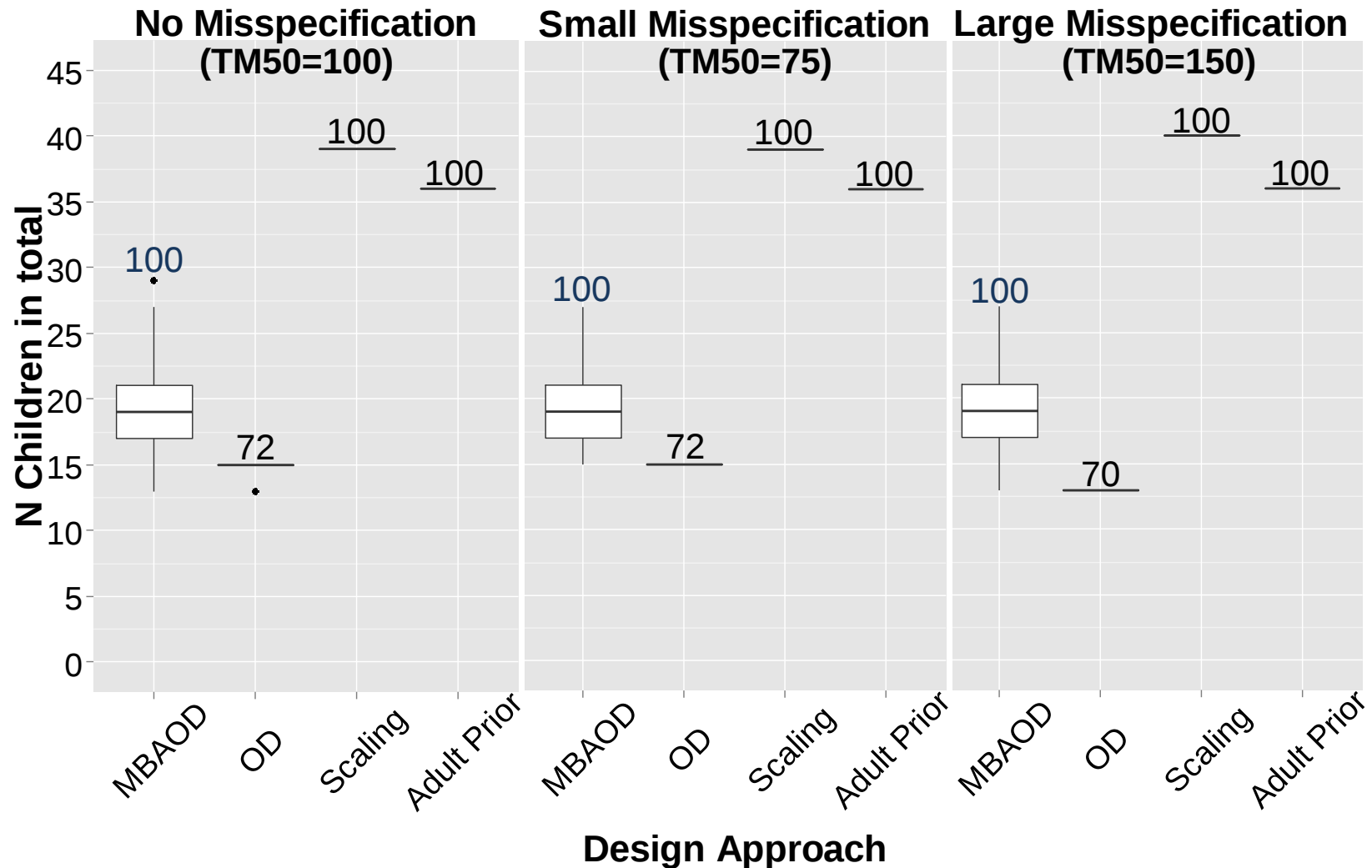
Results

Total Number of Children



Results

Total Number of Children and Power



Conclusions

The FDA precision criteria was successfully implemented as a stopping criteria in the MBAOD R-Package

The MBAOD required less children to fulfill the precision criteria than the traditional sample size estimation methodologies

Power for non-adaptive OD was lower than the required >80%

With the stopping criteria itself not being model dependent, any PK or scaling model could be used

Acknowledgements

Supervisor:
Andrew C. Hooker

Pharmacometrics Research Group



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This work was supported by the
DDMoRe project.
(www.ddmore.eu)



Travel and participation funding:



Github repository: https://github.com/IgnisDivne/mbaod_sim

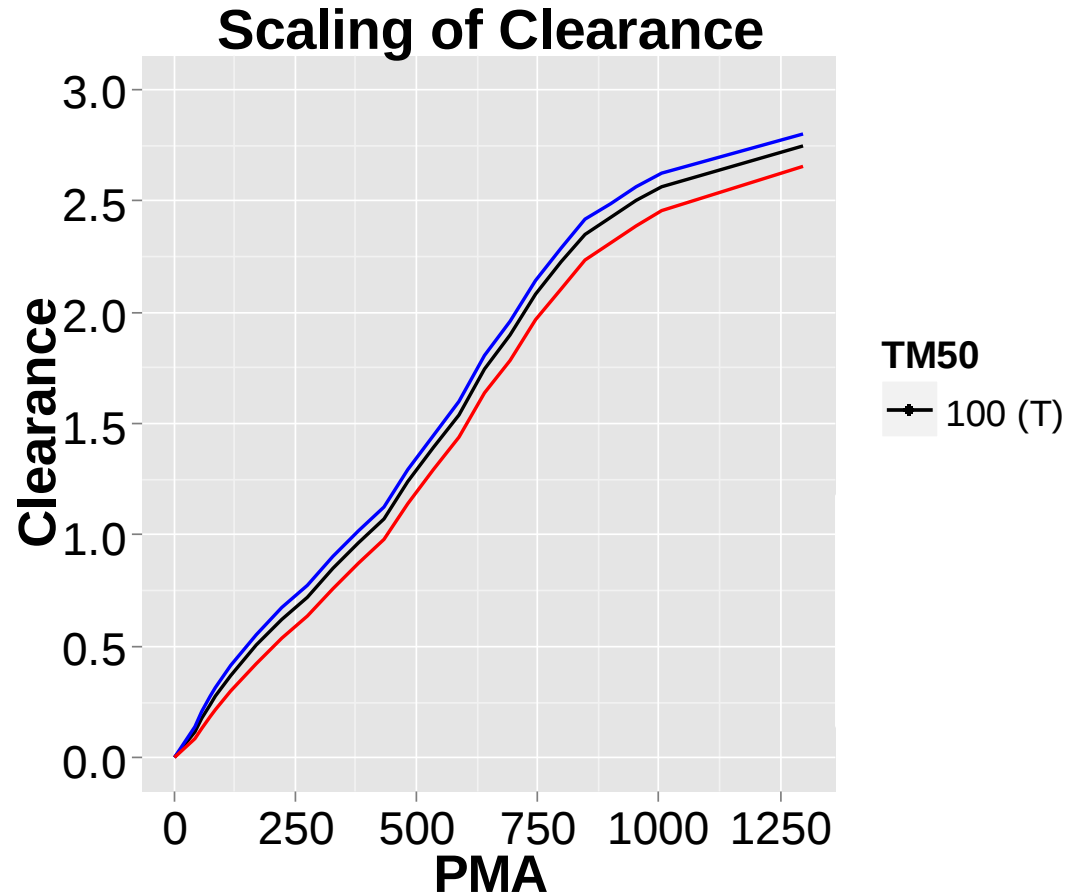


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Extra Slides

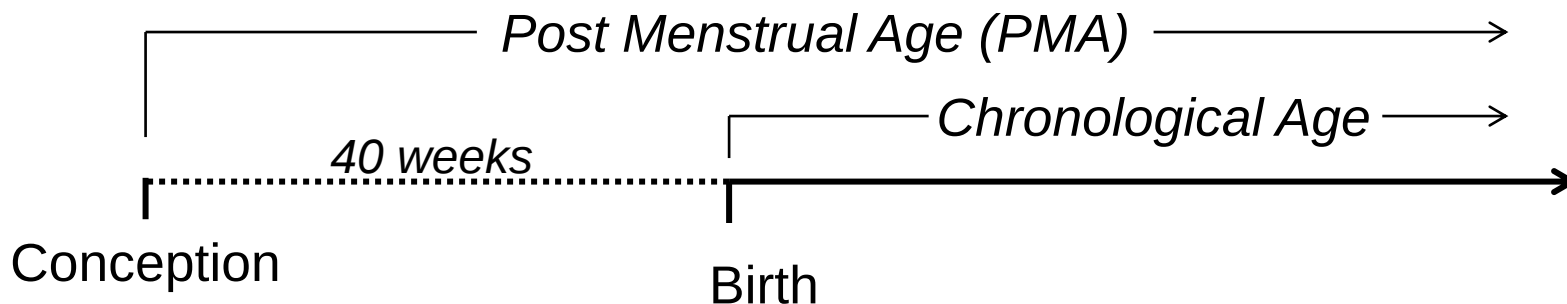
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$\sigma^2 (\text{Prop})$	0.015
$\sigma^2 (\text{Add})$	0.0001 FIX



The Simulated Study Population

Age Group	Description	Age Range	PMA Range [Weeks]
1	Young Infants	3 - <6 mo	53.05 - <66.1
2	Infants	6 - <12 mo	66.1 - <92.2
3	Toddlers	1 - < 2 y	92.2 - <144.4
4	Early Childhood	2 - <6 y	144.4 - <353.3
5	Childhood	6 - <12 y	353.3 - <666.5
6	Adolescence	12 - 18 y	666.5 - <1031.9
7	Adults	20 - 29 y	1084 - 1553.8



Fisher Information Matrix:

$$FIM = -E_y \left[\frac{\partial^2}{\partial \Theta^2} \ln(L(\Theta|y)) \right]$$

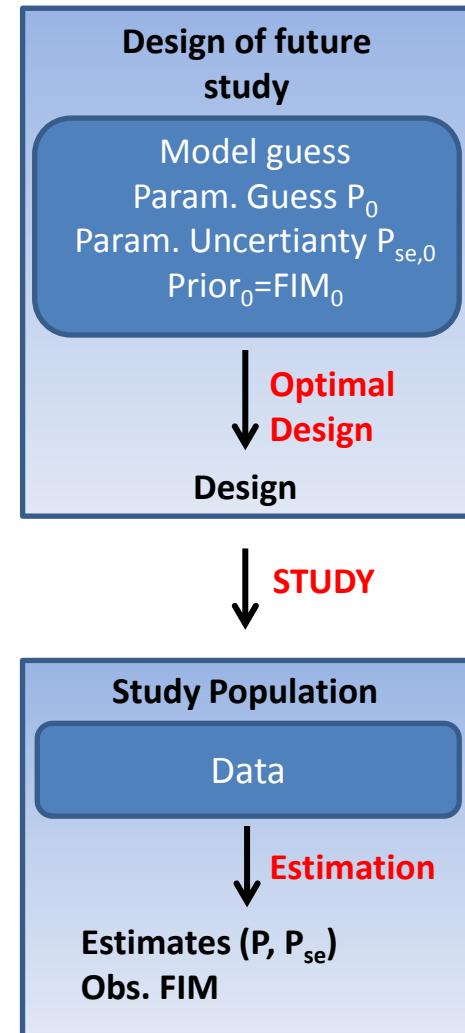
Cramer-Rao inequality:

$$\frac{1}{FIM}(q, \Theta) \leq COV(q, y, \Theta)$$

y : Model response
 Θ : Model parameters
 q : Design variables

Optimal Design

Adaptive vs Non-Adaptive



Expandability and future work

Implement a library of scaling models

Implement functionality for model averaging and model discrimination.

Optimal Design

Adaptive vs Non-Adaptive

