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# **A comparison of performance between parametric and nonparametric estimation for nonlinear mixed-effects models**

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# Questions

- For real data examples with models developed based on parametric methods, can nonparametric estimation offer
  - better description of data?
  - better prediction of new data?

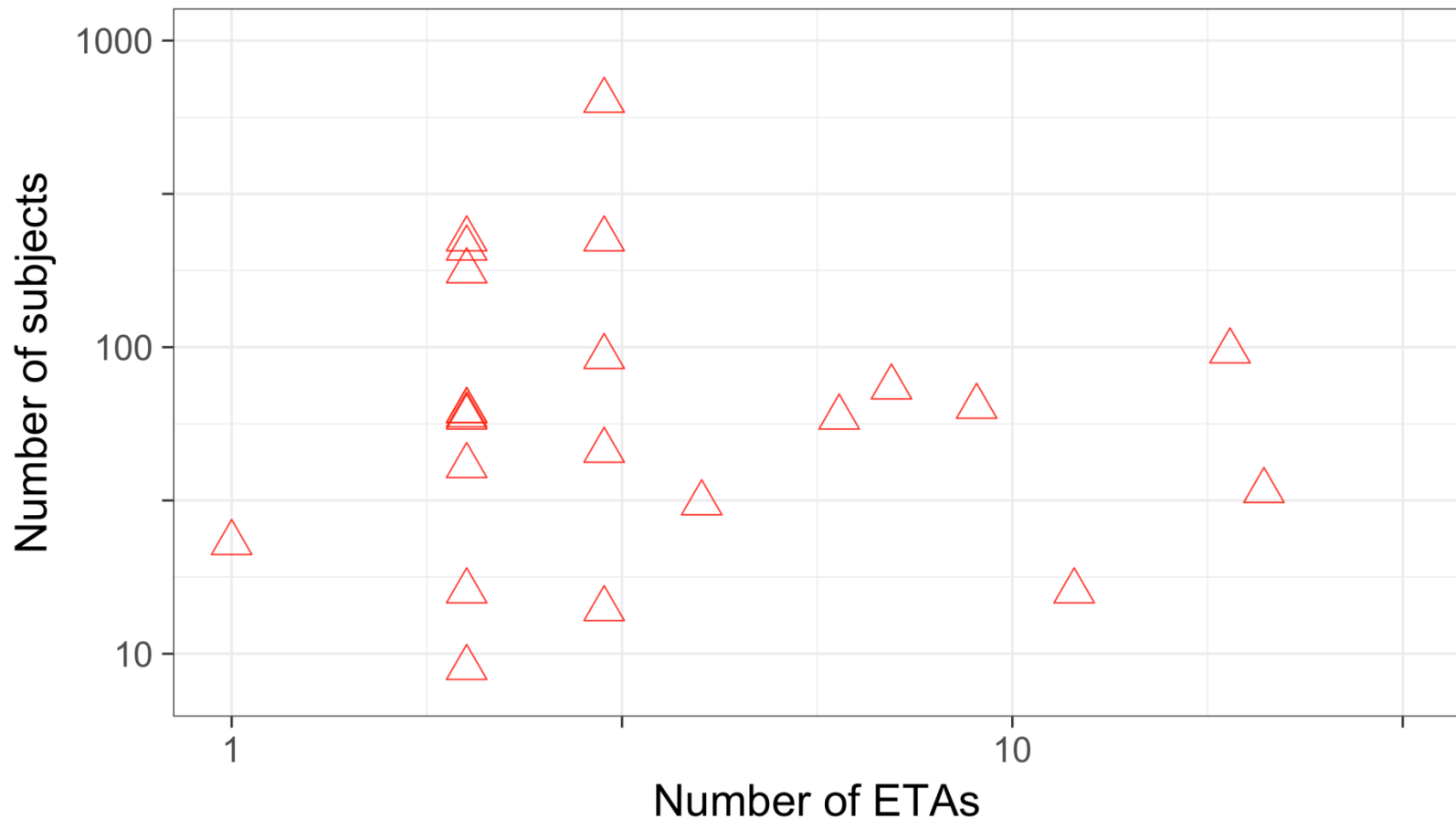
# Estimation methods

- Parametric (P): FOCE(I)/Laplace in NONMEM
  - But models also evaluated with Importance sampling
- Nonparametric (NP): \$NONP in NONMEM
  - But models also estimated with the extended grid method



# Models and data

- PK (n=16) and PD (n=7) model based on real data

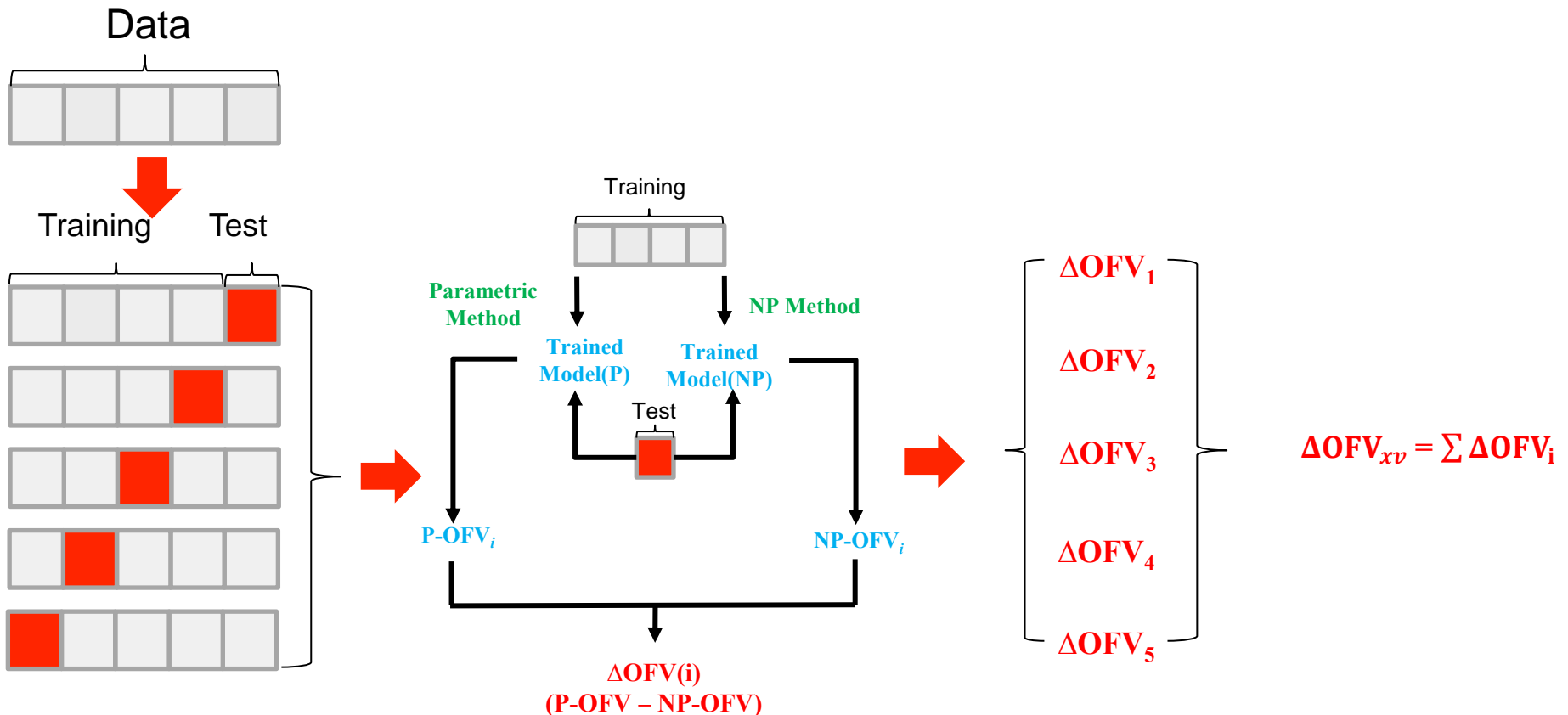


# Comparisons – description of data

- $\Delta\text{OFV}(\text{P-NP})$
- $\Delta\text{AIC} = \Delta\text{OFV}(\text{P-NP}) + 2 \cdot \Delta\#\text{parameters}(\text{P-NP})$ 
  - $\#\text{parameters}(\text{P}) = 2 \cdot \#\text{etas} + \#\text{covariance terms}$
  - $\#\text{parameters}(\text{NP}) = (\#\text{support points}) \cdot (\#\text{etas} + 1) - 1$
- $\Delta\text{OFV}(\text{P-NP})$  vs reference distribution for  $\Delta\text{OFV}(\text{P-NP})$  when simulating from parametric models and refit with P & NP

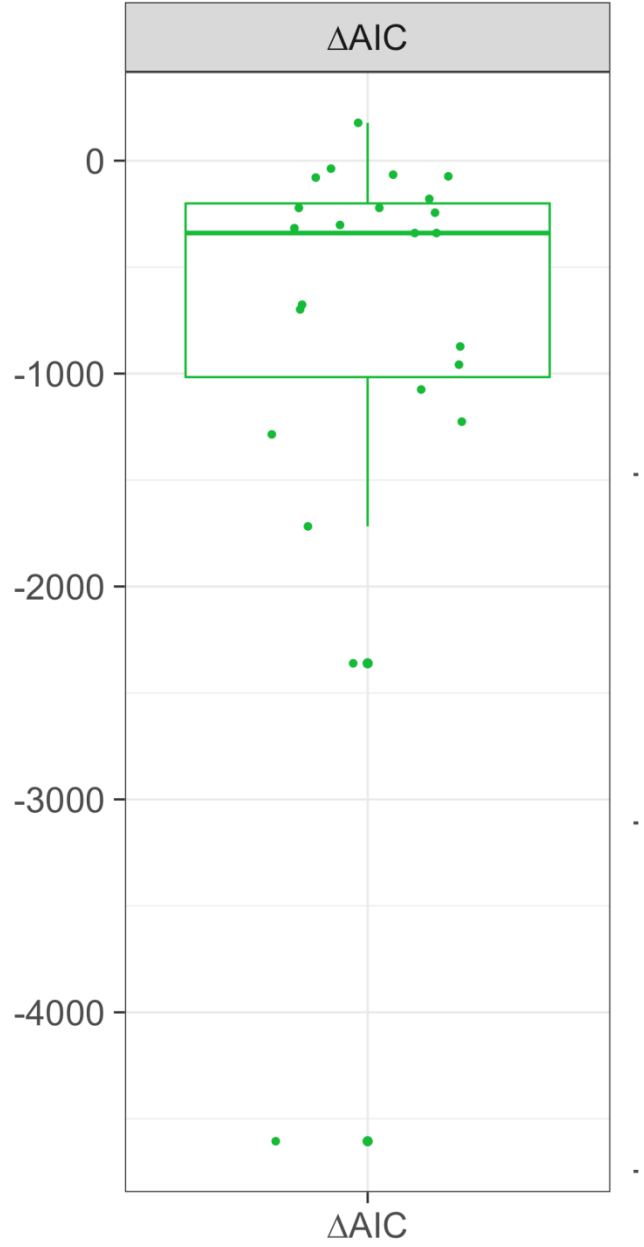
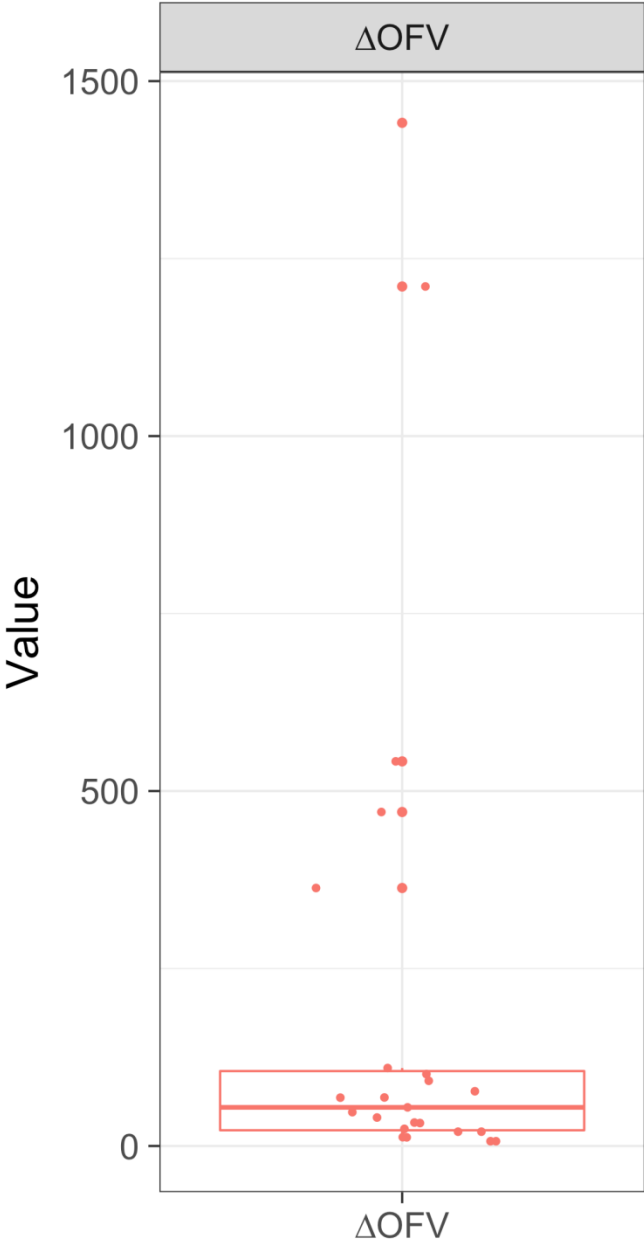
# Comparisons – prediction of new data

- $\Delta XVOFV$  (Cross-validated OFV)
  - 2-fold & 5-fold cross-validation



# Why compare based on OFV?

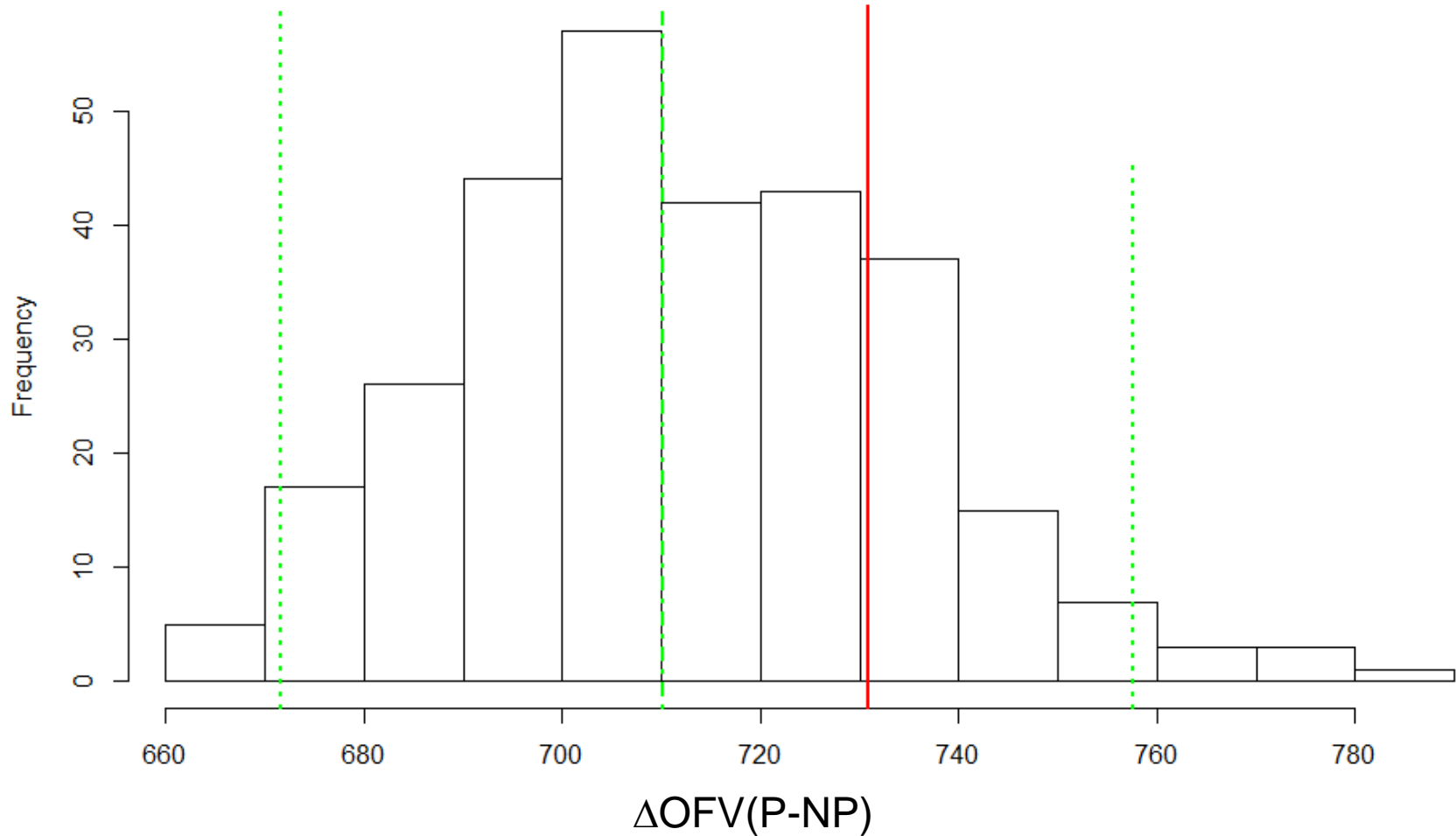
- Why not compare prediction error of concentrations/effects?
  - OFV incorporates this, but also accounts for:
    - Heteroscedasticity in residual error magnitude
    - Correlation among observations within individuals
  - Not unambiguous what "a" prediction is with NP distribution, OFV is calculated taking the full NP distribution into account



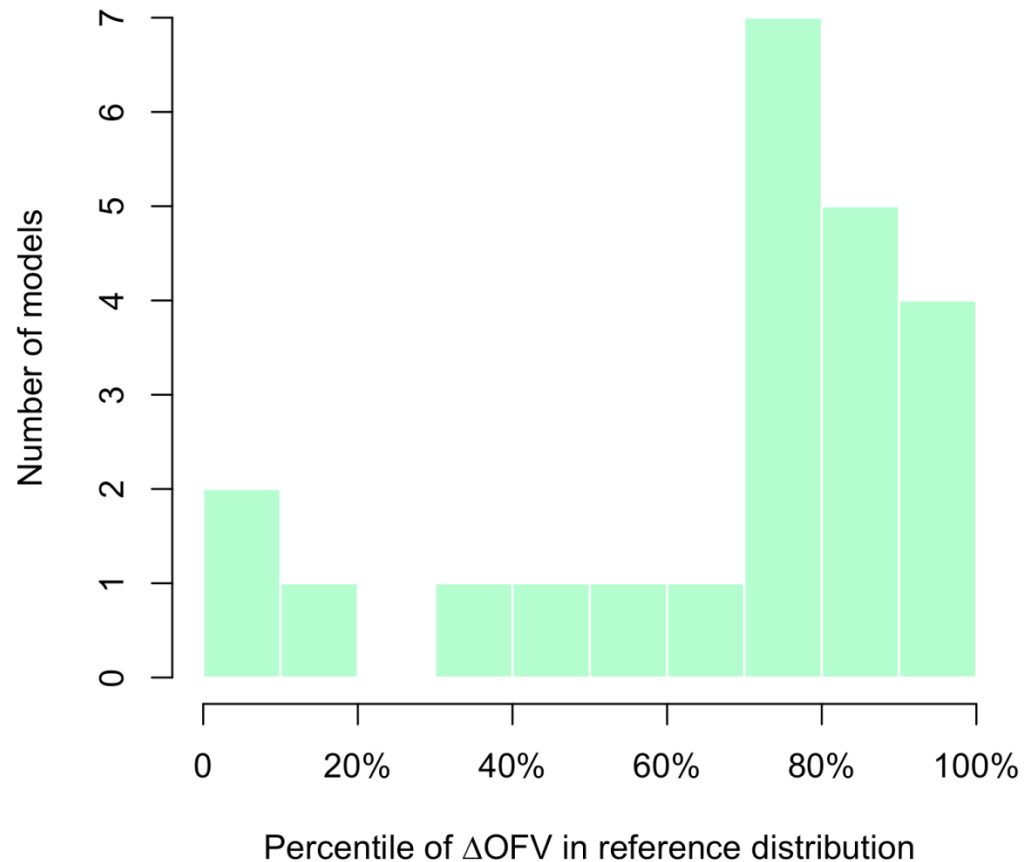




# $\Delta\text{OFV(P-NP)}$ reference distribution



# Observed $\Delta\text{OFV}(\text{P-NP})$ vs reference distribution for $\Delta\text{OFV}(\text{P-NP})$



# Use of NP information to improve parametric model

- Covariance terms

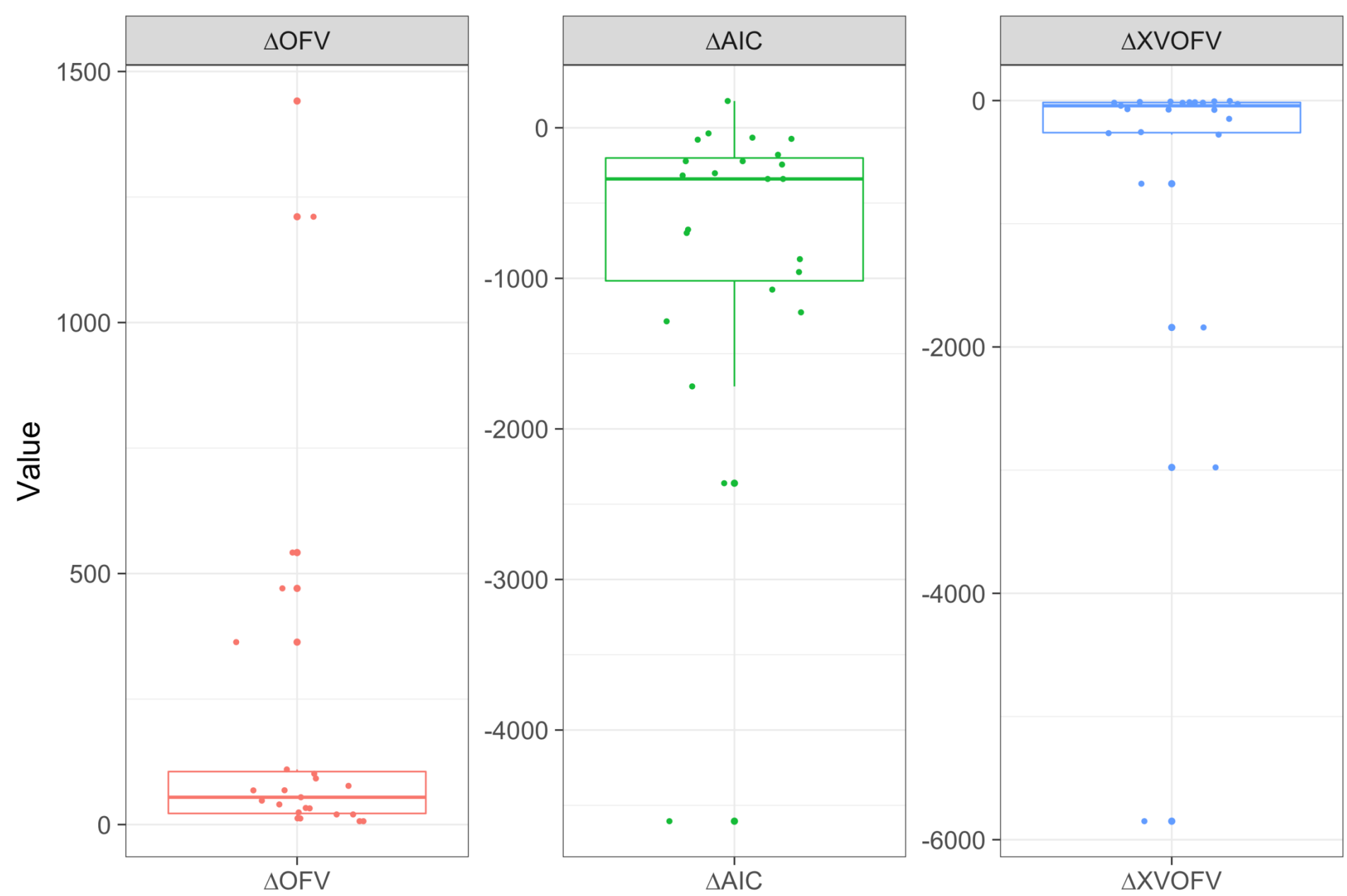
- When NP indicates correlations unaccounted for in P

- Mixture models

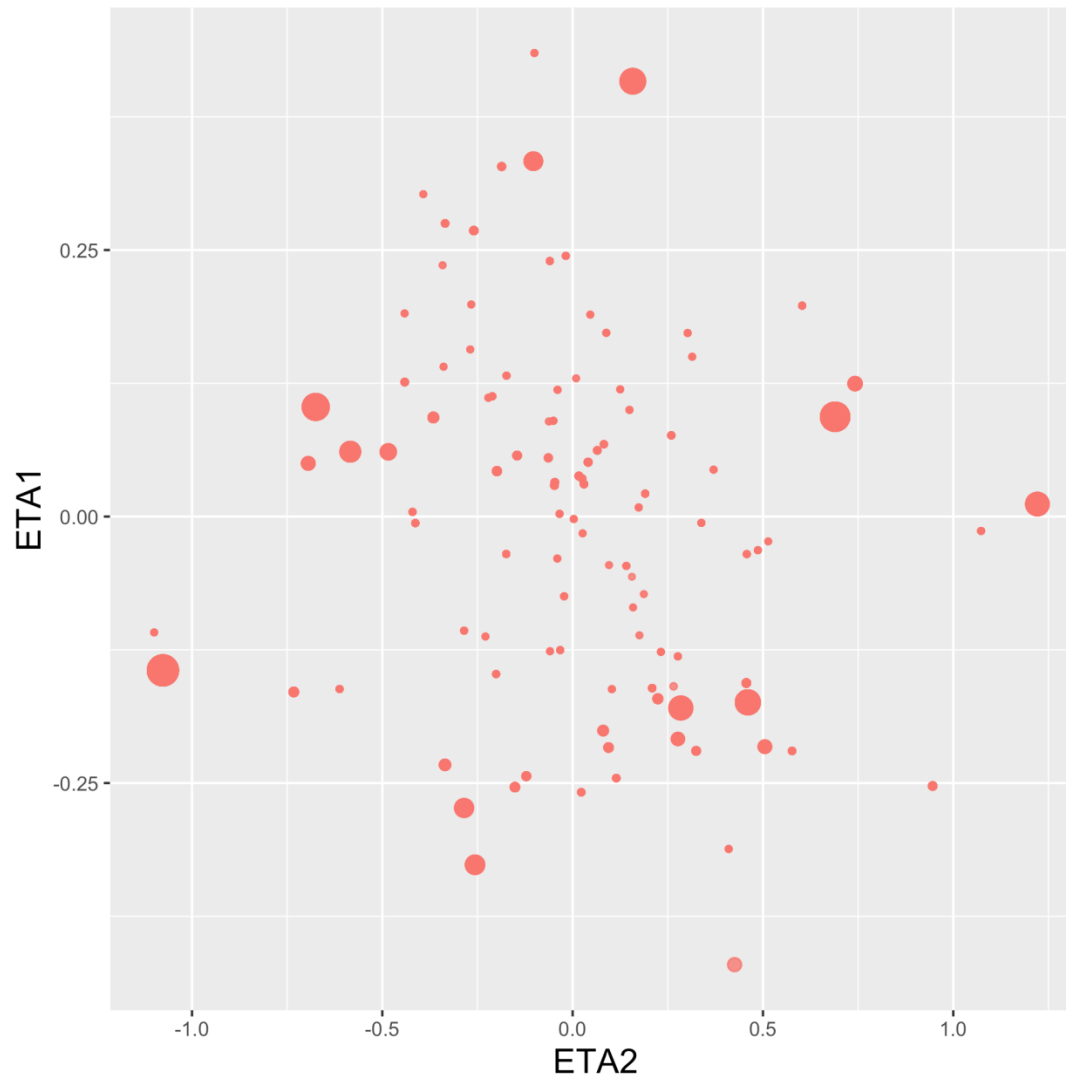
- When NP indicates multimodality

- Semi-parametric models with estimated shape parameter(s)

- When NP indicate skewed or heavy-tailed distributions

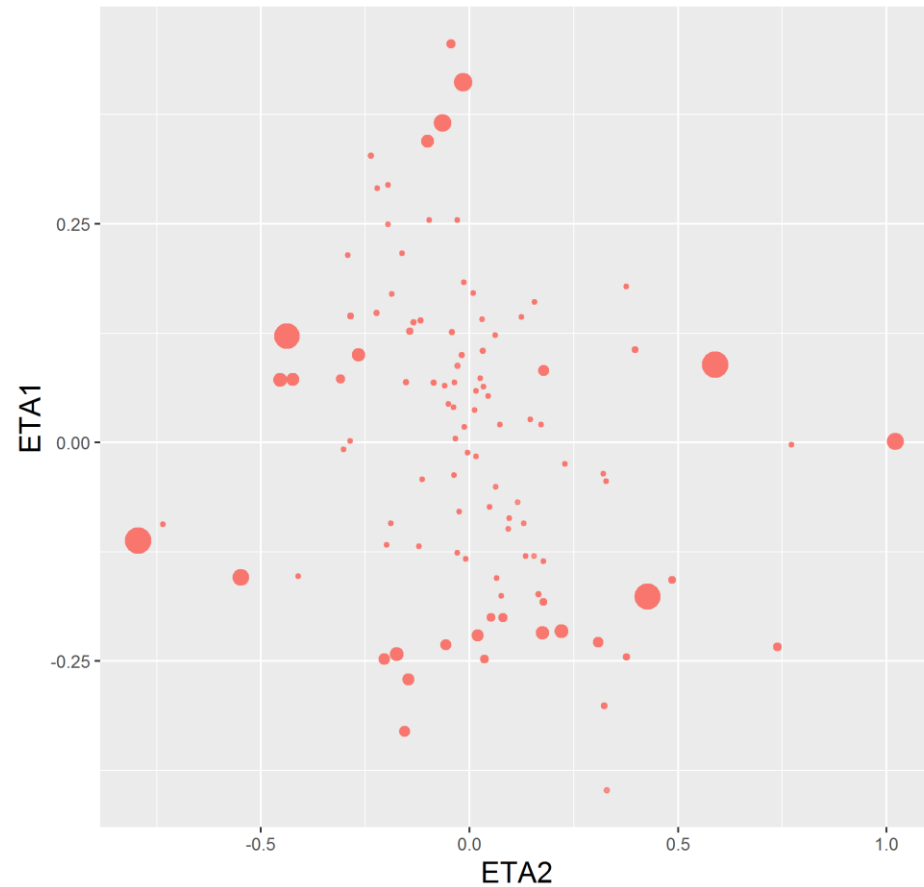


# Estimated NP distribution - gentamicin PK model (Nsubj=210)

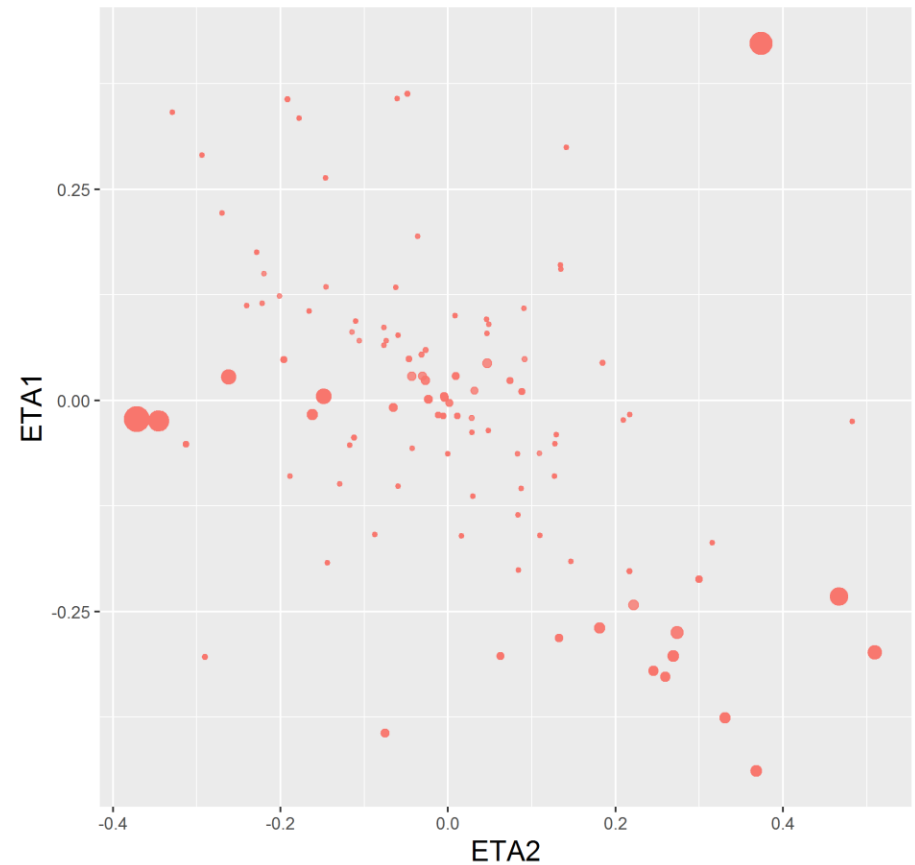


# Estimated NP distribution - gentamicin PK models on split data set

Gentamicin-2 (Nsubj=105)

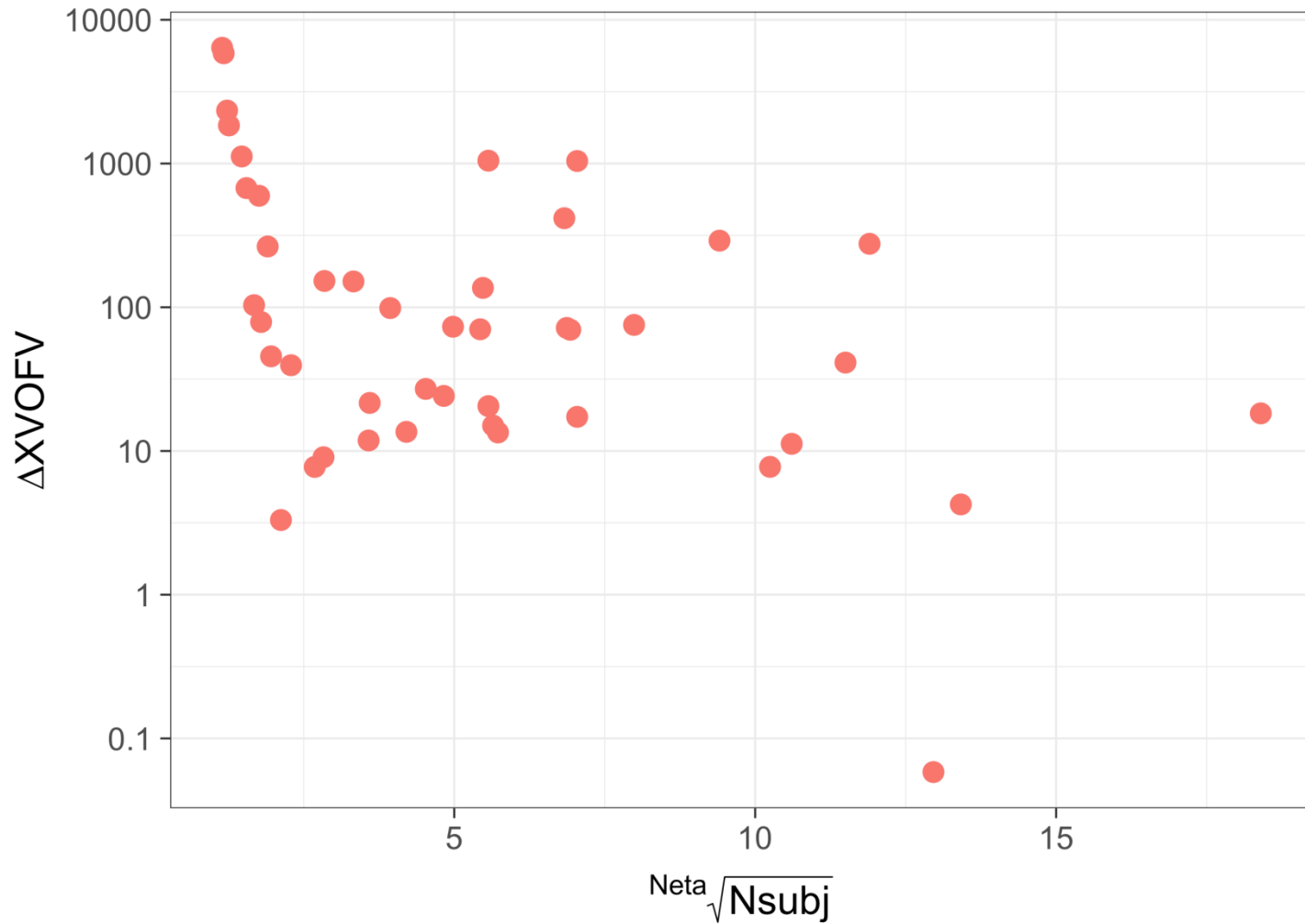


Gentamicin-1 (Nsubj=105)





# $\Delta x_{vOFV}$ versus density metric



- For the studied models, data and methods:
  - NP fit is better than fit of P
  - Accounting for parsimony, P fit typically better than NP fit
  - P better than NP for predicting new data



# What if we had used NPAG?

- $\Delta$ OFV

- NPAG likely to be better than \$NONP
- NPAG 1-step estimation
- \$NONP 2-step estimation (location, probability)

- $\Delta$ AIC

- NPAG likely to be better than \$NONP
- $\#parameters(NPAG) < \#parameters(\$NONP)$

- $\Delta$ xvOFV

- Not clear (fewer Nsupp of NPAG unlikely an advantage)



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## Models

10 20 50

Submission ID	Name	Format	Submitter	Submitted	Modified	Certification
DDMODEL00000119	Bender_2012_thrombocytopenia_TDM1	PharmML 0.8.x	Paolo Magni	2015/12/12	2016/10/13	☆
DDMODEL00000224	Kloft_2006_myelosuppression_docetaxel	Original code	Ida Netterberg	2016/10/12	2016/10/13	☆
DDMODEL00000110	Magni_2000_diabetes_C-peptide	PharmML 0.8.x	Paolo Magni	2015/12/11	2016/10/13	☆
DDMODEL00000225	PKPD model for ciprofloxacin	PharmML	David Khan	2016/10/13	2016/10/13	☆
DDMODEL00000222	Hansson_2013_Fatigue_GIST	Original code	Pierrillas Philippe	2016/10/11	2016/10/12	☆
DDMODEL00000223	Novakovic_2016_multiplesclerosis_cladribine_irt	Original code	Ana Novakovic	2016/10/12	2016/10/12	☆
DDMODEL00000221	Schindler_2016_SLD_SUV_OS_GIST	Original code	Emilie Schindler	2016/10/11	2016/10/12	☆
DDMODEL00000220	Jonsson_2011_ethambutol_pharmacokinetics	Original code	Siv Jonsson	2016/10/11	2016/10/12	☆
DDMODEL00000111	Magni_2004_diabetes_IVGTT	PharmML 0.8.x	Paolo Magni	2015/12/11	2016/10/11	☆
DDMODEL00000217	Tumour size dynamics model for ovarian cancer patients	Original code	Ivelina Gueorguieva	2016/10/07	2016/10/11	☆

Showing 31 to 40 of 109 models

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Thank you!