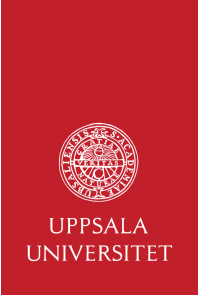


# Modeling a Composite Score in Parkinson's Disease using Item Response Theory

*PAGE - 2015*

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# Parkinson's Disease

- Parkinson's disease is a progressive neurodegenerative brain disorder characterized by
  - loss of neurons in substantia nigra
  - decrease in the dopamine levels
- Parkinson's disease is known to affect approximately 6.3 million people worldwide<sup>1</sup>
- Movement Disorder Society (MDS) - sponsored revision<sup>2</sup> of the Unified Parkinson's Disease Rating Scale (UPDRS)

1. European Parkinson's Disease Association (<http://www.epda.eu.com/en/>)

2. Goetz et al. Move Disord. 2007; 22(1) 41-7

# MDS-UPDRS

## Composite Scale



### Part I

- Non-motor aspects of experiences of daily living
- *e.g. cognitive impairment*

### Part II

- Motor aspects of experiences of daily living
- *e.g. tremors*



### Part III

- Motor examination
- *e.g. finger tapping – right & left hands*

### Part IV

- Motor complications
- *e.g. functional impact of dyskinesias*

- Overall, there are 68 items – 66 ordered categorical and 2 binary
- **Higher total score** (range: 0 – 267) indicates **more severe disease**



- Parkinson Progression Markers Initiative (PPMI) Database:
  - Longitudinal MDS-UPDRS data:  
at baseline(0), up to 12 visits (60 months) → 255023 observations

Healthy  
Controls

( $n = 196$ )

*Age  $\geq 30$  years*

*No first degree blood  
relative with  
Parkinson's disease*

De Novo  
Parkinson's  
Disease  
Subjects

( $n = 423$ )

*Diagnosed  $\leq 2$  years*

***Not** taking any  
medications for  
Parkinson's disease*

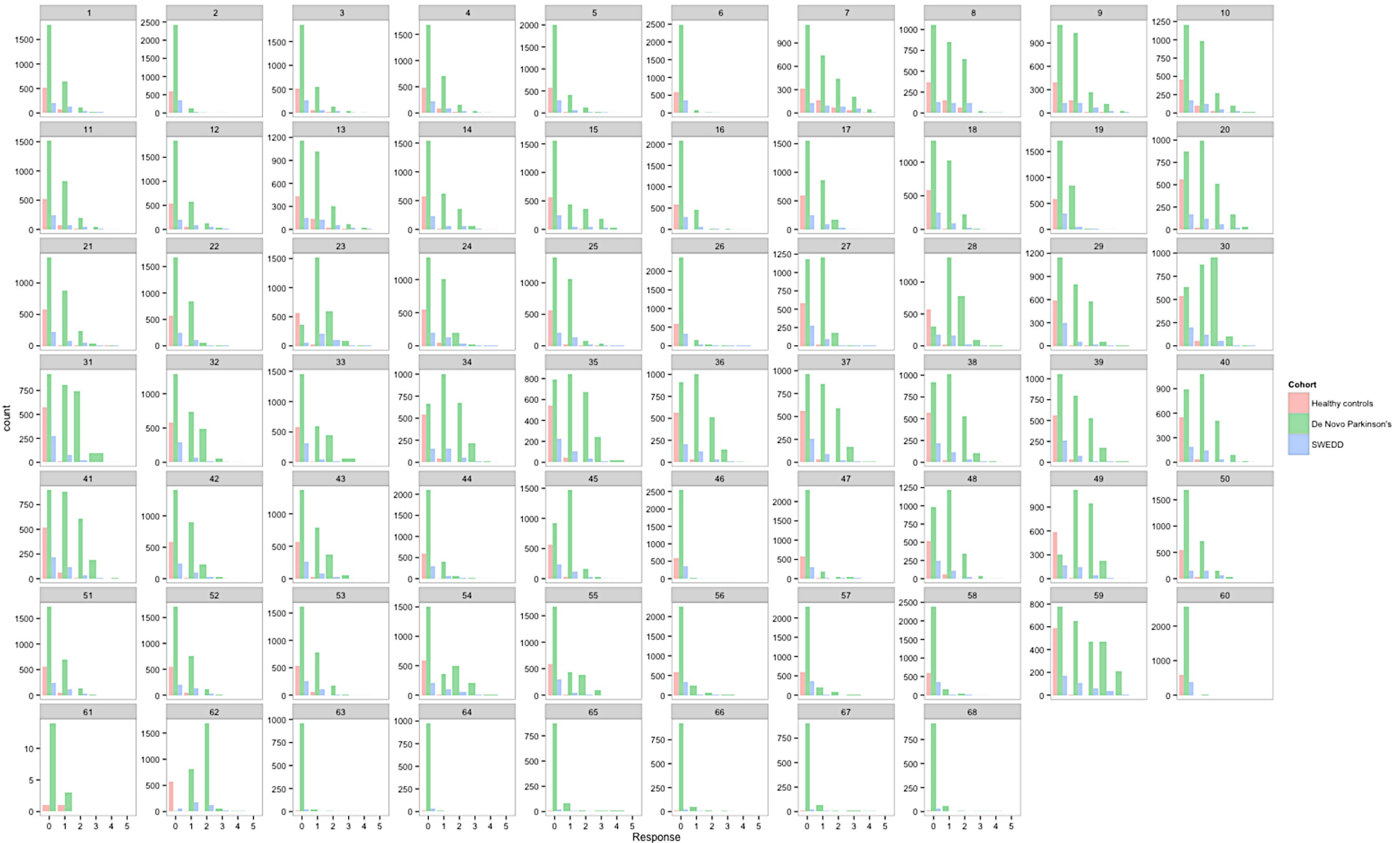
Subjects With  
Scans Without  
Evidence of  
Dopaminergic  
Deficit (SWEDD)

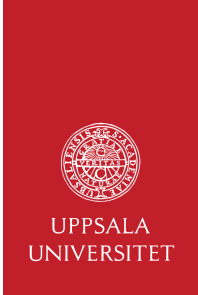
( $n = 64$ )

*Consented as  
Parkinson's patients*



# PPMI – Item Responses

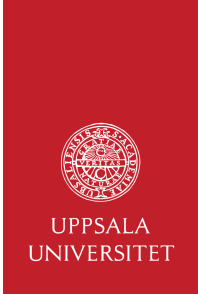




# Item 23

Over the past week, have you usually had a shaking or tremor?

- |             |   |
|-------------|---|
| 0: Normal   | Not at all. I have <b>no shaking</b> or tremor                                  |
| 1: Slight   | Shaking or tremor occurs but <b>does not cause problems</b> with any activities |
| 2: Mild     | Shaking or tremor cause problems with only a <b>few</b> activities              |
| 3: Moderate | Shaking or tremor cause problems with <b>many</b> of my daily activities        |
| 4: Severe   | Shaking or tremor cause problems with <b>most</b> of my activities              |



Over the past week, have you usually had a shaking or tremor?

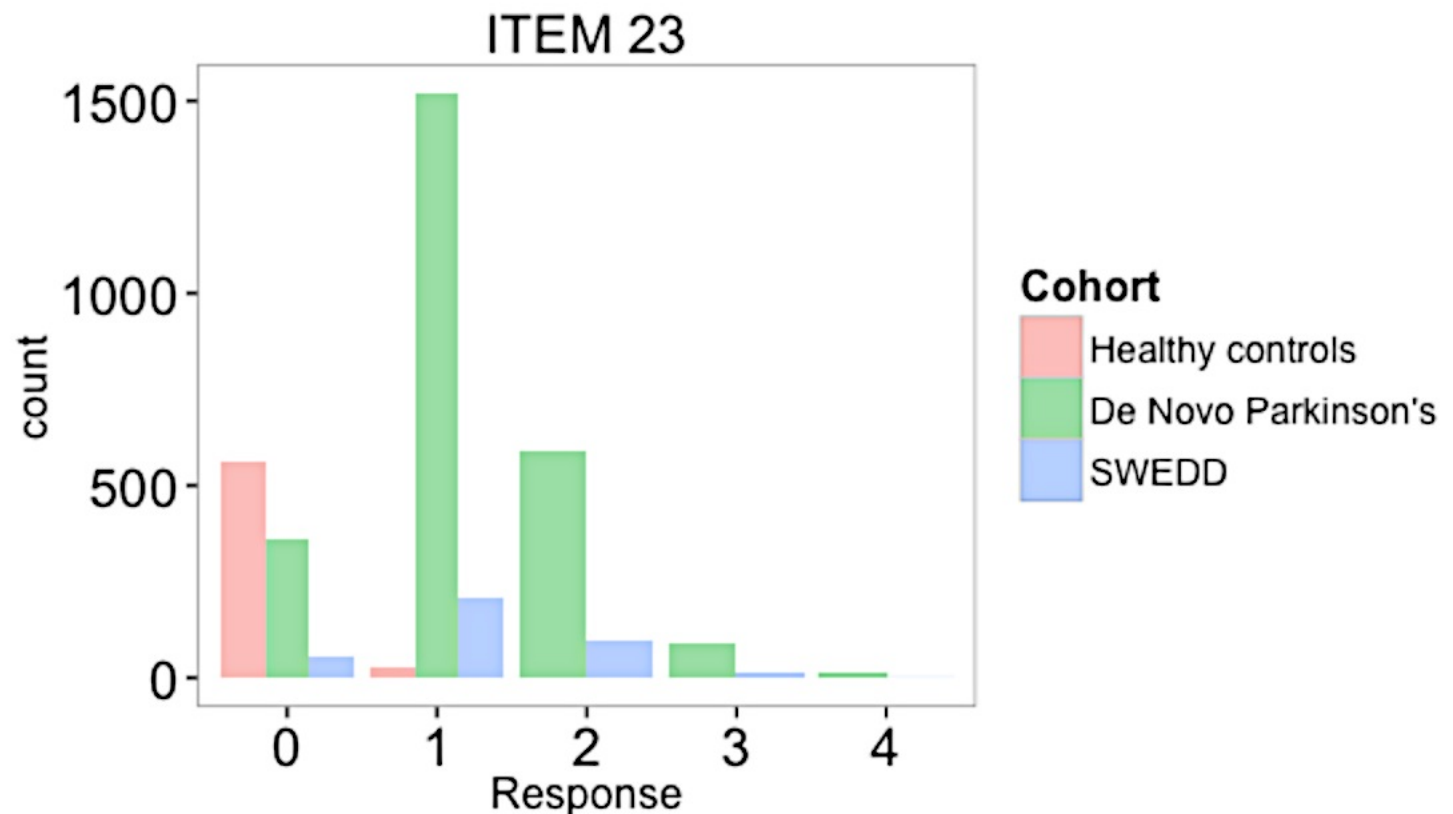
0: Normal

1: Slight

2: Mild

3: Moderate

4: Severe



# Item Response Theory

It relates the probability of responses to items in an assessment to an underlying latent (hidden) variable





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It has been applied in

- Alzheimer's<sup>1</sup> (ADAS-cog)
- Multiple Sclerosis<sup>2</sup> (EDSS)
- Schizophrenia<sup>3</sup> (PANSS)



1. Ueckert S., et al, Pharmaceutical Research 2014; 31(8):2152-2165.

2. Kalezic A., et al, PAGE 22 (2013) Abstract 2903

3. Krekels E., et al, PAGE 23 (2014) Abstract 3145

# Aims of the project

Disease/Patient Population

Methodology

- To explore IRT model components and investigate MDS-UPDRS features
- To describe MDS-UPDRS longitudinal changes
- To provide a model for future design and analysis of trials in Parkinson's Disease
- To explore model building strategies and diagnostics for IRT

# Model building strategy

- Subjects of De Novo cohort was used as reference population
  - Healthy controls and SWEDD cohort modeled by shift in (distribution of) disability

**Estimation of  
Item Characteristic Curves  
(ICC)**

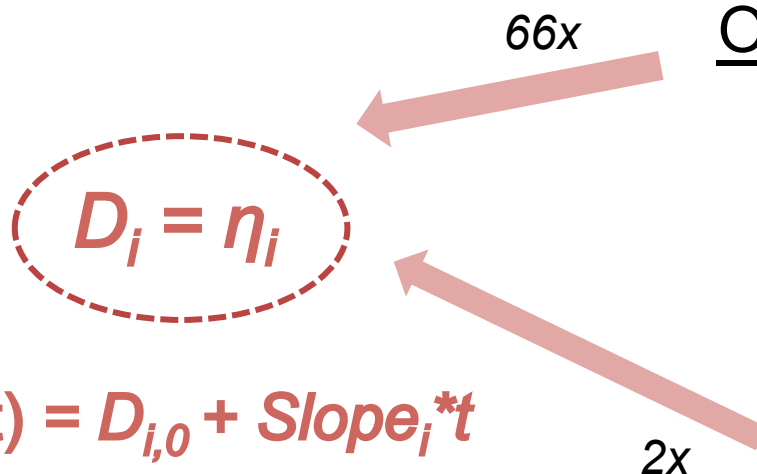
**Account for longitudinal  
changes**

- Estimation of ICC with shifts
  - Fix the ICC
  - Estimate the longitudinal changes
- Simultaneous estimation of ICC and longitudinal changes

# Structural IRT model

Model parameters divided into

- Item specific parameters –  $a_j, b_j \dots$  (discrimination and difficulty)
- Subject specific parameters –  $D_i$  (disability)



$$D_i(t) = D_{i,0} + \text{Slope}_i * t$$

De Novo cohort:  $D_{i,0} \sim N(0, 1)$

Other cohorts:

Shift in baseline

Different slopes

Ordered categorical (0 - 4/5)

$$P(Y_{ij} \geq k) = f_j(D_i) = \frac{e^{a_j(D_i - b_j)}}{1 + e^{a_j(D_i - b_j)}}$$

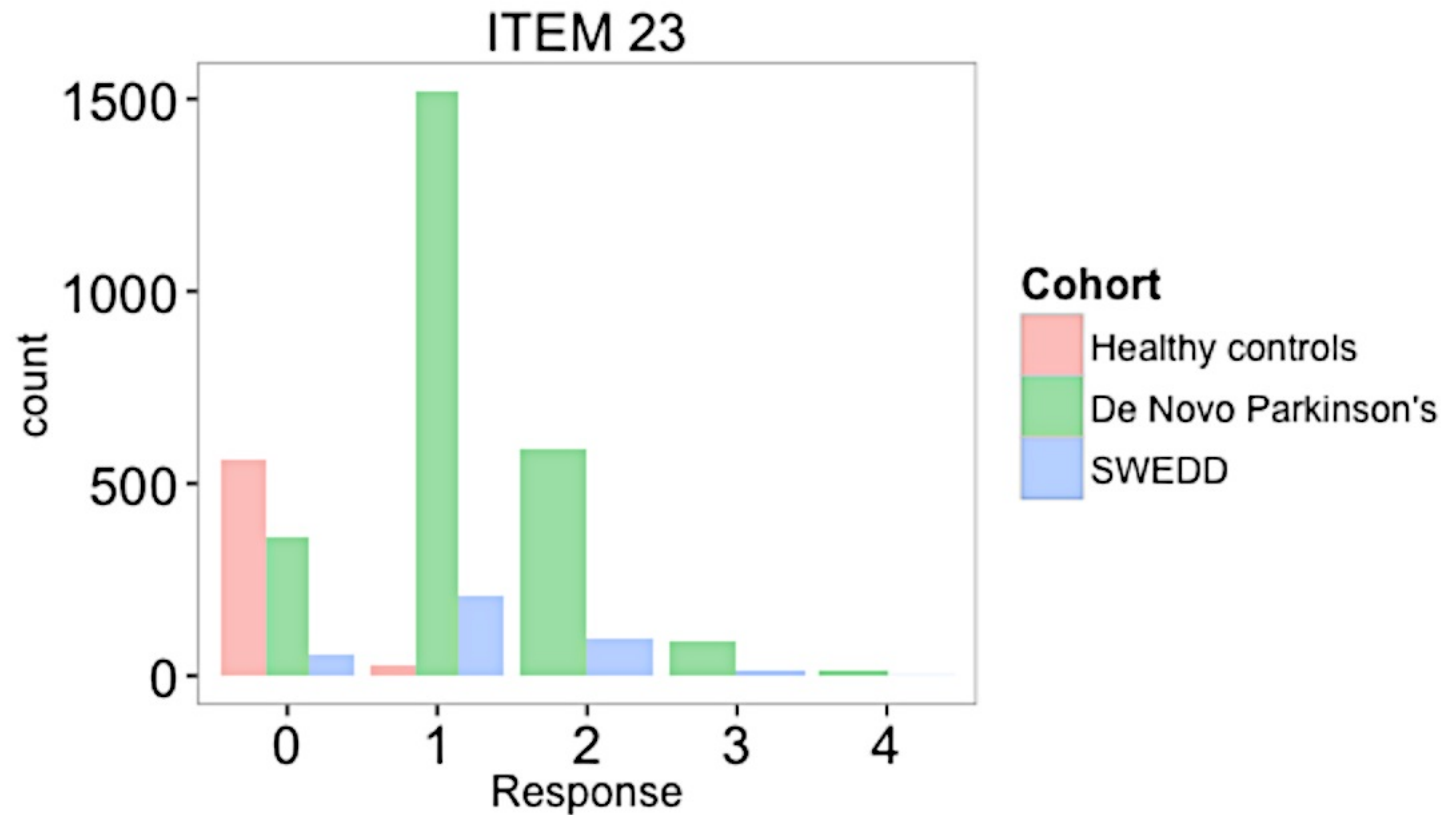
$$P(Y_{ij} = k) = P(Y_{ij} \geq k) - P(Y_{ij} \geq k+1)$$

Binary (0/1)

$$P(Y_{ij} = 1) = f_j(D_i) = \frac{e^{a_j(D_i - b_j)}}{1 + e^{a_j(D_i - b_j)}}$$

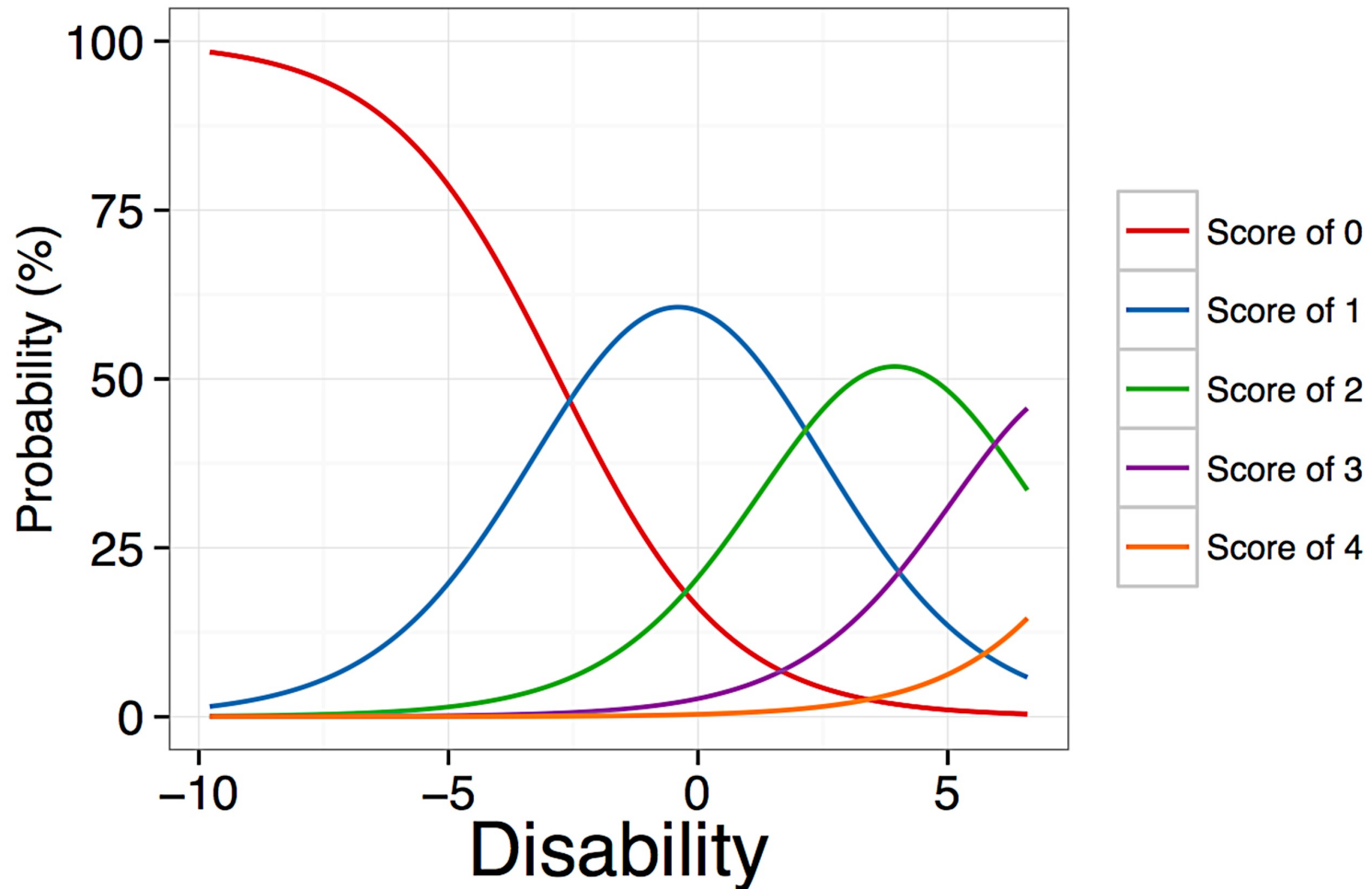
# Item Characteristic Curve

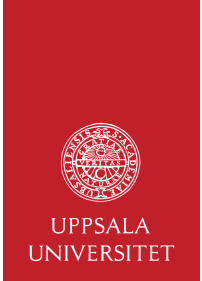
*Item 23 – Distribution of item responses*



# Item Characteristic Curve

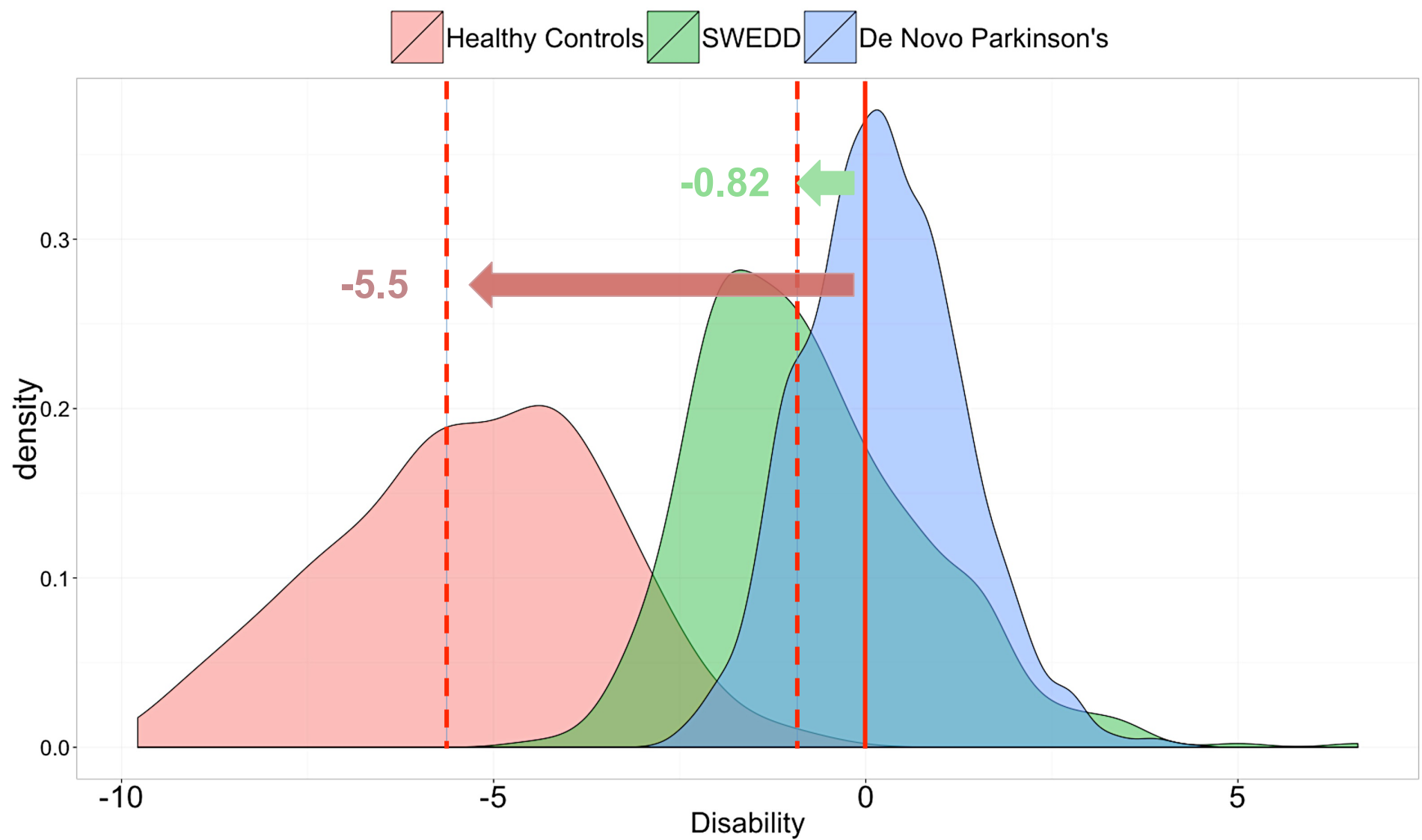
*Item 23 – Individual probabilities*





# Results

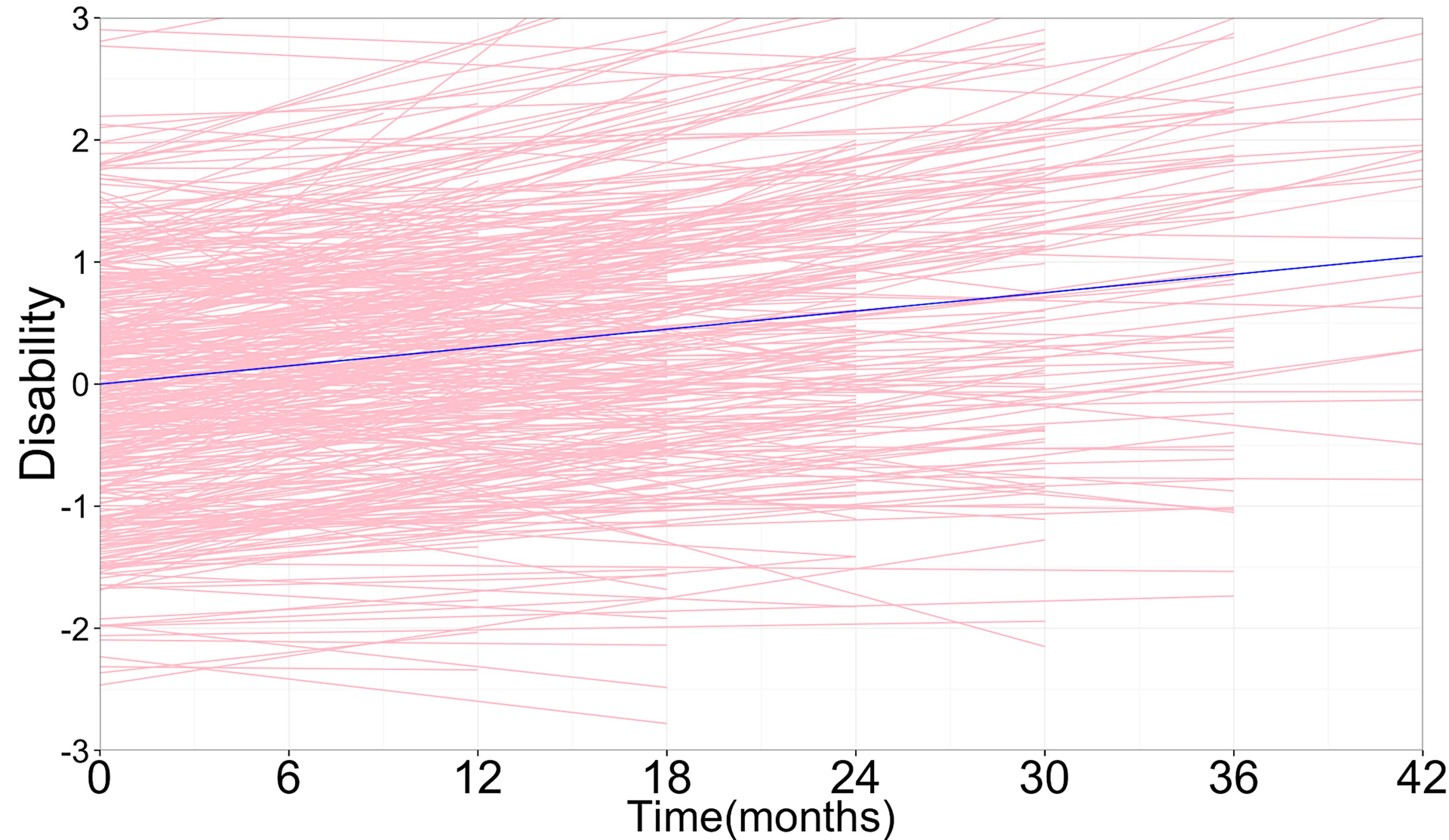
*Shift in baseline disability for a typical individual*





# Results

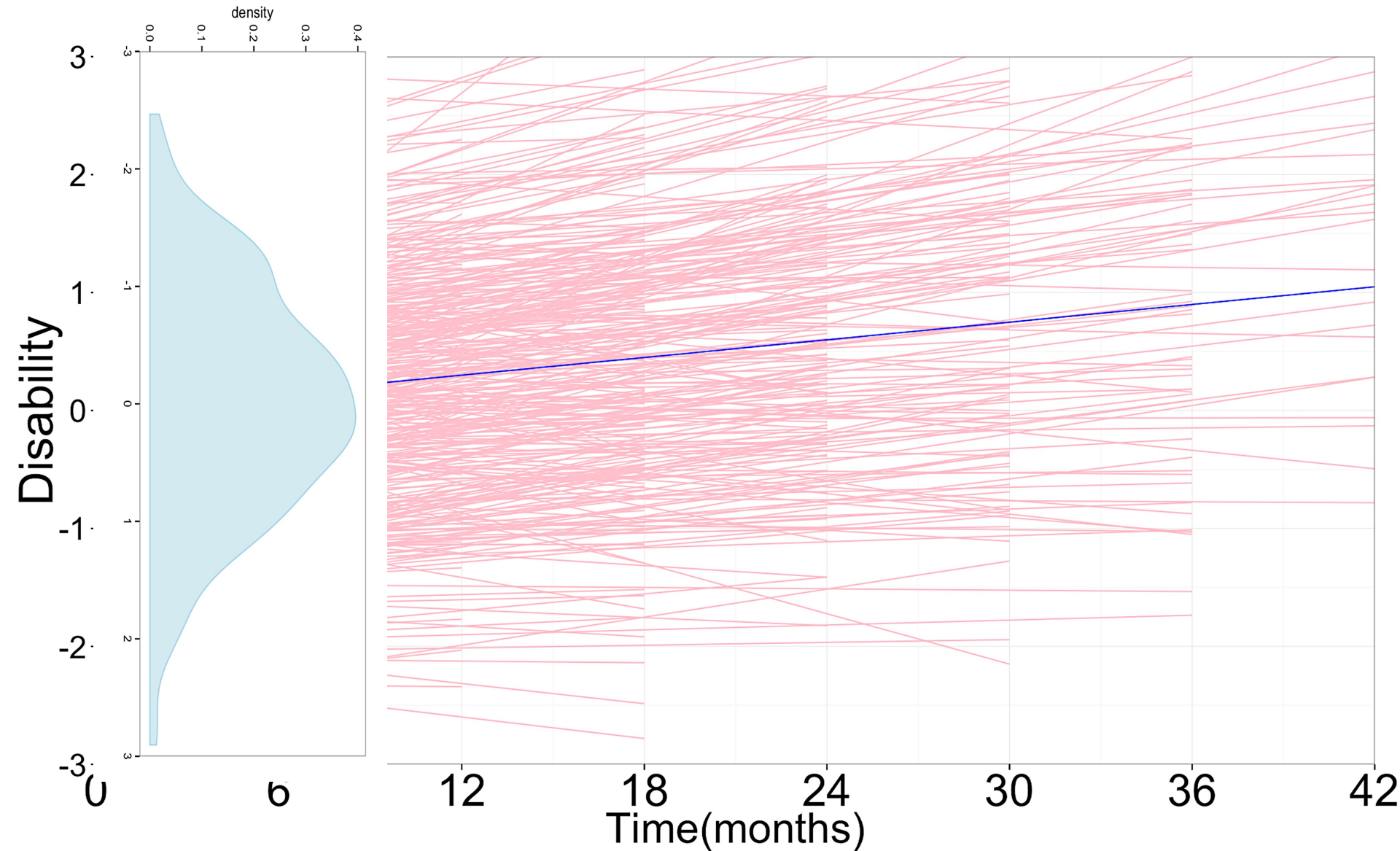
## *Longitudinal changes – De Novo cohort*





# Results

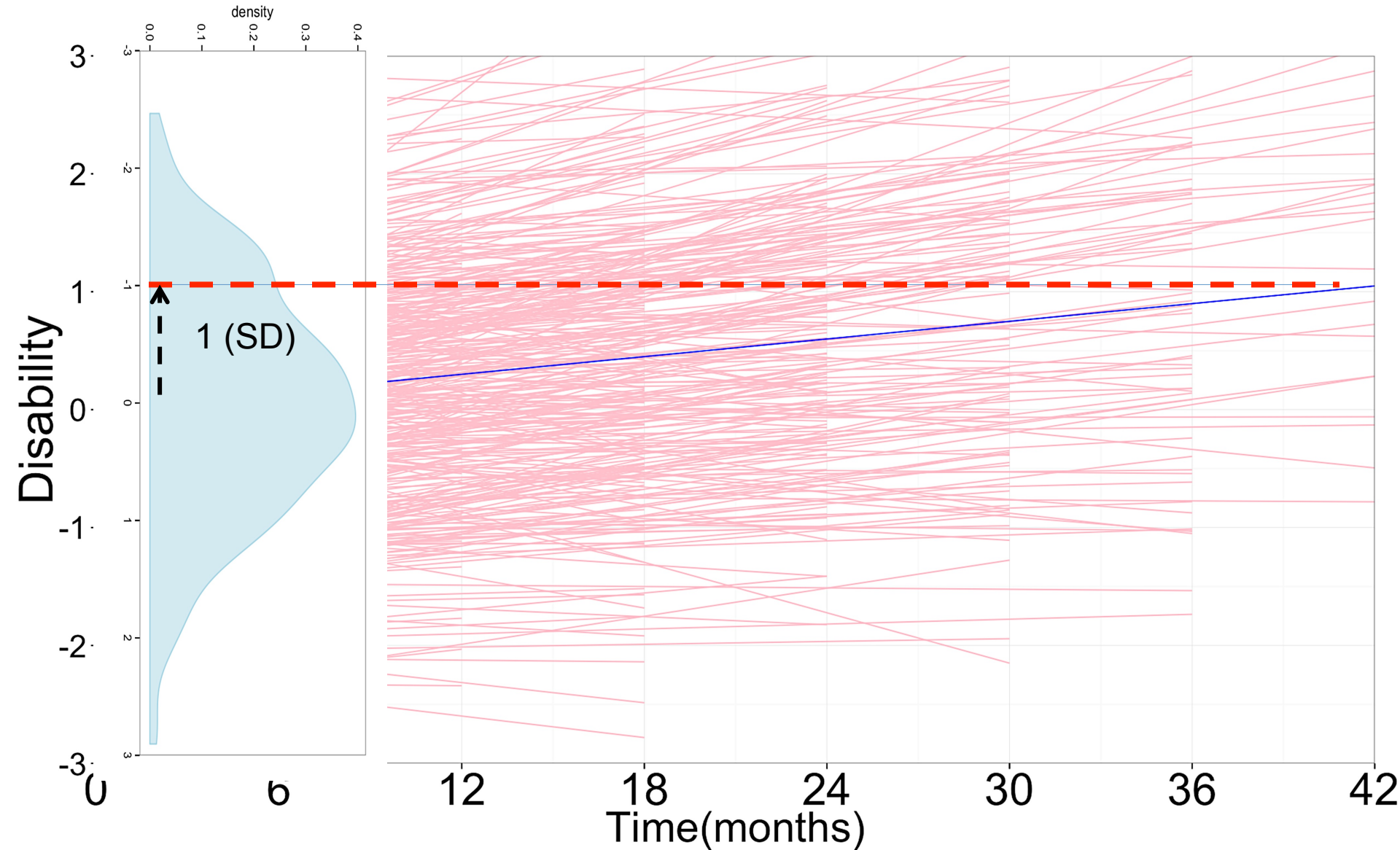
## *Longitudinal changes – De Novo cohort*





# Results

## *Longitudinal changes – De Novo cohort*

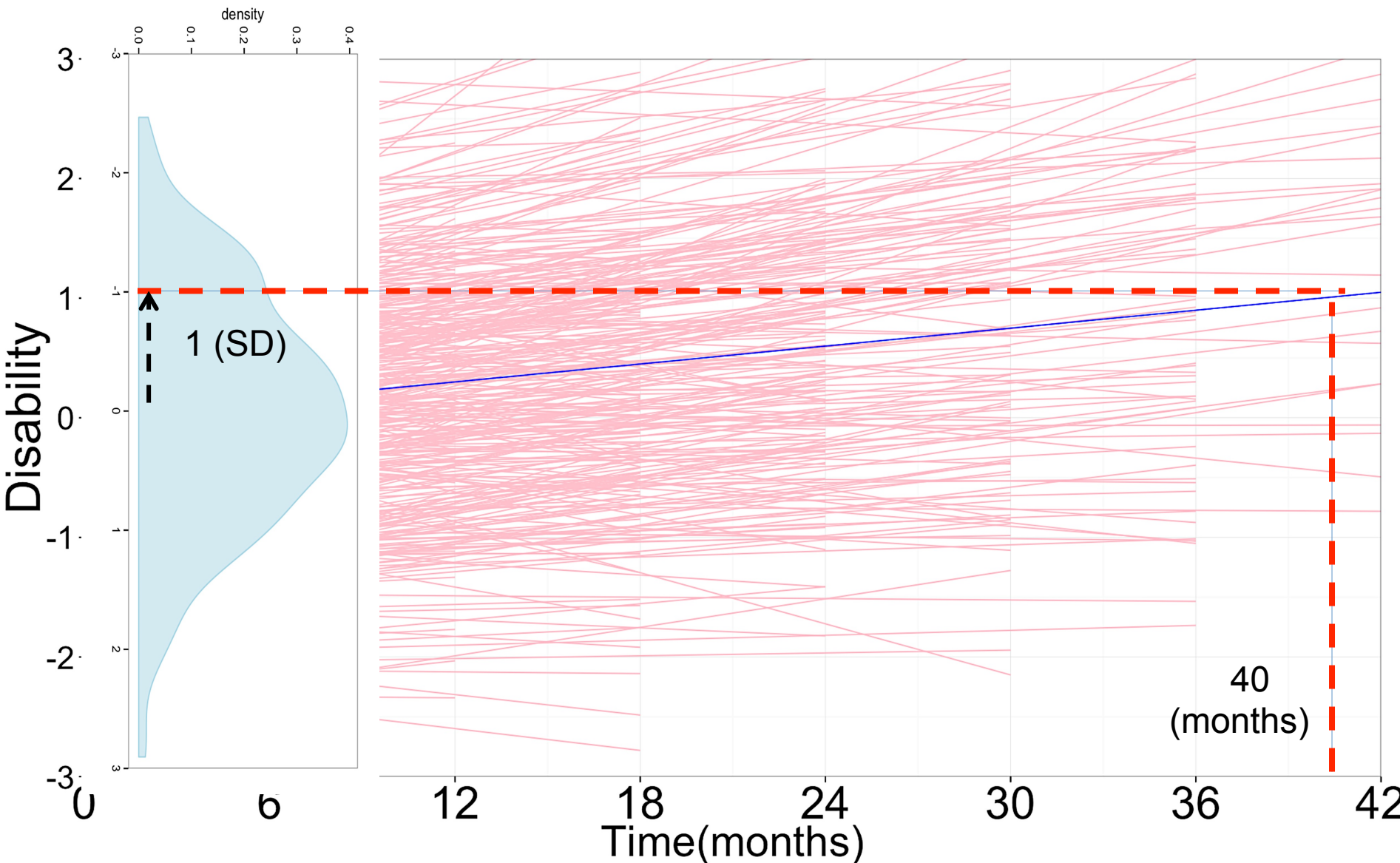


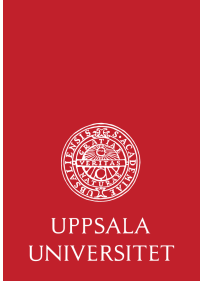




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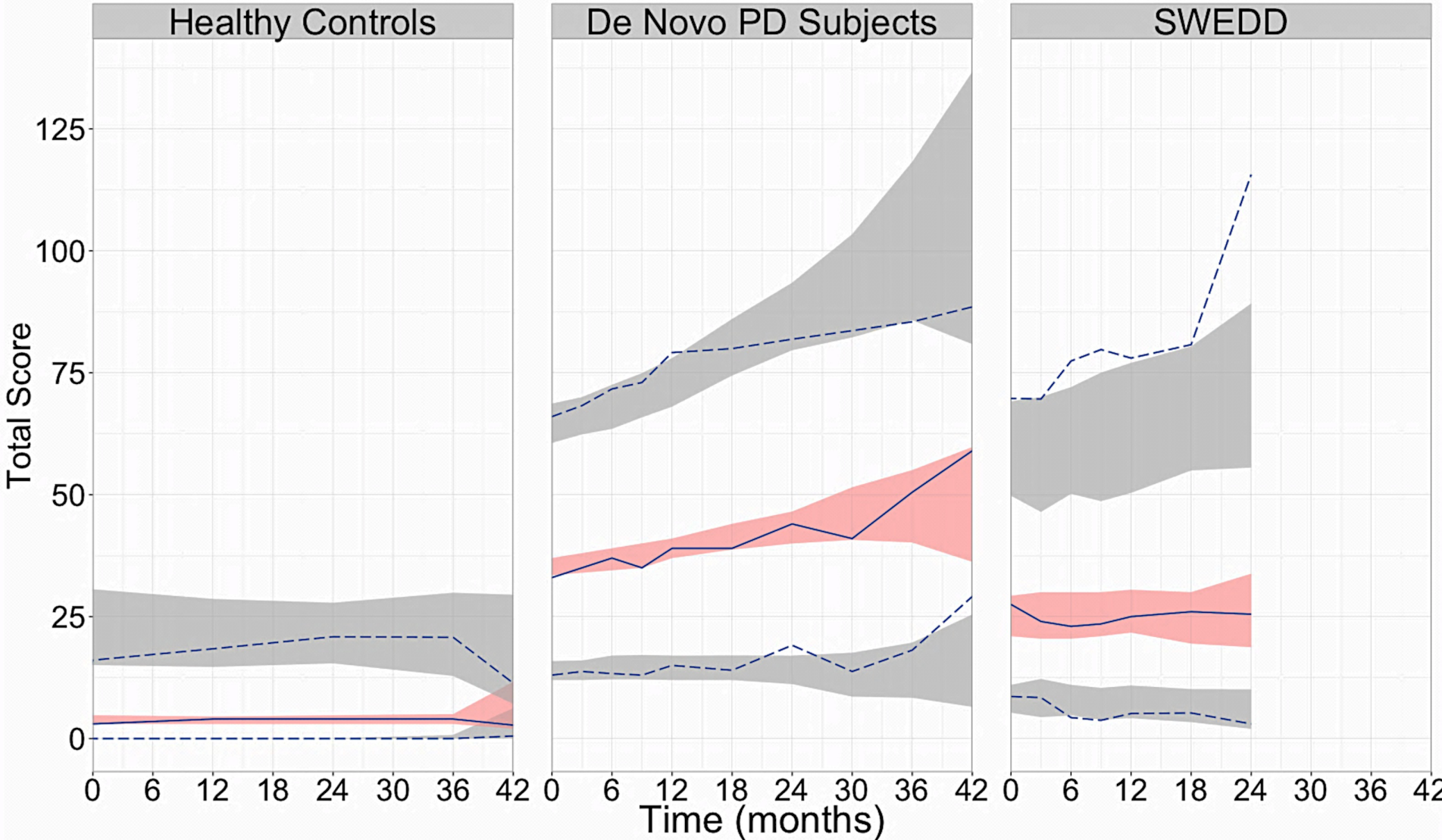
*Longitudinal changes – De Novo cohort*

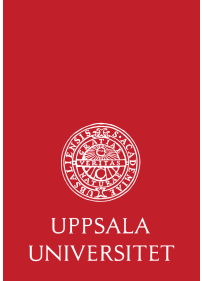




# Diagnostics

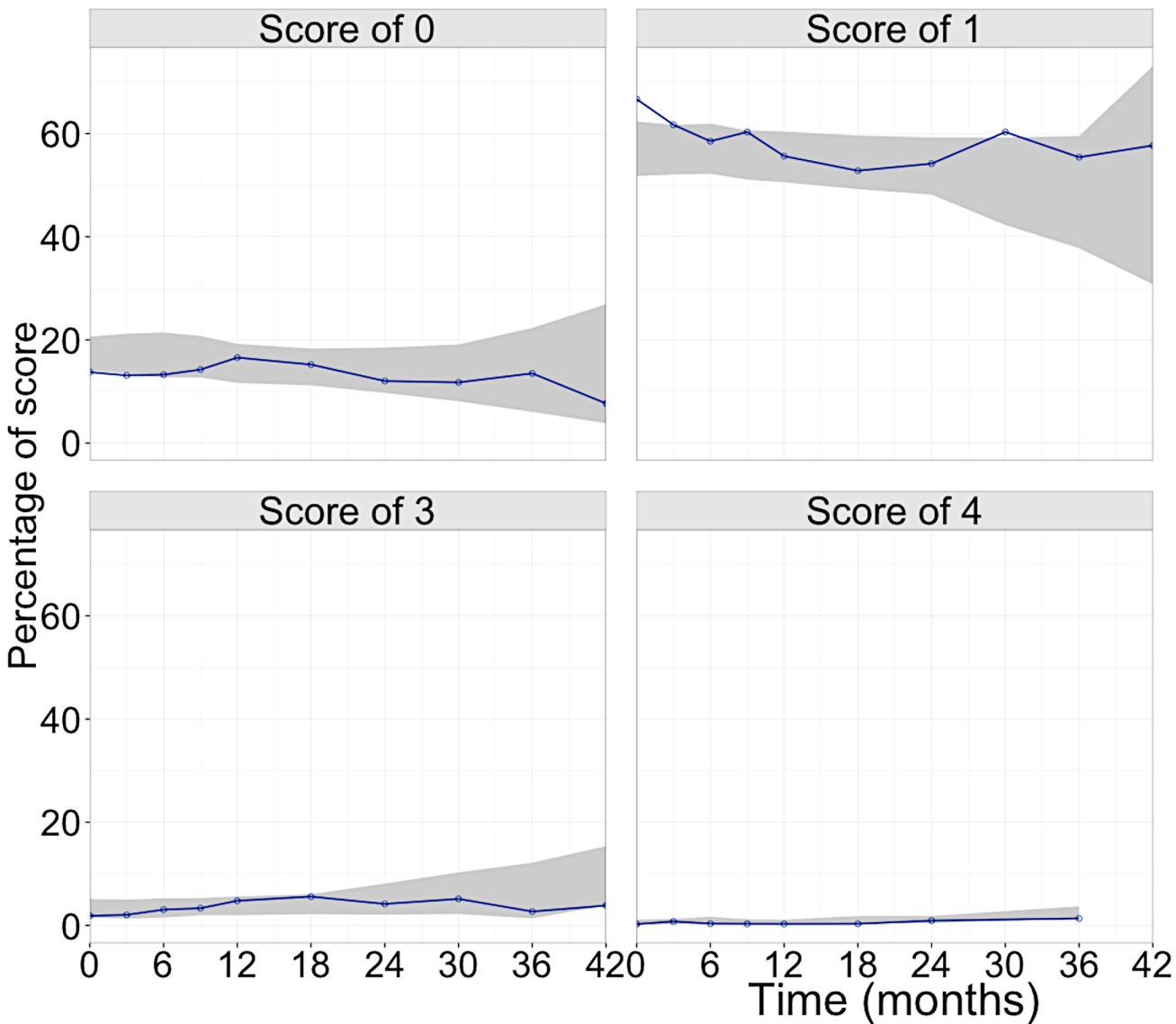
*VPC of longitudinal model – All cohorts*





# Diagnostics

*Item 23 - Longitudinal model – De Novo cohort*








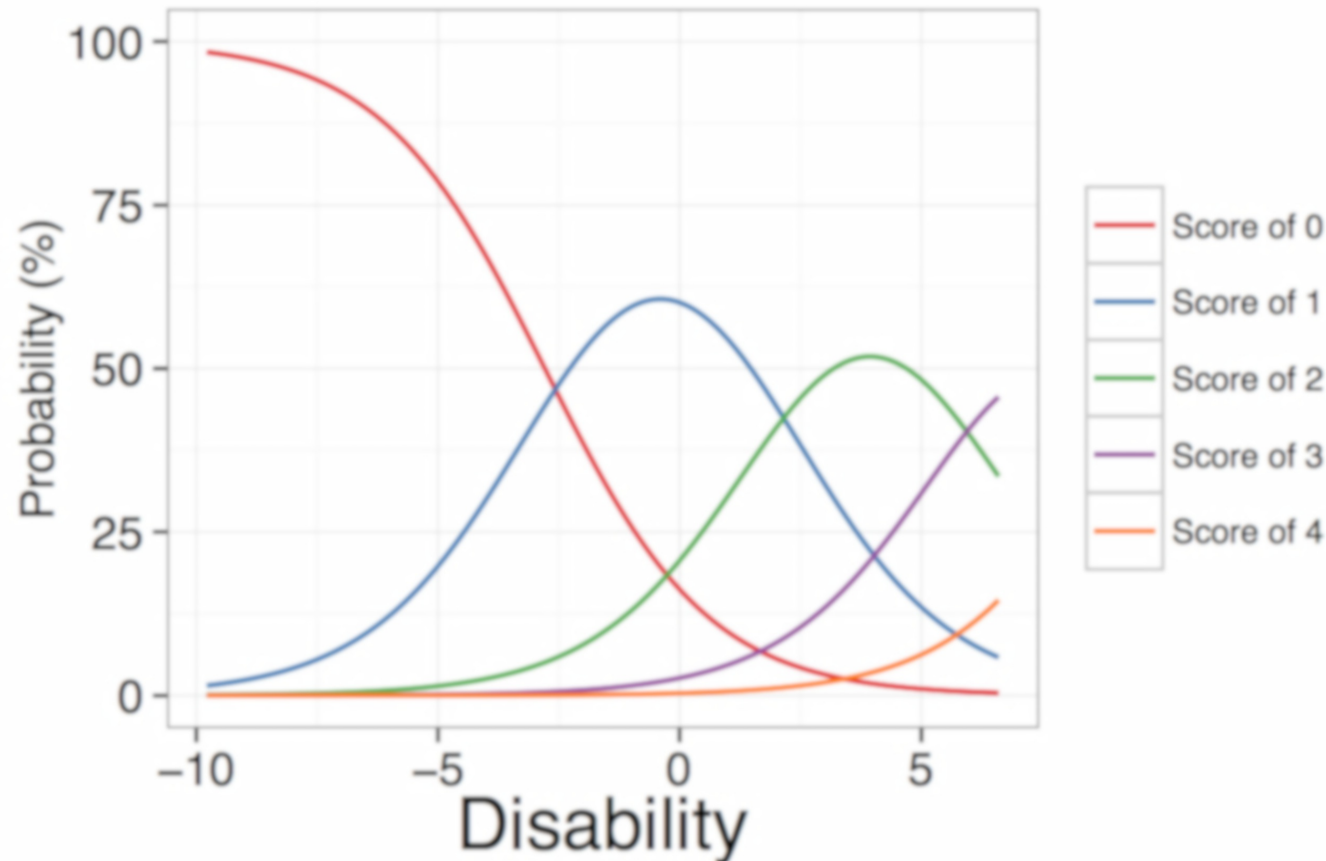
# Item Characteristic Curve

*Item 23 – Individual probabilities*

For  $i^{\text{th}}$  subject,  $j^{\text{th}}$  (23<sup>rd</sup>) item, **DV = 1**

Based on ICC

- 0 
- 1 
- 2 
- 3 
- 4 








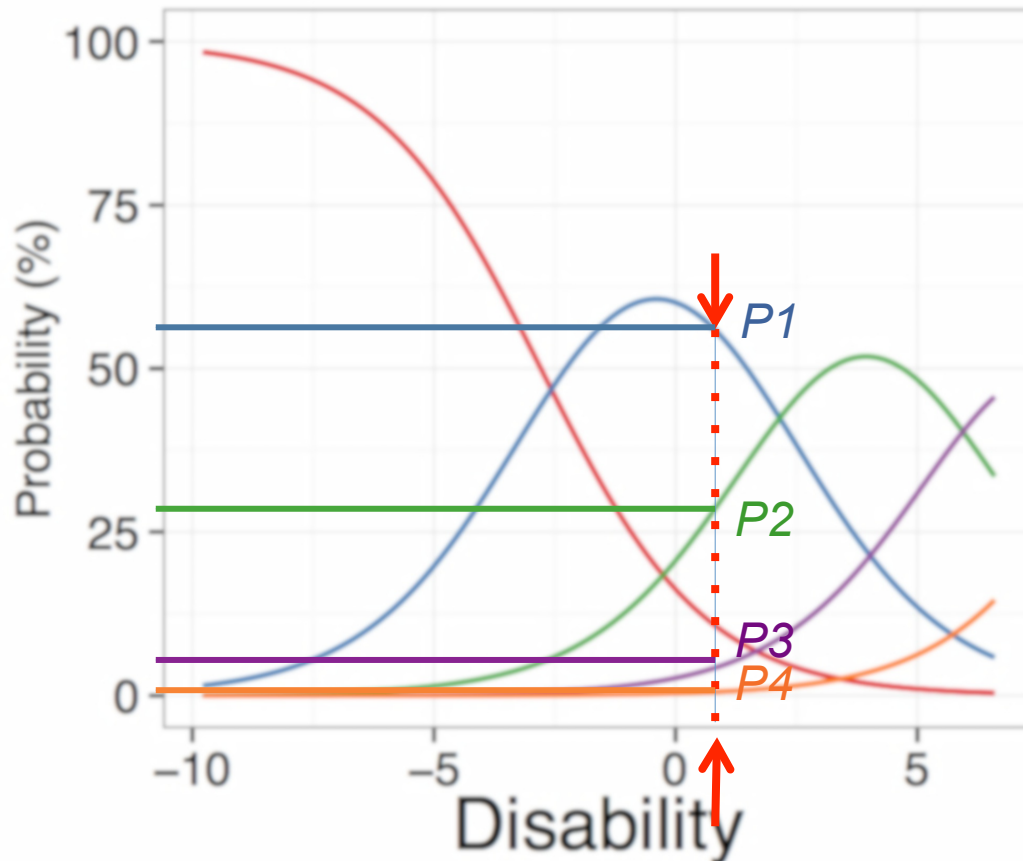
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Based on ICC

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- 2 
- 3 
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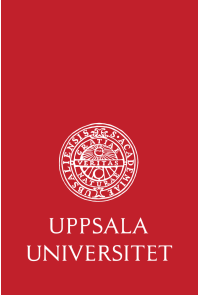
- Score of 0
- Score of 1
- Score of 2
- Score of 3
- Score of 4

$E_{ij}$  (weighted prediction)

$$= P1*1 + P2*2 + P3*3 + P4*4$$

$$RES = DV - E_{ij}$$





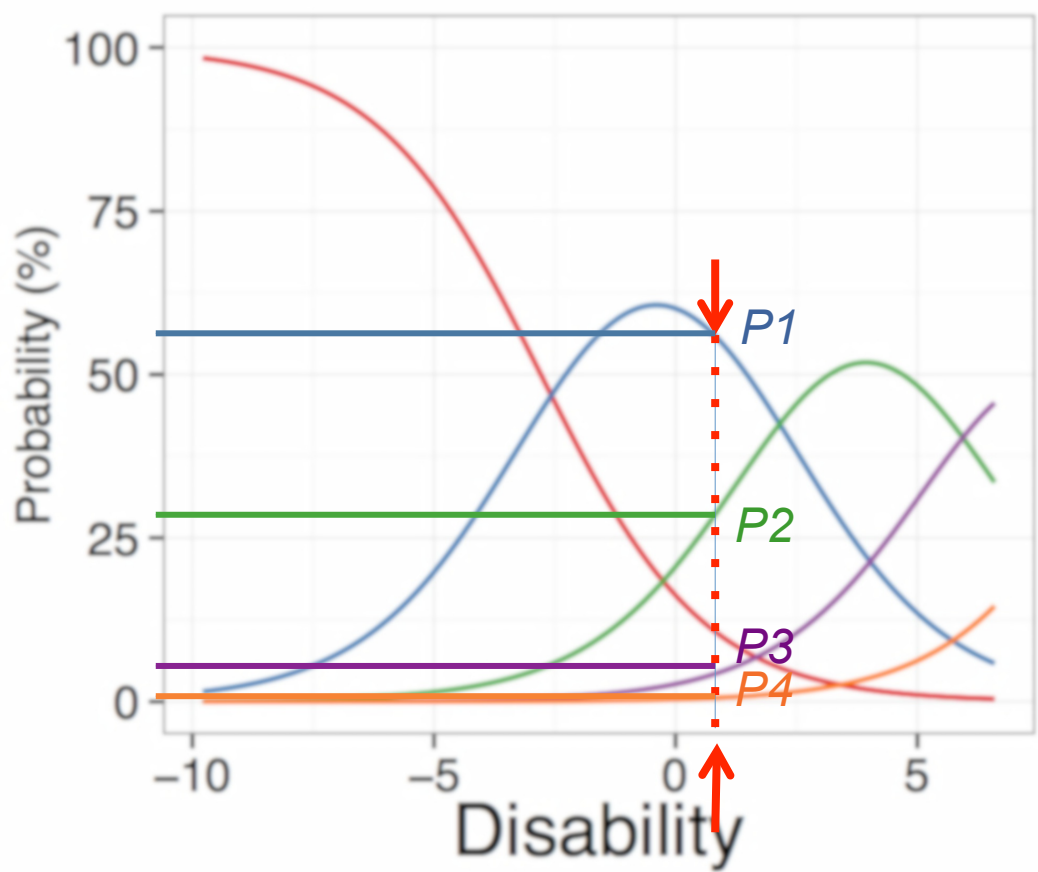
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Based on ICC

- 0
- 1
- 2
- 3
- 4

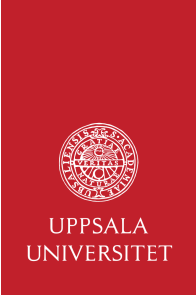


- Score of 0
- Score of 1
- Score of 2
- Score of 3
- Score of 4

$E_{ij}$  (weighted prediction)

$$= P1*1 + P2*2 + P3*3 + P4*4 = (1.289)$$

$$RES = DV - E_{ij} (-0.289)$$



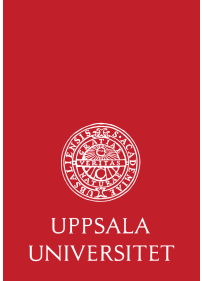
# Model-based diagnostics of ICC

## Correlation among item responses

- Already handled by the IRT model, all item responses are related to the same latent variable - disability

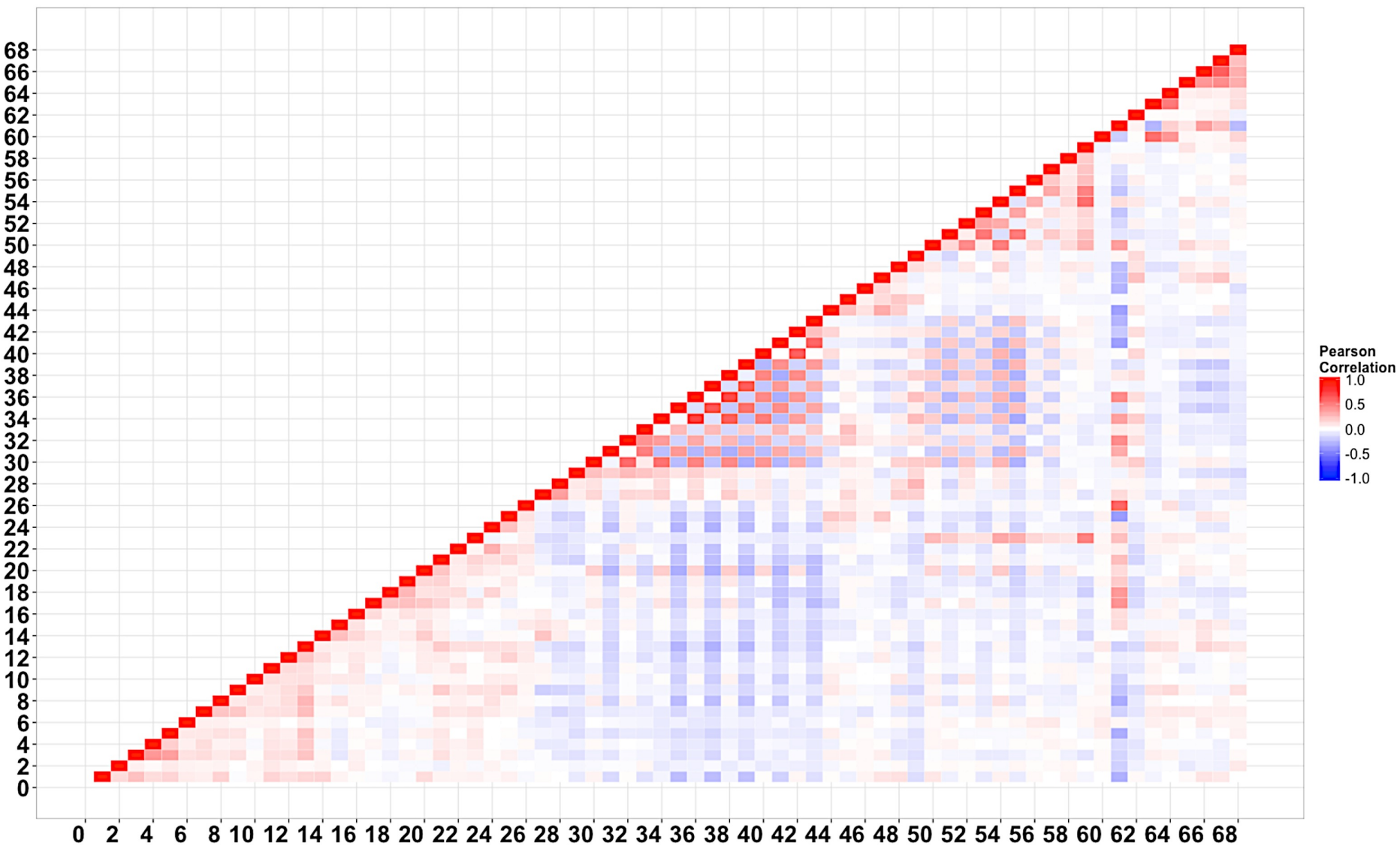
Certain item responses may be more (/less) correlated than what the model predicts

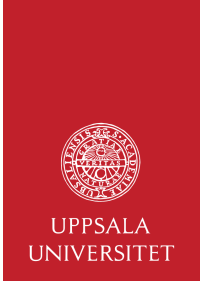
- Investigate multiple latent variables by exploring correlation of residuals among the item responses



# Correlation of residuals

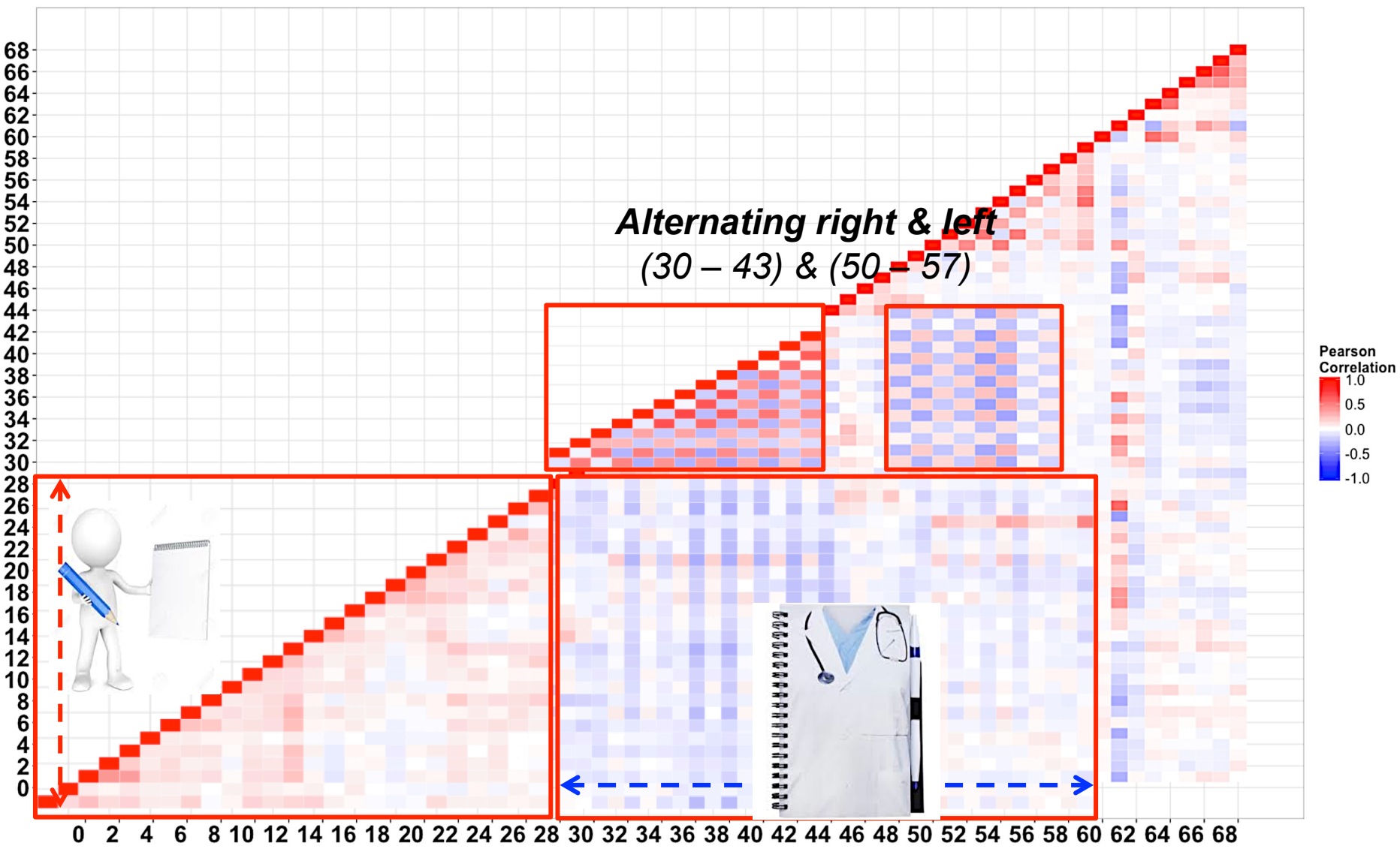
*All data from De Novo cohort ONLY – One latent variable*

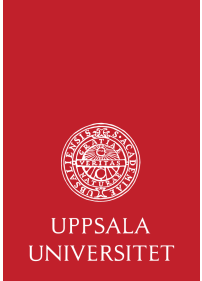




# Correlation of residuals

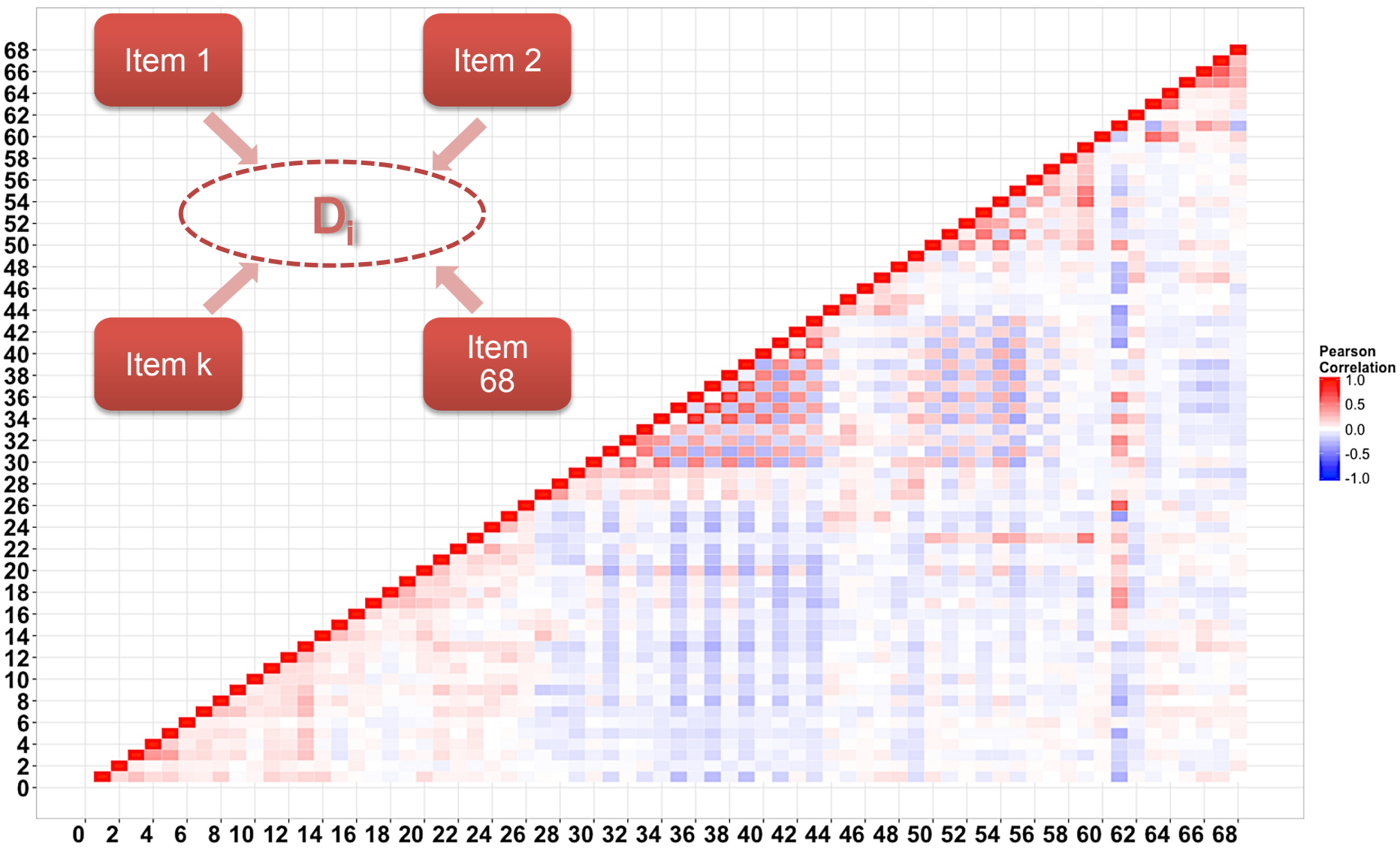
All data from De Novo cohort ONLY – One latent variable

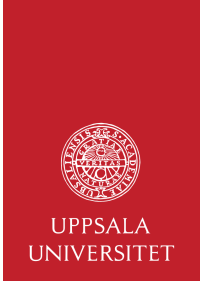




# Diagnostics – Residuals

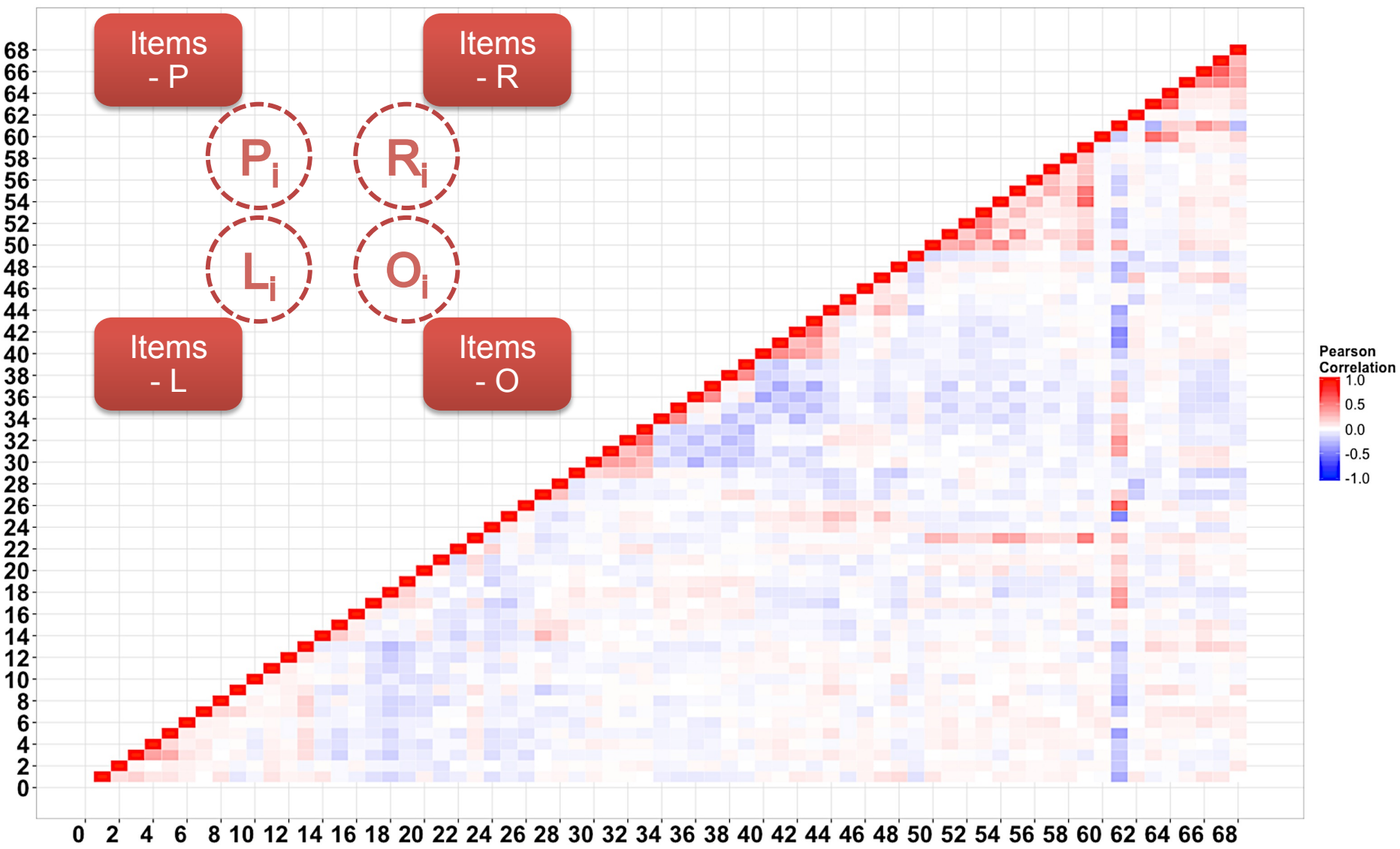
*All data from De Novo cohort ONLY – One latent variable*



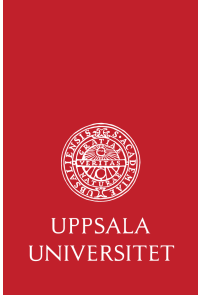


# Diagnostics – Residuals

All data from De Novo cohort ONLY – **Four** latent variables



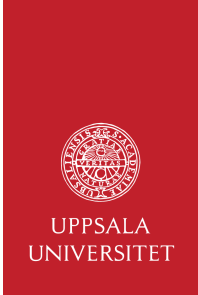




# Conclusions

## *Methodology*

- Simultaneous estimation of IRT parameters with the longitudinal changes described the data well.
  - The IRT model simulations for the **total score and at item level** were in good agreement with observations
- Model-based diagnostics based on the residuals can be used as a tool to assess the need for multiple latent variables to improve the IRT models



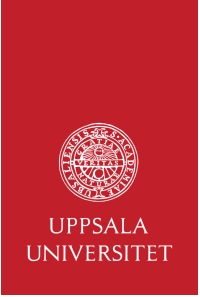
# Future direction

*Disease/patient population*

This framework may be then extended:

- To characterize the disease progression in Parkinson's
- As a basis for design and analysis of trials in Parkinson's
- Identifying false positive patients (e.g., misdiagnosed Parkinson's subjects) such as SWEDD





# Acknowledgement

- PPMI a public-private partnership – is funded by the Michael J. Fox Foundation for Parkinson's Research and industry partners
- Pharmacometrics research group, Uppsala University, Sweden