



Optimal Design To Estimate the Time Varying Receptor Occupancy Relationship in a PET Experiment

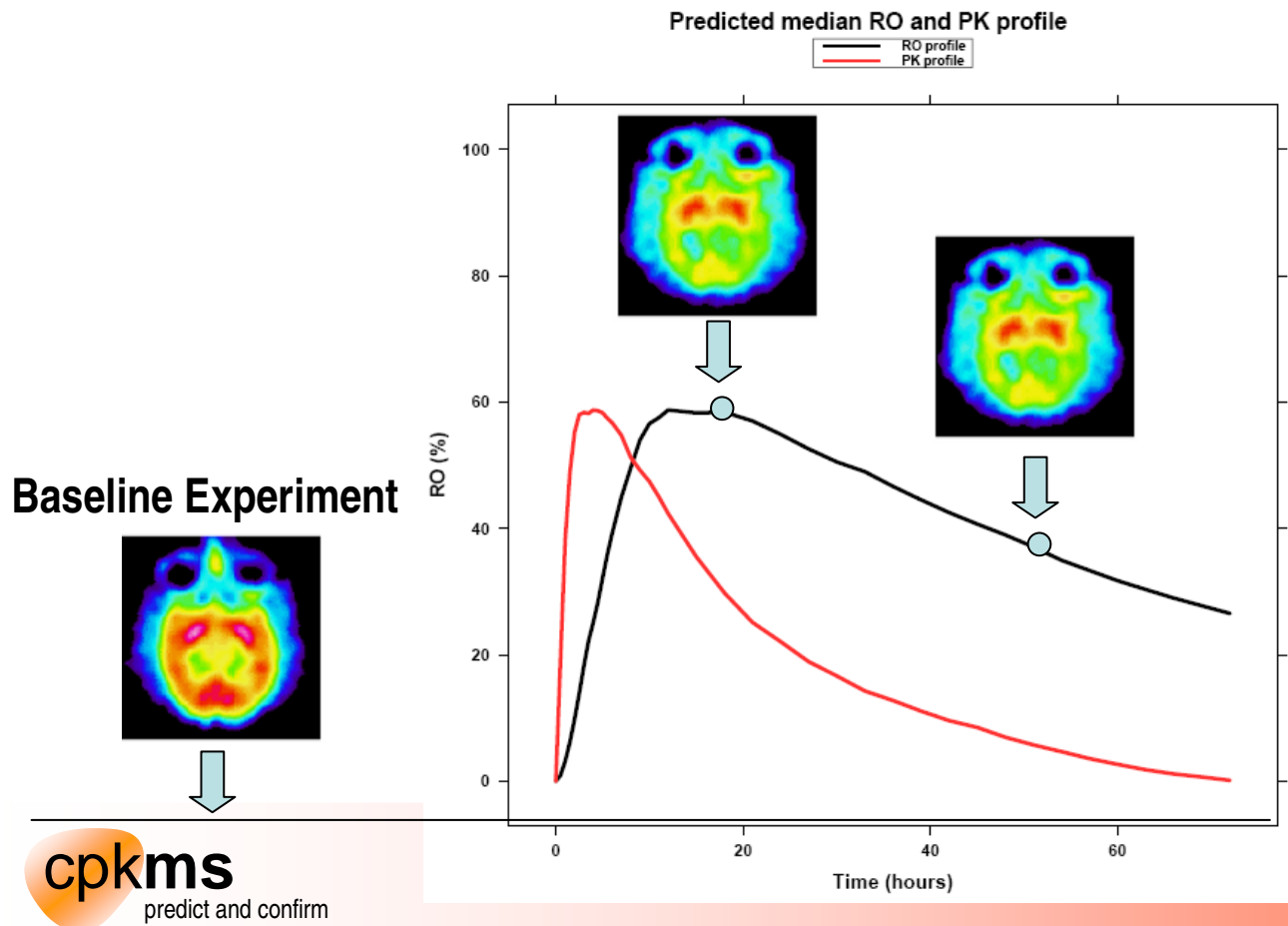
PAGE Meeting 2007, København

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Why Study PK/RO?

- Positron emission tomography (PET) is one of the most effective imaging in vivo techniques to estimate RO
- The assessment of the RO-time profile is critical to predict the time course of pharmacological response



Why Study PK/RO?

- To characterise the shape and location of the concentration-RO curve
- To explain variability in response
- To rationalise dose/dosing regimen selection
- To predict the time course of pharmacological response (therapeutic & toxic)
- To understand complex relations (tolerance, sensitisation)

Experimental design issues in a PET study

- Cost and ethical reasons limit the total number of subjects (usually $n < 20$) and the number of PET scans per individual (≤ 3 scans)
- Uncertainty in the structure of the mechanistic model relating RO and PK (*Equilibration delay, Mechanistic delay, Tolerance*)
- Inter- and intra-subject variability in PK and in drug-to-receptor binding resulting in an overall inflation in variability
- Need to estimate typical exposure/RO link in a target patient population (fraction of subjects achieving an 'effective' RO in a chronic treatment)

Time course RO – Mechanistic models

- Typically a direct link between plasma concentrations and RO is assumed
- To account for delay/hysteresis between occupancy levels and plasma concentration the following models* can be applied:

Effect Compartment Model

$$\frac{dC_E}{dt} = k_{eo} \cdot (C_P - C_E) \quad \longrightarrow \quad \%RO = 100 \frac{C_E}{EC_{50} + C_E}$$

Receptor Association-Dissociation Model

$$\frac{dRO}{dt} = k_{on} \cdot C_P \cdot (R_T - RO) - k_{off} \cdot RO$$

R_T = maximum receptor occupancy (fixed at 100%)
 RO = observed receptor occupancy time course data

Combined Biophase / Receptor Association-Dissociation Model

$$\frac{dRO}{dt} = k_{on} \cdot C_E \cdot (R_T - RO) - k_{off} \cdot RO$$

Optimal Population Design

$$\begin{aligned}
 CP_i &= f(\theta_{CP_i}, \xi_{CP_i}) + \varepsilon_{CP_i} && \text{Population PK model (fixed effect)} \\
 RO_i &= g(CP_i, \theta_{RO_i}, \xi_{RO_i}) + \varepsilon_{RO_i} && \text{Population PK/RO model (fixed effect)} \\
 \theta_i &\in N(\Phi, \Omega) && \text{Population PK/RO parameters (random effect)} \\
 \Xi &&& \text{Population design vector of PK and RO sampling times } (\xi) \\
 \Psi &&& \text{Vector of population fixed } (\Phi) \text{ and random effect } (\Omega) \text{ parameters}
 \end{aligned}$$

For a given individual with design ξ

$$M_F(\Psi, \xi) = E\left(-\frac{\partial^2 l(\Psi; y)}{\partial \Psi \partial \Psi^T}\right)$$

$l(\Psi; y)$ is the log-likelihood of vector of observation y of individual for the population parameters

Population Fisher information matrix (PFIM):
$$M_F(\Psi, \Xi) = \sum_{i=1}^N M_F(\Psi, \xi_i)$$

Designs are optimized maximizing the determinant of the PFIM with respect to Ξ assuming known Ψ

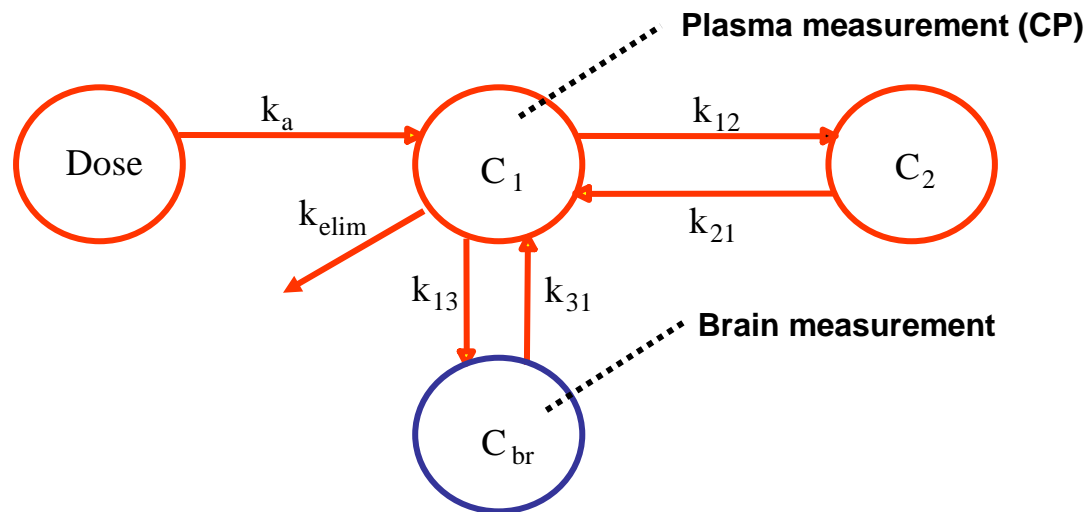
$$\det[M_F(\Psi, \Xi)]^{\frac{1}{\dim(\Psi)}}$$

Case study: Optimal study design

- PK/PD model was defined using pre-clinical data (kon/koff) and human PK data (considered fixed)
- Optimal design was performed to allocate PET scans at the most informative time-points
- Various designs exploring the influence of optimizing the PET scan time allocation, the number of subjects to elementary design and the number of dose levels were considered
- Optimisation was performed using WinPOPT^{®*}
- Study designs: 16 subjects in total, up to 4 doses (1.5, 2.5, 4 and 6 mg), and 3 PET scans per subject

Modelling time-course RO data

- A mechanistic model was developed using pre-clinical data to estimate the RO time-course and the time-varying link between PK and RO based on k_{on} and k_{off} parameters



1) Modelling of plasma/brain data

2) Receptor Association-Dissociation Model

C_p = predicted plasma concentrations (input function)

R_T = maximum receptor occupancy (fixed at 100%)

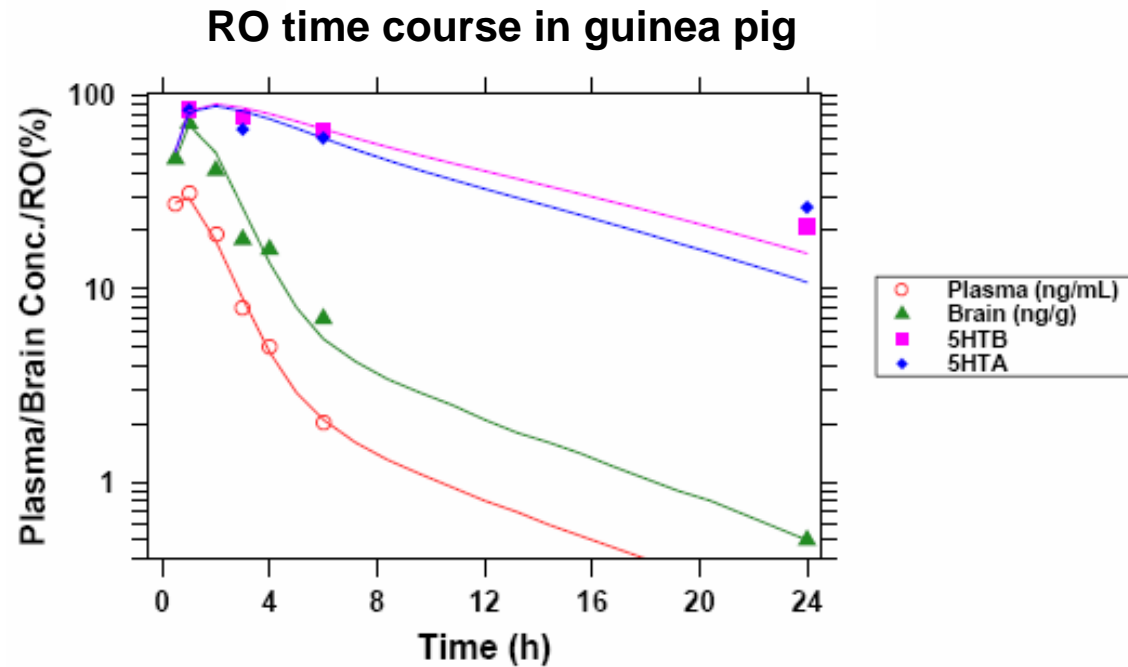
RO = observed receptor occupancy time course data

k_{on} = association binding rate constant

k_{off} = dissociation binding rate constant.

$$\frac{dRO}{dt} = k_{on} \cdot C_p \cdot (R_T - RO) - k_{off} \cdot RO$$

Preclinical data - Results



PK/RO parameters estimates			
Receptor	k_{on} (ml.ng ⁻¹ .h ⁻¹)	k_{off} (h ⁻¹)	$Kd=k_{off}/k_{on}$ (ng/ml)
5-HT _{1A}	0.088	0.221	2.5
5-HT _{1B}	0.088	0.183	2.1

Population PK/PD model

- Optimization was performed on the PK/PD model based on pre-clinical data ($k_{on}=0.088$ and $k_{off}=0.221$, variability=30%) and human PK data (first order absorption with 2 comp. model)

Parameter (units)	Fixed effects	Between-subject variance	Population distribution
CL (L/h)	34.9 Fixed	0.112 Fixed	Log normal
VSS (L)	1200 Fixed	0.134 Fixed	Log normal
Q (L/h)	21.7 Fixed	0.179 Fixed	Log normal
FVC	0.67 Fixed	0 Fixed	Normal
Ka (h^{-1})	0.605 Fixed	0.97 Fixed	Log normal
Kon (h^{-1})	0.088	0.1	Log normal
Koff (h^{-1})	0.221	0.1	Log normal
σ^2	0.1	-	Proportional

Optimality criteria improved trial efficiency

Number of doses	Number of groups (n. groups x dose)	Sampling times	Efficiency (%)
4 (2.5, 4, 6, 1.5)	4 (1, 1, 1, 1)	{6, 48}; {6, 48}; {6, 48}; {6, 48} Empirical design (1)	50
4 (2.5, 4, 6, 1.5)	4 (1, 1, 1, 1)	{6, 48}; {6, 24}; {3, 36}; {6, 48} Empirical design (2)	100 (crit = 73.57)
4 (2.5, 4, 6, 1.5)	4 (1, 1, 1, 1)	{5.21 13.9}; {3.9 13.9}; {9.83 13.9}; {5.73 15.1}	558
2 (1.5,6)	8 (4, 4)	{5.73, 15.1} {5.73, 15.1} {5.73, 15.1} {5.73, 15.1}; {10.7, 15.1} {7.54, 11.7} {4.74, 9.01} {9.83, 13.9}	563
4 (1.5, 2.5 ,4 ,6)	8 (2, 2, 2, 2)	{5.73, 15.1} {5.73, 15.1}; {4.74, 13.9} {4.74, 13.9}; {3.90, 13.9} {10.7, 15.1}; {8.24, 12.7} {10.7, 15.1}	554
3 (2.5, 4, 6)	8 (3, 2, 3)	{4.74, 13.9} {4.74, 13.9} {4.74, 13.9}; {3.9, 13.9} {3.9, 13.9}; {9.83, 13.9} {9.83, 13.9} {9.83, 13.9}	549

- number of groups and number of doses appear not to be relevant
- sampling time has been identified as the key driver to optimize the design

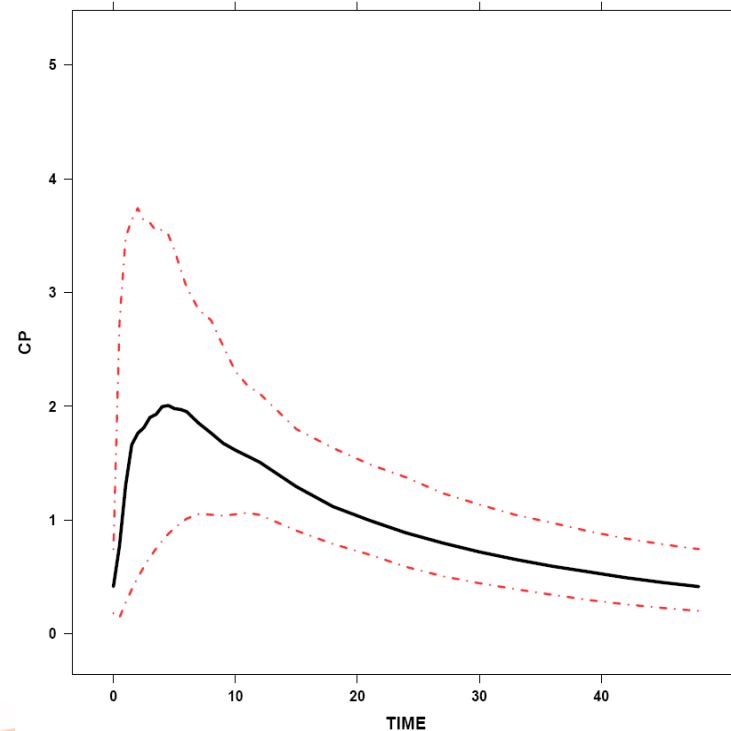
Simulation approach to assess the design performance

- Simulate RO time course with optimal and empirical time-points (~ Cmax and trough levels)
- Study design: 4 doses (1.5, 2.5, 4 and 6 mg); 4 subjects per dose (16 subjects in total)
- RO were sampled at two time-points
 - Empirical design: {6, 48} {6, 24} {3, 36} {6, 48}
 - Optimal design (at least 4 hours between two PET scans): {5.21 13.9} {3.9 13.9} {9.83 13.9} {5.73 15.1}
- Test the performance of the two approaches (bias, precision and accuracy)

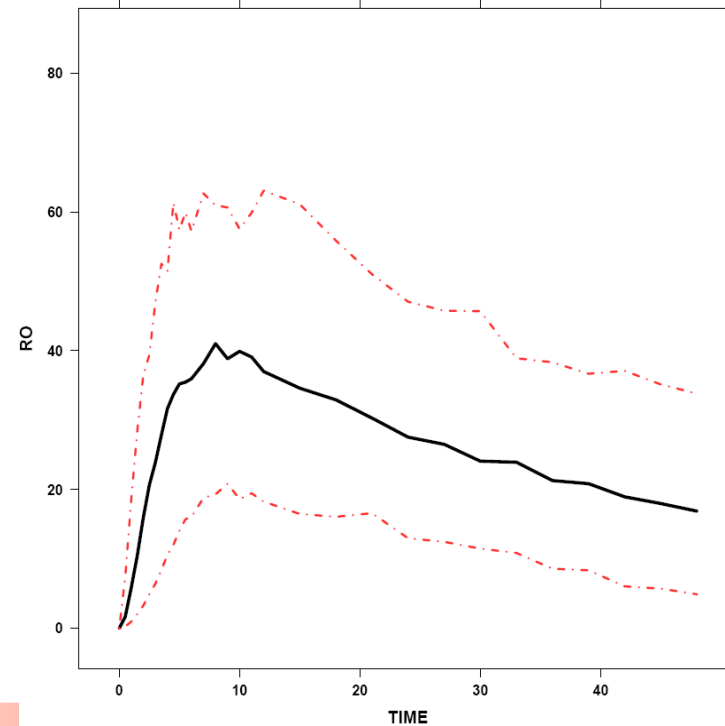
PK and RO profile (typical dose)

- PK/PD model defined using pre-clinical data ($k_{on}=0.088$ and $k_{off}=0.221$, variability=30%) and human PK data (first order absorption with 2 comp. model)
- N=1600 subjects were generated from the PK/RO model

PK profile (Median with 5th and 95th perc.)

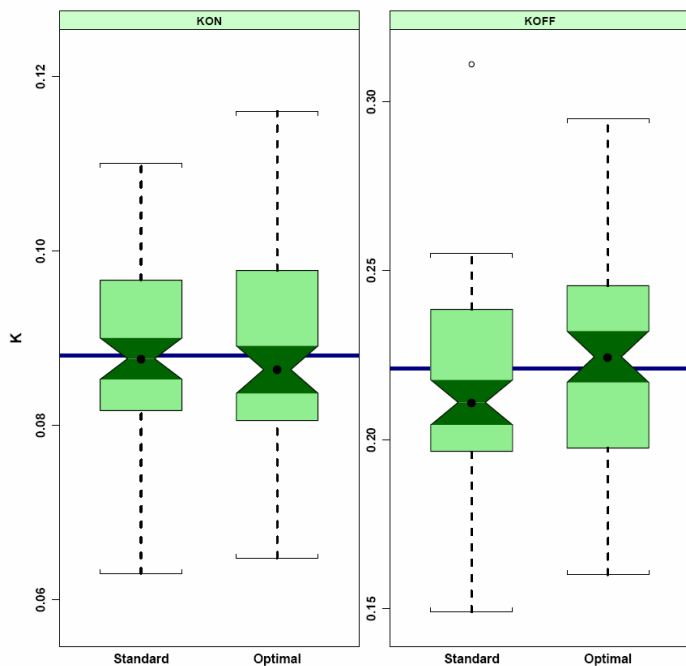


RO profile (Median with 5th and 95th perc.)



Simulation – Results

- 100 trials (with 16 subject/trial) were generated using a Monte Carlo simulation approach
- A non-linear mixed-effect methodology was used to estimate the kon and koff parameters with their inter-individual variability
- Performances were measured as bias, precision and accuracy on kon and koff estimates

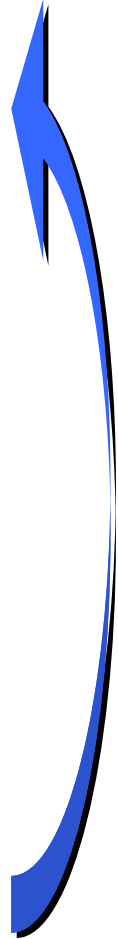
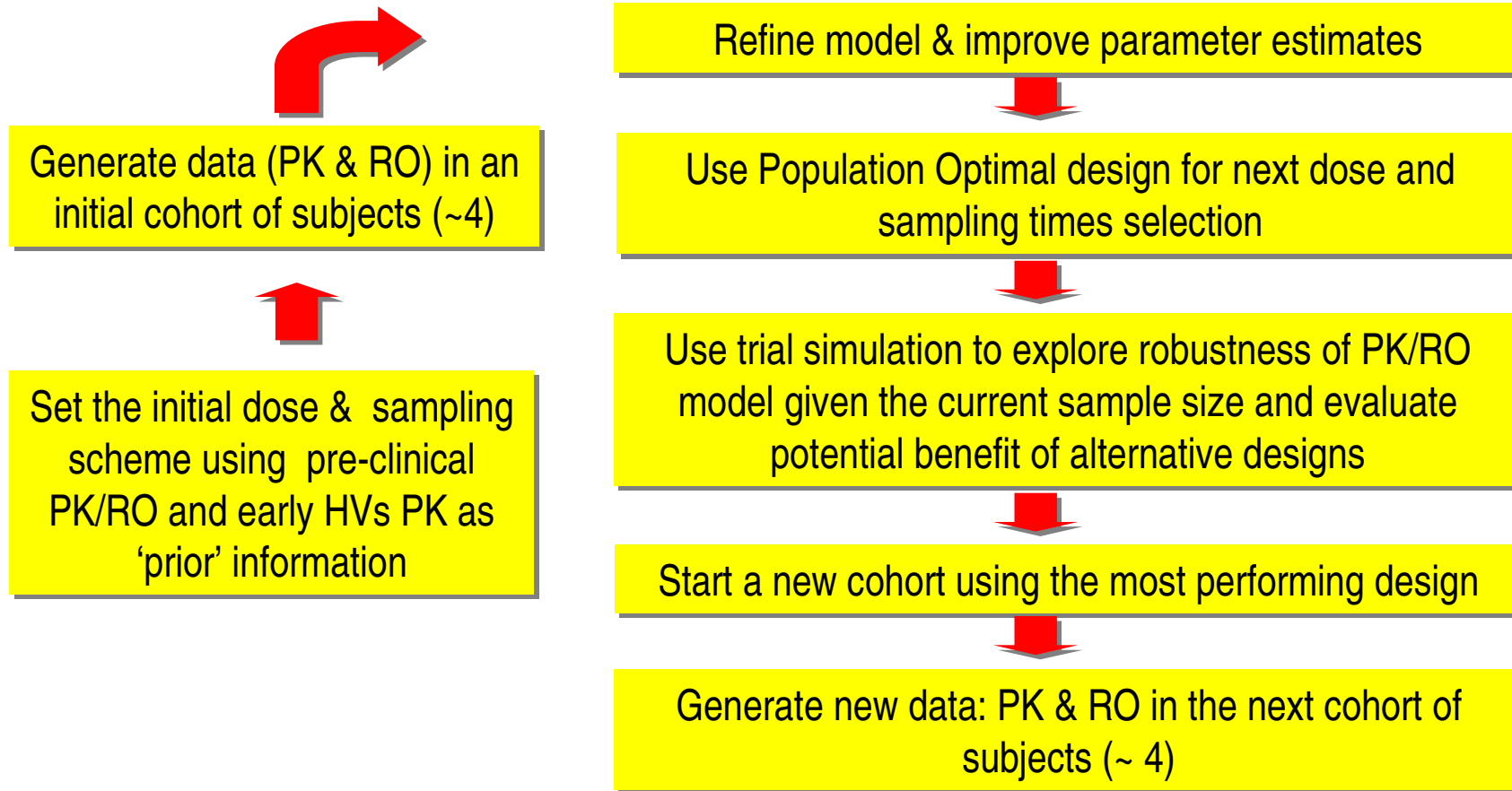


Performance	Measure	Standard		Optimal	
		Kon	Koff	Kon	Koff
Unscaled measures					
Bias	ME	3.32	6.84	0.0274	0.0799
Precision	Var	216	898	0.0692	0.614
	SD	14.7	30.0	0.263	0.783
Accuracy	MSE	227	944	0.0699	0.620
Scaled measures					
Bias	SME	37.7	31.0	0.311	0.361
Precision	CV	431	424	228	260

ME = mean error, Var = variance, SD = standard deviation, MSE = mean square error, SME = scaled mean error, CV = coefficient of variation

As expected the optimal study design approach provided more accurate and reliable model parameter estimates

Design of sequential PET experiments based on Optimality Criteria



Conclusions

- A mechanistic model has been proposed to estimate the RO time-course and the time-varying link between PK and RO
- Optimal study design approach provided more accurate and reliable model parameter estimates
- The use of sequential model design could increase the efficiency of the study for the PK/RO assessment especially when the human receptor kinetic model cannot be properly inferred from animal estimates
- Further work to develop a standardized methodology for the use of sequential optimal design approach is in progress