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Analysis Approaches Handling Both Event Frequency & Symptomatic Severity

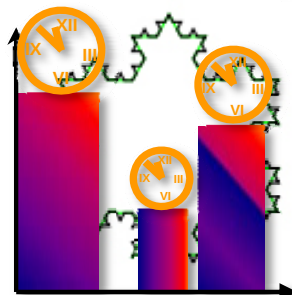
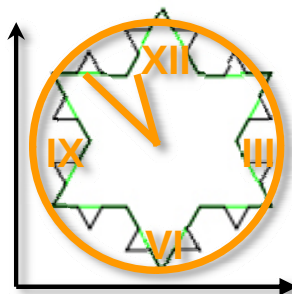
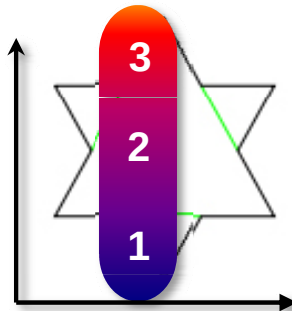
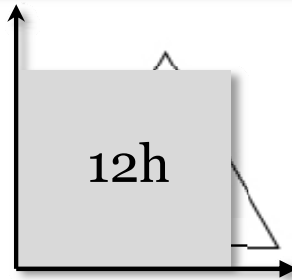
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Outcome data

- o Background
- o Objectives
- o Methods
- o Results
- o Conclusions





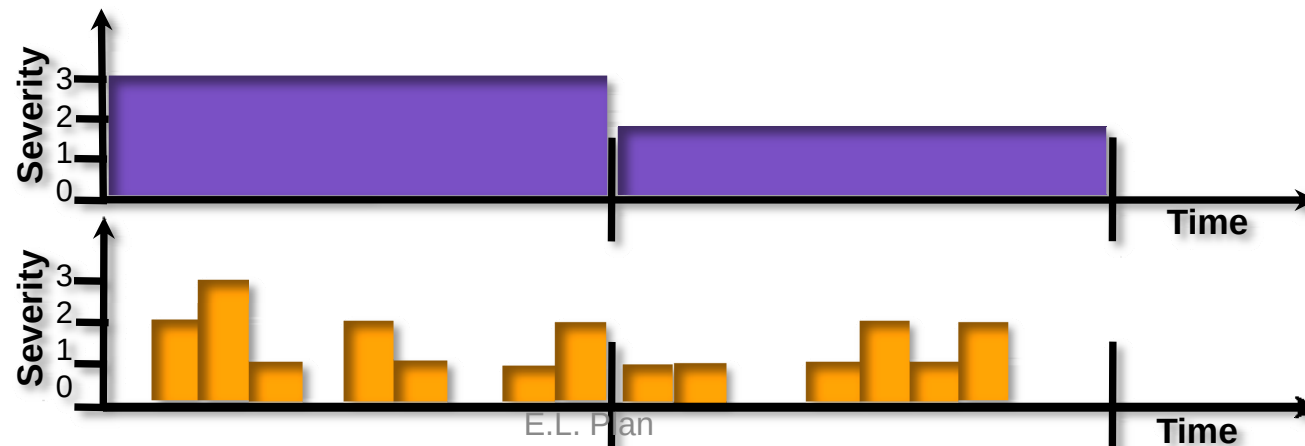
OC model

➤ An ordered categorical approach

- Analgesic efficacy [0-4] pain relief index [Sheiner, L.B. CPT (1994)]
- Intestinal toxicity [0-4] diarrhea score [Xie, R. et al. CPT (2002)]

➤ Pros & Cons

- 👍 IIV, time-course, drug effect better described by use of ALL severity grades
- 👎 Data simplification still remaining by recording only WORST diarrhea score per 3-w. course





Rationale

- Data to model often complex:
 - ➔ Simplifications done
 - ➔ Information lost
 - Last 20y, NLME approach accompanied with:
 - ➔ Computing power
 - ➔ Estimation method performance
 - Models treating data in their true nature!
 - **Event at a particular time**
 - + **of a particular severity**
- = Repeated Time-To-Categorical Event (RTTCE)**





Objectives

- To introduce new mixed-effects models addressing the original nature of data
- To illustrate their benefits in terms of:
 - Goodness of fit
 - Simulation properties
 - Drug effect assessment
 - Drug effect detection power



[<http://www.nedarc.org/nedarc/analyzingData/index.html>]



RTTCE model

➤ Combine Repeated Time-To-Event model

• **Probability (no event occurring) =**

$$h(t) = \theta_{\beta} \cdot e^{\eta_{\beta i}} \cdot f(PK_i, t, X_i)$$

$$P(Y_{ij} = 0, t_j > T > t_{j+1} | \eta_i) = e^{-\int_{t_j}^{t_{j+1}} h(t) dt}$$

Y = dependent variable
 t = independent variable
 i = patients
 j = observation point
 θ = population median
 η = random effect
 h = hazard
 PK = drug exposure
 X = covariate
 m = instant degree of severity

➤ & Ordered Categorical model

• **Probability (occurring event of severity m) =**

$$\text{Logit}[P(Y_{ij} \geq m | \eta_i)] = \theta_{\alpha_m} + \eta_{\alpha_i} + g(PK_i, t, X_i)$$

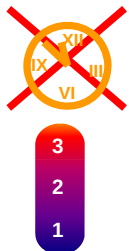
$$P(Y_{ij} \geq m | \eta_i) = \frac{e^{\text{Logit}[P(Y_{ij} \geq m | \eta_i)]}}{1 + e^{\text{Logit}[P(Y_{ij} \geq m | \eta_i)]}}$$

$$P(Y_{ij} = m | \eta_i) = (P(Y_{ij} \geq m | \eta_i) - P(Y_{ij} \geq (m+1) | \eta_i)) \cdot (1 - P(Y_{ij} = 0 | \eta_i))$$



RTTCE features

- Models simultaneously two aspects of the data
- Enables drug effect on both:
 - Frequency aspect → fewer events
 - Severity aspect → lower proportion of severe vs mild
- Pros & Cons
 - 👍 Model treating data in their true nature!
 - 👎 Data must have been recorded as such,
If not, if maximal events per time-intervals reported:



**Repeated Categorical Event per Time-interval
(RCE_pT)**



RCEpT model

➤ Combine Repeated Time-To-Event model

• *Probability (no event per time-interval) =*

$$h(t) = \theta_{\beta} \cdot e^{\eta_{\beta_i}} \cdot f(PK_i, t, X_i)$$

$$P(Y_{ij} = 0, t_j > T > t_{j+1} | \eta_i) = e^{-\int_{t_j}^{t_{j+1}} h(t) dt} = e^{-\lambda}$$

Y = dependent variable
 t = independent variable
 i = patients
 k = observation interval
 θ = population median
 η = random effect
 h = hazard
 PK = drug exposure
 X = covariate
 m = max. degree of severity
 n = number of $Y > 0$ per interval

➤ Ordered Categorical & Count models

• *Probability (max m of severity of expected number of events per time-interval) =*

$$\text{Logit}[P(\max(Y_{ik}) \geq m | \eta_i)] = \theta_{\alpha_m} + \eta'_{\alpha_i} + g(PK_i, t, X_i)$$

$$P(\max(Y_{ik}) \geq m | \eta_i) = \frac{e^{\text{Logit}[P(\max(Y_{ik}) \geq m | \eta_i)]}}{1 + e^{\text{Logit}[P(\max(Y_{ik}) \geq m | \eta_i)]}}$$

$$P(\max(Y_{ik}) = m | \eta_i) = \sum_{n=1}^{+\infty} \left(\frac{\lambda^n \cdot e^{-\lambda}}{n!} \cdot \left((P(\max(Y_{ik}) \leq m | \eta_i))^n - (P(\max(Y_{ik}) < m | \eta_i))^n \right) \right)$$



Study design

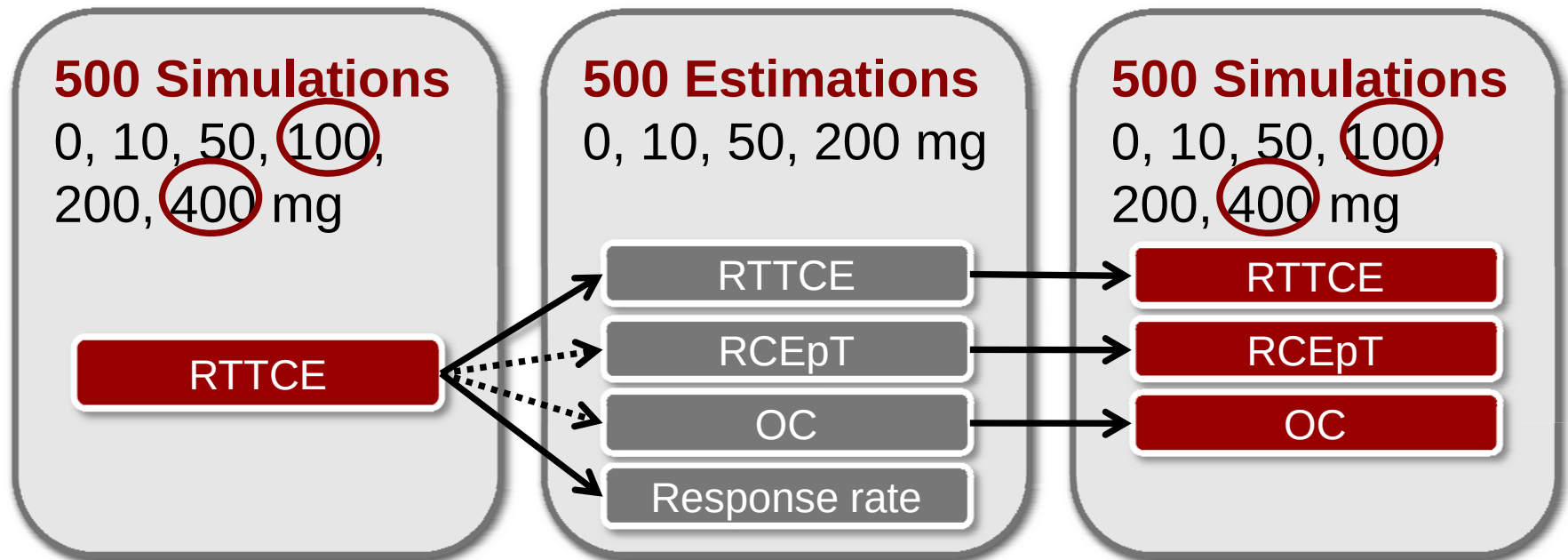
- Mimics Phase II clinical trial
 - **72** individuals
 - **6** parallel dose arms
- Simulation of drug effect (function of C)
 - I_{max} on hazard
 - Linear inhibition on logit
 - Shared IIV
- Simulation of symptoms (acid refluxes)
 - **Time of symptoms:** recorded during **0-12h**
 - **Grade of symptoms:** **Mild, moderate or severe**





Study methodology

- Stochastic Simulations and Estimations (SSE)
- In NONMEM 7[®], with LAPLACIAN LIKE approx.



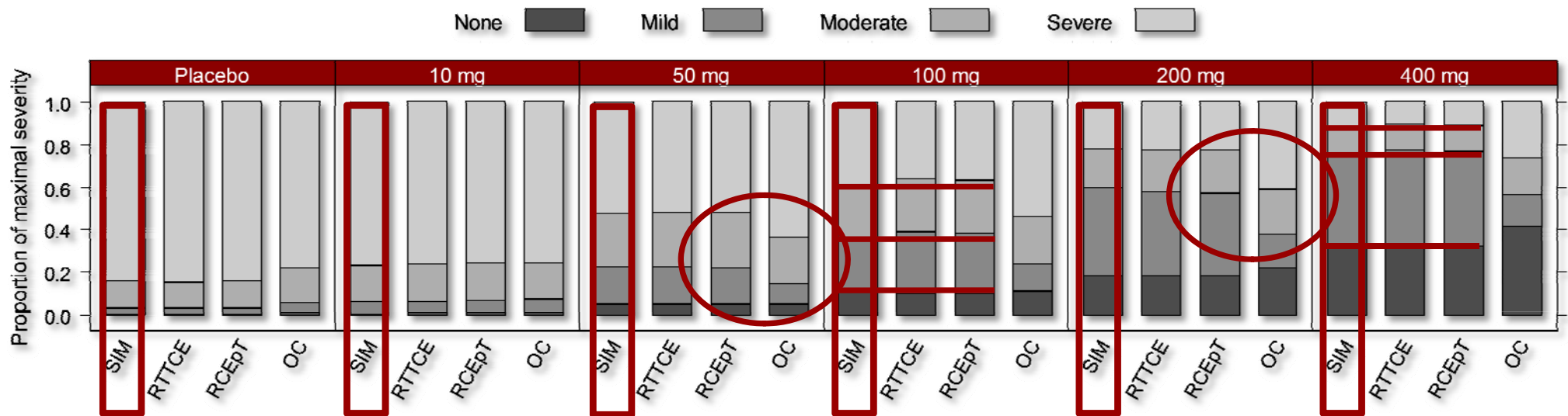
...➤ Data simplified as max per hour



Simulation properties

➤ Maximal reflux grade per patient over 12h

- Favours OC theoretically
- Illustrates OC limitations



Proportions of none, mild, moderate and severe maximums obtained from 100 sets of parameter estimates and simulated on a large sample



Drug effect assessment

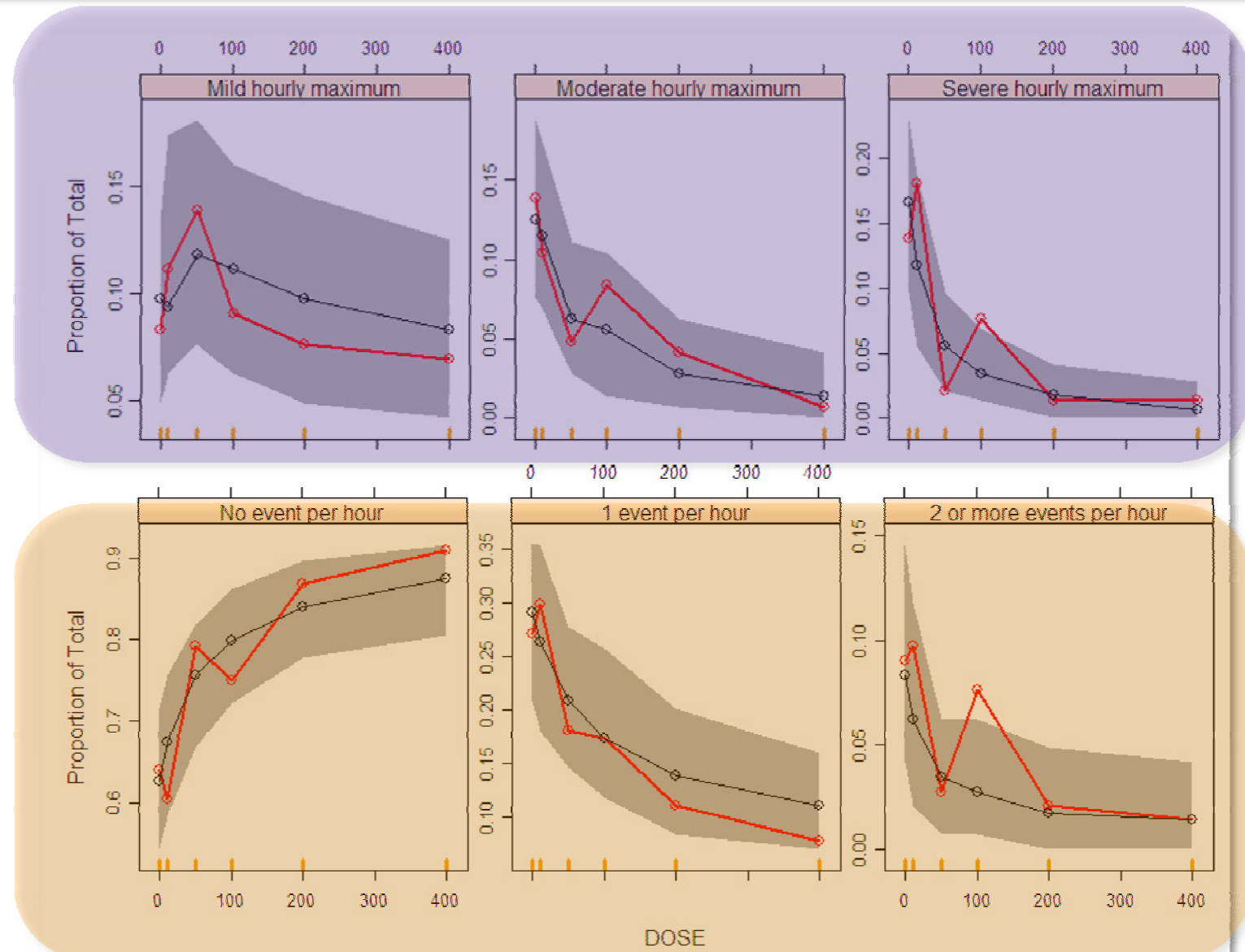
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RCEpT model

-- = median of
original datasets

■ = 95% CI

-- = median of
predictions from 100
simulated samples





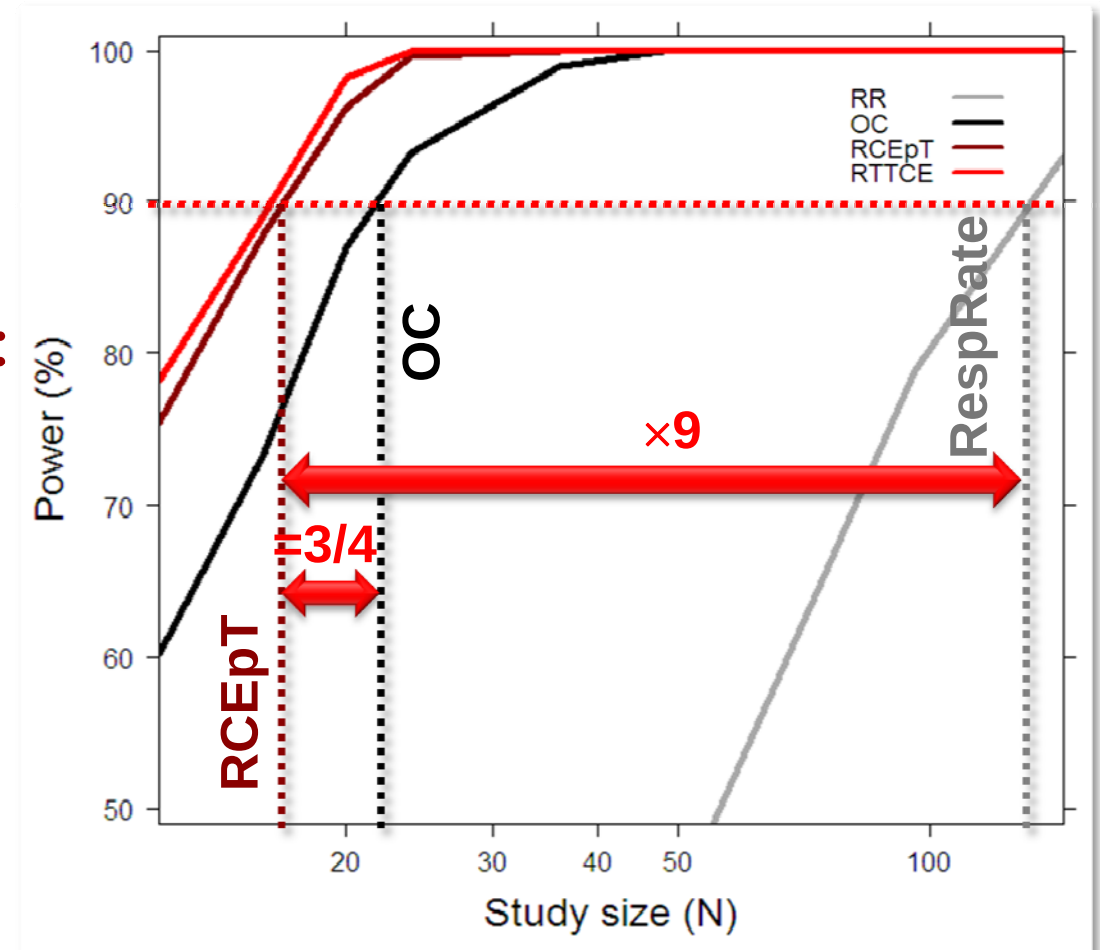
Drug effect detection power

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➤ Chi square test

$$p = 0.01$$

➤ For a Power = 90%:



Response rate definition = severity < 1 during 3 last h



Summary

- Modeling graded symptoms with summarized information
 - ➔ poor description of the events
 - ➔ incomplete drug effect assessment
 - ➔ excessive study sizes
- Modeling simultaneously both severity and frequency of symptoms
 - ➔ good predictive performance
 - ➔ extended simulation capabilities
 - ➔ high power to identify drug effects

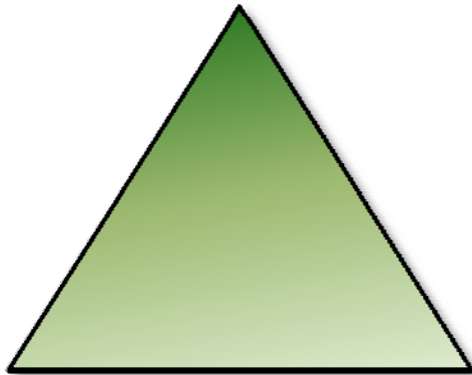


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Bleeding episodes

Asthma crises



Rhinitis



Epilepsy seizures



<http://en.wikipedia.org/wiki/Fractal>

Nicotine craving

Sleep apnoea



Acknowledgments

- ❖ UCB Pharma, for research funds
- ❖ Uppsala colleagues, for research fun
- ❖ You, for your attention
And...questions?